# Mathletics NSW Curriculum

Understanding Practice and Fluency (UPF)







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### **Understanding Practice and Fluency (UPF)**

### **Number and Algebra**

		Quest: Whole numb	per - counting (1)
Learning Journey	Steps	Spine Nodes	Subnodes
	1	Counting forwards in ones within 100	<ul><li>count forwards in ones from any number up to 100</li><li>identify missing numbers on a number line up to 100</li></ul>
Count forwards and backwards	2	Counting backwards in ones within 100	<ul><li>count backwards in ones from any number within 100</li><li>identify missing numbers on a number line up to 100</li></ul>
to 100	3	Counting forwards and backwards in ones within 100	<ul> <li>count forwards and backwards in ones from any number up to 100</li> <li>identify missing numbers on a number line up to 100</li> </ul>
Find numbers before and after to 100	1	Identifying numbers before and after up to 100	<ul> <li>identify the number that comes before a given number up to 100;- describe this number as 'one more than'</li> <li>identify the number that comes after a given number up to 100;- describe this numbers as 'one less than'</li> <li>identify the number that comes before or after a given number up to 100;- describe this number as 'one more than' or 'one less than'</li> </ul>
Identify ordinal numbers up to 31st	1	Using ordinal numbers up to 31st	read, write and use ordinal numbers in everyday situations, eg when reading a calendar
Co	ount col	lections to 100 by partitioning n	umbers using place value (ACMNA014)
Count collections 0 to 100	1	Counting collections 0 to 100	count everyday concrete materials using one-to-one correspondence
Use groups of 10 to count large collections	1	Using groups of ten to count large collections	<ul> <li>count by systematically organising collections into groups of tens and then skip counting in tens</li> <li>record and describe the count, eg 'there are 4 groups o ten and 3 left over'</li> </ul>
ldentify place value up to 2 digits	1	Identifying the place value of digits in 2-digit numbers	<ul> <li>write the numeral for a 2-digit number modelled using place value equipment</li> <li>identify the digit in the tens or ones column for a given 2-digit number</li> </ul>
Solve problems using place value up to 2 digits	1	Solving problems using place value with 2-digit numbers	<ul> <li>identify, record and model a number using place value clues, eg 'a 5 in the tens and a 2 in the ones' as 52</li> <li>create the smallest and largest possible number using digits</li> </ul>
Partition 2-digit numbers (standard)	1	Using place value to partition 2-digit numbers	<ul> <li>use place value equipment and models, eg tens frames to partition a given 2-digit number into tens and ones</li> <li>model and describe a 2-digit number in both words and numerals, eg 53 as '5 tens and 3 ones' or '50 and 3'</li> <li>model a number expressed in words, eg '6 tens and 2 ones'</li> </ul>
Partition 2-digit numbers (non- standard)	1	Partitioning 2-digit numbers using non-standard partitioning	<ul> <li>use place value equipment and models, eg tens frames to partition a given 2-digit number using non-standard partitioning, eg 35 as 2 tens and 15 ones</li> <li>model and identify a number from non-standard partitioning, eg recognise 4 tens and 13 ones as 53</li> </ul>

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### **Understanding Practice and Fluency (UPF)**

			(ACMNA013)
		Quest: Wh	ole number – place value (1)
Learning Journey	Steps	Spine Nodes	Subnodes
	1		<ul> <li>write the numerals and words, eg 'fifty three' for a 2-digit number represented using place value equipment or using pictures, drawings</li> </ul>
Model, read, write and count			• count in tens and then ones along a partially labelled number line to place a number, up to 100
2-digit numbers	2	Counting in tens and ones	• use clues to identify a number on a number line, eg 3 tens and 7 ones as 37
			<ul> <li>count in tens and ones on a partially labelled number chart to position a number up to 100</li> </ul>
Compare and	1	Comparing numbers to 100	<ul> <li>model and compare two 2-digit numbers using place value equipment</li> <li>compare two 2-digit numbers</li> </ul>
order numbers to 100	2	Ordering numbers to 100	<ul> <li>order up to 4 consecutive numbers within 100 from smallest to largest or largest to smallest; explain the reason for the order giver</li> <li>order up to 4 non-consecutive numbers within 100 from smallest to largest or largest to smallest; explain the reason for the order giver</li> </ul>
Round numbers up to 100	1	Rounding numbers up to 100 to the nearest 10	<ul> <li>model a 2-digit number and recognise which ten it is nearer to;     explain reasoning</li> <li>round a 2-digit number to the nearest 10;- explain reasoning</li> </ul>
Solve problems with 2-digit numbers on number lines	1	Solving place value problems with 2-digit numbers	<ul> <li>use clues to identify numbers on a number line, eg use a number line to find out how many jumps of 10 from 12 make 52</li> <li>use clues to identify a number on a number chart starting from any number, eg starting from 14 count on 4 groups of 10 to identify the new number</li> </ul>
Recognise Australian coins	1	Recognising coins   Australia	<ul><li>recognise the monetary value of Australian coins</li><li>order Australian coins by value</li></ul>
Develop cor	nfidence	with number sequer	nces from 100 by ones from any starting point (ACMNA012)
		Quest: W	hole number - counting (2)
Count in ones up to 1000	1	Counting forwards in ones within 1000	<ul> <li>count forwards in ones between 100 and 1000, starting from any number</li> <li>identify missing numbers in the hundreds on a number line up to 1000</li> </ul>
	2	Counting backwards in ones within 1000	<ul> <li>count backwards in ones between 100 and 1000, starting from any number</li> <li>identify missing numbers in the hundreds on a number line up to 1000</li> </ul>
	3	Counting forwards and backwards in ones within 1000	<ul> <li>count forwards and backwards in ones between 100 and 1000, starting from any number</li> <li>identify missing numbers in the hundreds on a number line up to 1000</li> </ul>



### **Understanding Practice and Fluency (UPF)**

Develop confidence with number sequences from 100 by ones from any starting point (ACMNA012)			
Quest: Whole number – counting (2)			
Learning Journey	Steps	Spine Nodes	Subnodes
Identify numbers before and after up to 1000	1	Identifying numbers before and after within 1000	<ul> <li>identify the number that comes before a given 3-digit number up to 1000;- describe this number as 'one more than'</li> <li>identify the number that comes after a given 3-digit number up to 1000;- describe this numbers as 'one less than'</li> <li>identify the number that comes before or after a given 3-digit number up to 1000;- describe this number as 'one more than' or 'one less than'</li> </ul>
R	ecogni	se, model, represent a	and order numbers to at least 1000 (ACMNA027)
		Quest: Wh	ole number - place value (2)
	1	Reading and writing 3-digit numbers using numeral only	read a given 3-digit number in words, eg 456 says 'four hundred and fifty-six'
Read and represent 3-digit	2	Reading and writing 3-digit numbers using words and numerals	<ul> <li>write a given 3-digit number in words, eg 456 as four hundred and fifty-six</li> <li>write the numerals for a 3-digit number given in words</li> </ul>
numbers	3	Representing 3-digit numbers using words, numerals and objects	<ul> <li>model a given 3-digit number using concrete materials, pictures or drawings</li> <li>write the numerals and words, eg 'two hundred and fifty-three' for a 3-digit number represented using place value equipment or using pictures and drawings</li> </ul>
1 Compare and	1	Comparing numbers to 1000	<ul> <li>model and compare two 3-digit numbers using place value equipment</li> <li>compare two 3-digit numbers;- describe as 'more than' or 'less than', 'smaller than', greater than'</li> </ul>
order numbers to 1000	2	Ordering numbers to 1000	<ul> <li>order up to 4 consecutive numbers within 1000 in ascending order or descending order;- explain the reason for the order given</li> <li>order up to 4 non-consecutive numbers within 1000 in ascending order;- explain the reason for the order given</li> </ul>
Investigate nu			ose increasing and decreasing by twos, threes, fives and tens
	- irom		en moving to other sequences (ACMNA026) nole number - sequences (2)
			loie Humber - sequences (2)
Identify, describe and continue number sequences	1	Identifying and describing number patterns (1s, 2s, 5s, 10s, 25s) up to 100	• identify and describe growing and shrinking patterns generated by the repeated addition or subtraction of 1s, 2s, 5s, 10s or 25s on a number line or number chart
	2	Counting forwards and backwards by 2s, 3s and 5s from any starting point	<ul> <li>count forwards and backwards by 2s from any starting point</li> <li>count forwards and backwards by 5s from any starting point</li> <li>count forwards and backwards by 3s from any starting point</li> <li>identify sequences in 2s, 3s, or 5s in a number chart</li> </ul>



### **Understanding Practice and Fluency (UPF)**

Quest: Whole number - sequences (2)			
Learning Journey	Steps	Spine Nodes	Subnodes
	1	Counting in tens with 2-digit numbers, on the decade, using number lines and charts	<ul> <li>count forwards and backwards in tens, on the decade, with 2-digit numbers using number lines</li> <li>count forwards and backwards in tens, on the decade, with 2-digit numbers and number charts</li> </ul>
Count in tens with 2- and	2	Counting in tens with 3-digit numbers using number lines and charts	<ul> <li>count forwards and backwards in tens, on the decade, with 3-digit numbers using number lines</li> <li>count forwards and backwards in tens, on the decade, with 3-digit numbers using number charts</li> </ul>
3-digit numbers  3	3	Counting in tens from any number with 2-digit numbers	<ul> <li>count forwards and backwards in tens, off the decade, with 2-digit numbers using number lines</li> <li>count forwards and backwards in tens, off the decade, with 2-digit numbers using number charts</li> </ul>
	4	Counting in tens from any number with 3-digit numbers	<ul> <li>count forwards and backwards in tens, off the decade, with 3-digit numbers using number lines</li> <li>count forwards and backwards in tens, off the decade, with 3-digit numbers using number charts</li> </ul>
Find numbers	1	Finding numbers 10 before and 10 after a 2-digit number on the decade	find the number '10 before' or '10 after' a given 2-digit on the decade number using number lines and number charts
10 before and 10 after up to 1000	2	Finding numbers 10 before and 10 after a 2-digit and 3-digit number off the decade	find the number '10 before' or '10 after' a given 2-digit or 3-digit number off the decade, using number lines and number charts
Group, partit	ion and		of up to 1000 in hundreds, tens and ones to facilitate more not counting (ACMNA028)
		Quest: Whole i	number - partition and group (2)
Identify place value in 3-digit numbers	1	Identifying the place value of digits in 3-digit numbers	<ul> <li>write the numeral for a 3-digit number modelled using place value equipment</li> <li>identify the digit in the hundreds, tens or ones column for a given 3-digit number</li> <li>recognise that the value of the digit is determined by its place value, eg in 689 the digit 8 has a place value of tens and a total value of 80</li> <li>identify, record and model a number using place value clues, eg 'a 5 in the hundreds and a 2 in the ones' as 502</li> <li>recognise the role of zero as a placeholder</li> <li>create the smallest and largest numbers possible using 3 digits</li> </ul>



### **Understanding Practice and Fluency (UPF)**

Group, parti	Group, partition and rearrange collections of up to 1000 in hundreds, tens and ones to facilitate more efficient counting (ACMNA028)				
		Quest: Whole number	- partition and group (2)		
Learning Journey	Steps	Spine Nodes	Subnodes		
Count in hundreds, tens and ones	1	Counting in hundreds, tens and ones	<ul> <li>count in hundreds, tens and then ones along a partially labelled number line to place a number between 100 and 1000</li> <li>use clues to identify a number between 100 and 1000 on a number line, eg 3 hundreds, 5 tens and 7 ones as 357</li> <li>count in hundreds, tens and ones on a partially labelled number chart to position a number between 100 and 1000</li> </ul>		
Partition 3-digit numbers (standard)	1	Using place value to partition 3-digit numbers	<ul> <li>use place value equipment to partition a given 3-digit number into hundreds, tens and ones</li> <li>describe a 3-digit number using words, eg 523 as '5 hundreds, 2 tens and 3 ones'</li> <li>write a 3-digit number in expanded notation, eg 523 as 500 + 20 + 3</li> <li>write the numeral for a number represented by expanded notation</li> <li>recognise zero as a placeholder</li> </ul>		
Partition 3-digit numbers (non- standard)	1	Partitioning 3-digit numbers using non-standard partitioning	<ul> <li>use place value equipment to partition a given 3-digit number using non-standard partitioning, eg 375 as 2 hundreds and 175 ones or 200 + 175</li> <li>model and identify a number from non-standard partitioning, eg recognise 3 hundreds, 4 tens and 27 ones or 300 + 40 + 27 as 367</li> </ul>		
Round numbers up to 1000 to the nearest 100	1	Rounding numbers up to 1000 to the nearest 100	<ul> <li>model a 3-digit number and recognise which hundred it is nearer to;- explain reasoning</li> <li>round a 3-digit number to the nearest 100, recognise the digit in the tens column as the key digit</li> </ul>		
Count and c	order sm	nall collections of Australian co	oins and notes according to their value (ACMNA034)		
		Quest: Whole nu	ımber - money (2)		
	1	Recognising notes and coins   Australia	<ul> <li>recognise the value of all Australian coins and notes</li> <li>recognise that there are 100 cents in 1 dollar</li> <li>recognise and generate combinations of the same and different denominations of coins that make \$1</li> </ul>		
	2	Counting totals using notes and coins of the same denomination   Australia	determine the total amount of money by counting the value of notes of the same denomination		
Count and order	3	Using notes and coins to make amounts   Australia#values up to \$100 only	combine amounts of notes and coins to make a given amount of money shown in dollars and cents (no decimal point)		
Australian notes and coins	4	Calculating totals of notes and coins and record using symbols   Australia#values up to \$100 only	• calculate the total value of a group of notes and coins and record this value in dollars and cents using the correct symbols (no decimal point)		
	5	Recognising that the same value can be created using different combinations of coins   Australia#values up to \$100 only	generate and recognise different combinations of coins that have the same value (combining coins of the same denominations and different denominations) and record these using the symbol c		
	J	Recognising that the same value can be created using different combinations of notes   Australia#values up to \$100 only	<ul> <li>generate and recognise different combinations of notes that have the same value (combining notes of the same denominations and different denominations) and record these using the symbol \$</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

Represent and solve simple addition and subtraction problems using a range of strategies, including counting on, partitioning and rearranging parts (ACMNA015)

counting on, partitioning and rearranging parts (ACMNA015)					
	Quest: Addition and subtraction (1)				
Learning Journey	Steps	Spine Nodes	Subnodes		
	1	Modelling and recording combinations that add up to 5	<ul> <li>model and record with numerals, the patterns of numbers that add to 5</li> <li>find the missing number to add to 5 when one number is given</li> </ul>		
Model and	2	Modelling and recording combinations that add up to 6	<ul> <li>model and record with numerals, the patterns of numbers that add to 6</li> <li>find the missing number to add to 6 when one number is given</li> </ul>		
record combinations that make 5 – 9	3	Modelling and recording combinations that add up to 7	<ul> <li>model and record with numerals the patterns of numbers that add to 7</li> <li>find the missing number to add to 7 when one number is given</li> </ul>		
	4	Modelling and recording combinations that add up to 8	<ul> <li>model and record the patterns of numbers that add to 8</li> <li>find the missing number to add to 8 when one number is given</li> </ul>		
	5	Modelling and recording combinations that add up to 9	<ul> <li>model and record the patterns of numbers that add to 9</li> <li>find the missing number to add to 9 when one number is given</li> </ul>		
Model and record combinations that make 11 – 20	1	Modelling and recording combinations that add to numbers from 11 to 20	<ul> <li>model and recognise the relationship between numbers to 10 and numbers to 20 using models eg tens frames eg 5 + 4 = 9 and 15 + 4 = 19</li> <li>use the additions to 10 to record the combinations of numbers that add to between 11 and 20</li> </ul>		
Recognise and recall bonds to 10	1	Recognising and recalling bonds to 10	<ul> <li>recognise pairs of numbers that add to 10</li> <li>find the missing number to add to 10 given one number</li> <li>recall and record the bonds that add to 10</li> </ul>		
Add zero to a number (up to 20)	1	Adding zero to a number (up to 20)	investigate and recognise the effect of adding zero to a number; generalise that adding zero does not change the number		
Introduce the commutative property of addition	1	Introducing the commutative property of addition	<ul> <li>represent and solve an addition problem both ways using concrete materials and models eg 5 + 4 or 4 + 5</li> <li>swap an addition problem around so the larger number comes first and add by counting on (within 20)</li> </ul>		
Add and subtract by counting on/ back up to 100	1	Counting on and back to add and subtract up to 100	count on or back to add and subtract with numbers up to 100		
Add doubles up	1	Recalling doubles up to 10	recall doubles and add doubles to 10 fluently		
to 20	2	Adding doubles up to 20	add doubles with and without using models (up to 20)		
Add and subtract	1	Adding doubles or near doubles	<ul> <li>solve addition problems using doubles, eg 4 + 3 + 4 as 4 + 4 + 3</li> <li>model and solve addition problems with near doubles, eg 5 + 7 as 5 + 5 + 2 = 12</li> </ul>		
near doubles	2	Subtracting using doubles	• model and solve subtraction problems using doubles, eg 14 - 7 as 7 + 7 = 14 or 15 - 8 as 7 + 7 + 1 = 15		



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

Represent and solve simple addition and subtraction problems using a range of strategies, including counting on, partitioning and rearranging parts (ACMNA015)

counting on, partitioning and rearranging parts (ACMNA015)					
	Quest: Addition and subtraction (1)				
Learning Journey	Steps	Spine Nodes	Subnodes		
Find the difference between 2 numbers (to 20)	1	Finding the difference between 2 numbers (up to 20)	<ul> <li>represent two numbers using concrete materials and a number line eg place value equipment and a number line;- compare the materials and count from the smaller number to find the difference</li> <li>find the missing number in an addition problem eg 4 + ? = 9</li> <li>solve word problems which involve finding the difference between two numbers</li> </ul>		
Add compatible numbers (doubles or bonds to 10)	1	Adding using compatible numbers and manipulatives for support	• find compatible numbers (bonds to 10 or doubles) to add a list of 1-digit numbers, eg 6 + 3 + 4 + 3		
1	1	Bridging to ten to add a 1-digit and 1-digit number using models and diagrams	<ul> <li>add to the nearest ten first then add the rest, using models for support, eg 8 + 7 as 8 + 2 = 10 and 10 + 5 = 15</li> <li>record the strategy of bridging to ten using numbers and/or models, eg number lines</li> </ul>		
Add and subtract	2	Bridging to ten to add a 2-digit and 1-digit number using models and diagrams	<ul> <li>add to the nearest ten first then add the rest, using models for support, eg 28 + 7 as 28 + 2 = 30 and 30 + 5 = 35</li> <li>record the strategy of bridging to ten using numbers and/or models, eg number lines</li> </ul>		
using bridging to 10 up to 100	3	Bridging to ten to subtract a 1-digit number from a 2-digit number using models and diagrams	<ul> <li>subtract to the nearest ten first then subtract the rest, using models for support, eg 32 - 6 as 32 - 2 = 30 and 30 - 4 = 26</li> <li>record the strategy of bridging to ten using numbers and/or models eg number lines</li> </ul>		
	4	Bridging to ten to mentally add or subtract a 1-digit and 2-digit number	<ul> <li>use bridging to ten to solve addition and subtraction problems with 1- and 2-digit numbers</li> <li>use bridging to ten to solve addition and subtraction problems with 1- and 2-digit numbers where the change is unknown, eg 25 + ? = 32</li> </ul>		
Add using place	1	Adding 2-digit and 1-digit numbers using place value partitioning with models (split strategy)	• model and solve the addition of a 2-digit and 1-digit number using place value equipment, eg use base 10 blocks to show 25 + 8 as 20 + 5 + 8 and then 20 + 13 = 33		
value up to 100	2	Adding 2-digit and 1-digit numbers using place value understanding (split strategy)	mentally solve the addition of a 2-digit and 1-digit number using place value partitioning		
Solve addition and subtraction word problems	1	Creating and solving simple addition and subtraction word problems in context (within 20)	<ul> <li>represent a word problem as an addition or subtraction number sentence</li> <li>solve a variety of simple addition and subtraction word problems in context, eg find the difference, find the sum, change unknown, start unknown simple addition and subtraction word problems</li> <li>explain and compare strategies used to solve addition and subtraction word problems</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

Represent a	and solv		raction problems using a range of strategies, including and rearranging parts (ACMNA015)	
Quest: Addition and subtraction (1)				
Learning Journey	Steps	Spine Nodes	Subnodes	
	1	Exploring equality and inequality (up to 10)	<ul> <li>create a set in which the number of objects is greater than, less than or equal to the number of objects in a given set</li> <li>determine if 2 given concrete sets are equal or unequal and explain the process used</li> </ul>	
Explore equality and inequality up to 10 and 20	2	Exploring equality and inequality (up to 20)	<ul> <li>create a set in which the number of objects is greater than, less than or equal to the number of objects in a given set</li> <li>determine if 2 given concrete sets are equal or unequal and explain the process used</li> </ul>	
	3	Recognising equality in addition and subtraction number sentences using objects and models for support	<ul> <li>determine if equations involving addition or subtraction are true or false, eg 6 = 6, 7 = 8 - 1, 5 + 2 = 2</li> </ul>	
	Expl	ore the connection betwee	n addition and subtraction (ACMNA029)	
		Quest: Addition	on and subtraction (2)	
Find fact families for addition and subtraction	1	Finding fact families for addition and subtraction (between 10 and 20)	• find the other three facts given one fact, eg 12 + 5 = 17	
	2	Finding fact families for addition and subtraction (within 30)	• find the other three facts given one fact, eg 12 + 5 = 17	
Solve simple	additio		s using a range of efficient mental and written strategies	
			CMNA030)	
Use mental strategies to add and subtract (to 100)	1	Adding with 1 digit to/from 2-digit numbers using efficient mental strategies (max sum 100)	select, use and record an efficient strategy to solve an addition problem, eg counting on, bridging to ten, split strategy, jump strategy, place value	
	2	Subtracting with 1 digit to/ from 2-digit numbers using efficient strategies	• select, use and record an efficient strategy to solve the subtraction of a 1-digit number from a 2-digit number, eg counting back, bridging to ten, inverse relationship with addition, jump strategy (max sum 100)	
	3	Adding and subtracting 1 digit to/from 2-digit numbers using efficient strategies (max sum 100)	<ul> <li>select, use and record an efficient strategy to solve an addition or subtraction problem (max sum 100)</li> </ul>	
Add and subtract	1	Adding tens to a 2-digit number using models and/or equipment for support	• add ten and multiples of ten to a give 2-digit number, eg 36 + 20 = 56 (max sum 100)	
tens from a 2-digit number	2	Subtracting tens from a 2-digit number using models and/or equipment for support	• subtract ten and multiples of ten to a give 2-digit number, eg 36 - 20 = 16 (max sum 100)	



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

Solve simple addition and subtraction problems using a range of efficient mental and written strategies (ACMNA030)

	(ACMNA030)				
	Quest: Addition and subtraction (2)				
Learning Journey	Steps	Spine Nodes	Subnodes		
	1	Introducing the addition of two 2-digit numbers using place value partitioning on a number line (jump strategy)	• use an empty number line to model and solve the addition of two 2-digit numbers, eg solve 35 + 43 as 35 + 10 + 10 + 10 + 10 = 75 then 75 + 1 + 1 + 1 = 78 (max sum 100)		
Introduce place value to add and subtract (to 200)	2	Introducing subtraction of two 2-digit numbers using place value partitioning on a number line (jump strategy)	<ul> <li>use an empty number line to model and solve the subtraction of two 2-digit numbers by counting back, eg solve 52 – 23 as 52 – 10 – 10 = 32 then 32 – 1 – 1 – 1 = 29 (max sum 100)</li> </ul>		
	3	Introducing the mental addition and subtraction of two 2-digit numbers using place value understanding (jump strategy)	mentally solve the addition or subtraction of two 2-digit numbers using place value partitioning (max sum 100)		
	1	Adding two 2-digit numbers using place value partitioning on a number line (jump strategy)	• use an empty number line to model and solve the addition of two 2-digit numbers, eg solve 35 + 43 as 35 + 40 = 75 then 75 + 3 = 78		
Use place value	2	Subtracting two 2-digit numbers using place value partitioning on a number line (jump strategy)	<ul> <li>use an empty number line to model and solve the subtraction of two 2-digit numbers by counting back, eg solve 52 – 23 as 52 – 20 = 32 then 32 – 3 = 29 (max sum 100)</li> </ul>		
to add and subtract (to 200)	3	Adding tens and ones using place value equipment and a split strategy (no crossing tens)	• model and solve the addition of two 2-digit numbers represented horizontally using place value equipment (not crossing ten), eg use base 10 blocks to model 34 + 12 as 30 + 10 and 4 + 2 (max sum 100)		
	4	Subtracting tens and ones using place value equipment and a split strategy (no crossing tens)	• model and solve the subtraction of two 2-digit numbers represented horizontally using place value equipment (not crossing ten), eg use base 10 blocks to model 34 - 12 as 30 - 10 and 4 - 2		
Use place value (no models) to add and subtract	1	Adding and subtracting tens and ones mentally using place value understanding (no crossing tens)	<ul> <li>solve the addition or subtraction of two 2-digit numbers represented horizontally (no crossing ten)</li> <li>check calculations by doing the inverse operation</li> </ul>		
	2	Adding and subtracting two 2-digit numbers mentally using place value understanding	<ul> <li>mentally solve the addition or subtraction of two 2-digit numbers using a jump strategy, eg solve 35 + 43 as 35 + 40 = 75 then 75 + 3 = 78 (max sum 100)</li> <li>check calculations by doing the inverse operation</li> </ul>		
Use place value to add (crossing a 10)	1	Adding two 2-digit numbers using place value models (split strategy)	<ul> <li>use place value equipment to model and solve the addition of two 2-digit numbers using standard partitioning, eg 37 + 45 as 30 + 40 and 5 + 7</li> </ul>		
Subtract using addition	1	Subtracting two 2-digit numbers using addition	<ul> <li>recognise and model the inverse relationship between addition and subtraction</li> <li>rearrange a subtraction problem into an addition problem with change unknown and then use an effective addition strategy to solve, eg using a jump strategy to solve 54 – 38 as 38 +? = 54 on a number line</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

Solve simple	addition		s using a range of efficient mental and written strategies CMNA030)
		Quest: Addition	on and subtraction (2)
Learning Journey	Steps	Spine Nodes	Subnodes
Solve word problems with start or change unknown	1	Solving addition and subtraction word problems where either the start or the is change unknown (1-digit and 2-digit numbers)	<ul> <li>solve word problems where the start is unknown, eg 'Anna had some plums. Sam gave her 5 more. Now she has 13 plums. How many did she have to start with?'</li> <li>solve word problems where the change is unknown, eg 'Anna has 5 plums. How many more does she need to have 13?' or 'Anna had 13 plums. She gave some to Sam. Now she has 7 plums. How many plums did she give to Sam?'</li> <li>solve word problems involving comparisons, eg Anna has 13 plums. Sam has 7 plums. How many more plums does Anna have? or Anna has 7 more plums than Sam. Sam has 5 plums. How many</li> </ul>
	1	Adding 10 then compensating to add a single digit (7, 8 or 9)	<ul> <li>add 10 first then subtract to compensate using models for support, eg, 6 + 9 as 6 + 10 = 16 then 16 -1 = 15</li> <li>record the strategy adding 10 then compensating to add a single</li> </ul>
Add and subtract using rounding and		to a 1- or 2-digit number  Subtracting 10 then	<ul> <li>digit (7, 8 or 9) using numbers and/or models, eg, number lines</li> <li>subtract 10 first then add to compensate using models for support, eg, 15 - 9 as 15 - 10 = 5 then 5 + 1 = 6</li> </ul>
compensating	2	compensating to subtract a single digit (7, 8 or 9) from a 2-digit number	<ul> <li>record the strategy subtracting 10 then compensating to subtract a single digit (7, 8 or 9) using numbers and/or models, eg, number lines</li> </ul>
	SI	kip count by twos, fives and	tens starting from zero (ACMNA012)
		Quest: Mult/o	div - skip counting (1)
	1	Using skip counting by 2s from zero up to 20	• use concrete materials, models, drawings, number lines/charts to skip count by 2s from zero
Skip count by 2s	2	Using skip counting by 2s from any multiple of 2 up to 50	use concrete materials, models, drawings, number lines/charts to skip count by 2s from any multiple of 2
Chip court by F-	1	Using skip counting by 5s from zero up to 20	• use concrete materials, models, drawings, number lines/charts to skip count by 5s from zero
Skip count by 5s	2	Using skip counting by 5s from zero up to 50	• use concrete materials, models, drawings, number lines/charts to skip count by 5s from zero



### **Understanding Practice and Fluency (UPF)**

Skip count by twos, fives and tens starting from zero (ACMNA012)			
		Quest: Mult	t/div - skip counting (1)
Learning Journey	Steps	Spine Nodes	Subnodes
	1	Counting by skip counting forwards by 10s from zero up to 50	use concrete materials, models, drawings, number lines/charts to skip count by 10s from zero
	2	Counting by skip counting backwards by 10s from numbers up to 50	use concrete materials, models, drawings, number lines/charts to skip count backwards by 10s
	3	Counting by skip counting forwards by 10s from zero up to 100	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count by 10s from zero</li> <li>recognise an error in the skip counting sequence</li> </ul>
Skip count by 10s	4	Counting by skip counting backwards by 10s from up to 100	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count backwards by 10s</li> <li>recognise an error in the skip counting sequence</li> </ul>
	5	Counting by skip counting forwards or backwards by 10s from zero up to 100	use concrete materials, models, drawings, number lines/charts to skip count forwards and backwards by 10s from zero
	5	Counting by skip counting forwards or backwards by 10s from zero up to 100	recognise an error in the skip counting sequence
	1	Counting by skip counting in 2s, 5s, 10s from zero to 50	• use concrete materials, models, drawings, number lines/charts to skip count by 2s, 5s, 10s from zero
Skip count by 2s,	2	Finding 'how many' objects using skip counting by 2, 5 or 10 up to 50	use skip counting by 2, 5 or 10 to determine 'how many' when objects are grouped or shared equally
5s and 10s	3	Counting by skip counting in 2s, 5s, 10s from zero to 100	• use concrete materials, models, drawings, number lines/charts to skip count by 2s, 5s, 10s from zero
	4	Finding 'how many' objects using skip counting by 2, 5 or 10 up to 100	use skip counting by 2, 5 or 10 to determine 'how many' when objects are grouped or shared equally
	Мос	del and use equal groups	of objects as a strategy for multiplication
			t/div – equal groups (1)
Use groups and skip counting to solve problems	1	Grouping and skip counting to solve simple multiplication problems	<ul> <li>record both the number of groups and the number in each group by completing stem sentences, eg '5 children with 2 marbles each makes 10 marbles altogether'</li> </ul>
Recognise and represent division as grouping into equal sets (ACMNA032)			
Share objects to divide	1	Sharing objects to divide up to 20	<ul> <li>share a collection of objects equally into a given number of groups using concrete materials, models or drawings, eg '15 balloons shared by 3 children, how many balloons will they each get?'</li> <li>relate to multiplication by recombining the groups, eg by counting or skip counting to check the total number of objects</li> <li>solve simple division problems by sharing into equal groups</li> <li>explain how to share a group of objects to divide and describe the number of groups and the number in each group using stem sentences;- when sharing into 2 groups students may refer to one group as being 'one half'</li> </ul>



### **Understanding Practice and Fluency (UPF)**

	Recog	nise and represent division	on as grouping into equal sets (ACMNA032)	
	Quest: Mult/div – equal groups (1)			
Learning Journey	Steps	Spine Nodes	Subnodes	
Share objects to divide	2	Sharing objects to divide (with leftovers) up to 20	<ul> <li>share a collection of objects equally into a given number of groups using concrete materials, models or drawings;- recognise that there are 'leftovers'</li> <li>describe the part left over when a collection cannot be shared equally</li> <li>describe the number of groups and the number in each group</li> </ul>	
Group objects to divide	1	Grouping objects to divide (groups of 2, 5 or 10)	<ul> <li>share a collection of objects equally into groups of a given size using concrete materials, models or drawings, eg 'there are 15 balloons tied into bunches of 5, how many bunches of balloons are there?'</li> <li>relate to multiplication by recombining the groups, eg skip counting to check the total number of objects</li> <li>solve simple division problems by grouping objects equally</li> <li>describe the number of groups and the number in each group; when sharing into 2 groups students may refer to one group as being 'one half'</li> </ul>	
	2	Grouping objects to divide (with leftovers)	<ul> <li>share a collection of objects equally into groups of a given size using concrete materials, models or drawings;- recognise that there are 'leftovers'</li> <li>describe the part left over when a collection cannot be shared equally</li> <li>describe the number of groups and the number in each group;- when sharing into 2 groups students may refer to one group as being 'one half'</li> </ul>	
Recogn	ise and	represent multiplication	as repeated addition, groups and arrays (ACMNA031)	
		Quest: Mult/div - r	models, repeated addition (2)	
Use repeated addition to multiply	1	Using repeated addition to multiply	<ul> <li>recognise and describe the relationship between, eg 3 groups of 4 as 4 + 4 + 4</li> <li>use empty number lines and number charts to help solve multiplication problems using repeated addition (2s, 5s, 10s, 3s, 4s)</li> <li>explore the use of repeated addition to count in practical situations</li> <li>apply known facts, such as doubles, to repeated addition problems, eg 5 + 5 + 5 + 5 as 10 + 10</li> </ul>	
Explore arrays (no x symbol)	1	Introducing arrays and describing arrays (no x symbol)	<ul> <li>describe simple multiplication problems represented in arrays using '_groups of _' and use 'rows' and 'columns' to describe the parts of the array</li> <li>represent simple multiplication problems using arrays (concrete materials, pictures or diagrams)</li> <li>recognise and describe practical examples of arrays, eg seedling trays, seating arrangements</li> </ul>	
Use the commutative property of multiplication	1	Introducing the commutative law of multiplication	use concrete materials or drawings of groups or arrays to model the commutative law, eg 3 groups of 2 is the same as 2 groups of 3	



### **Understanding Practice and Fluency (UPF)**

Represent d	ivision a		s and solve simple problems using these representations ACMNA032)		
	Quest: Mult-div – equal groups (2)				
Learning Journey	Steps	Spine Nodes	Subnodes		
Divide by aboving	1	Dividing by sharing (up to 50)	<ul> <li>model and solve division problems by equally sharing a collection into a given number of groups or number of columns/rows in an array</li> <li>record answers to division problems using drawings, words and numerals;- complete stem sentences eg 'when _ is shared into _ equal groups there are _ in each group'</li> <li>describe any parts left over when the collection is not able to be equally shared</li> </ul>		
Divide by sharing and grouping	2	Dividing by grouping (up to 50)	<ul> <li>model and solve division problems sharing a collection of objects into groups of a given size, and by arranging it into rows or columns of a given size in an array, eg determine the number of columns in an array when 20 objects are arranged into rows of 4</li> <li>record answers to division problems using drawings, words and numerals;- complete stem sentences, eg 'when _ is shared into _ equal groups there are _ in each group'</li> <li>describe an parts left over when the collection is not able to be equally shared</li> </ul>		
Use repeated subtraction to divide	1	Using repeated subtraction to divide	<ul> <li>solve division problems (group size known, number of groups unknown) using repeated subtraction and concrete materials, models or drawings of groups or arrays</li> <li>use an empty number line or number chart to represent division problems as repeated subtraction (group size known number of groups unknown)</li> <li>explore the use of repeated subtraction in practical situations</li> </ul>		
Solve simple multiplication problems (2,5,10x)	1	Solving simple multiplication and division problems using models and manipulatives (2x, 5x, 10x)	<ul> <li>recognise a simple word problem as a division or multiplication problem</li> <li>record answers to multiplication and division problems using drawings, words and numerals, eg '2 rows of 5 is 10'</li> </ul>		
Re	cognise	and describe one-half as	one of two equal parts of a whole (ACMNA016)		
		Quest: Frac	ctions and decimals (1)		
Find half of a set or quantity (no symbols)	1	Finding half of a set or quantity (no symbols)	<ul> <li>find half of a set using equal sharing</li> <li>find halves of quantities (up to 10)</li> <li>find the whole from a half</li> </ul>		
Find half of a set or quantity (symbols)	1	Finding half of a set or quantity (symbols used)	<ul> <li>find half of a set using equal sharing</li> <li>find halves of quantities (up to 10)</li> <li>find the whole from one half</li> <li>use the symbols to represent the fraction 1/2</li> </ul>		
Recognis	e and ir		halves, quarters and eighths of shapes and collections (ACMNA033)		
			tions and decimals (2)		
Explore the meaning of fraction symbols	1	Understanding the meaning of fraction symbols (no formal use of numerator or denominator)	<ul> <li>recognise the top number tells how many parts are selected</li> <li>recognise the bottom number tells how many parts the whole has been split into (the name of the fraction / size of the part)</li> <li>recognise the larger denominator = smaller parts as the whole has been split into more pieces</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

Recognise and interpret common uses of halves, quarters and eighths of shapes and collections (ACMNA033)					
	Quest: Fractions and decimals (2)				
Learning Journey	Steps	Spine Nodes	Subnodes		
Find quarters of sets or shapes (no symbols)	1	Introducing quarters of objects, sets or shapes (no symbols)	<ul> <li>recognise objects, shapes or set shared into 4 equal parts</li> <li>recognise that the same shape or object can be shared into 4 equal parts in different ways</li> <li>find the whole given quarter(s)</li> <li>use language 'one quarter', 'two quarters' and so on;- use words to describe fractions of sets and quantities eg 'one quarter of 12 is 3'</li> </ul>		
	2	Finding quarters by halving	<ul> <li>find a quarter of a shape or region by halving and halving again</li> <li>find a quarter of a set by halving and halving again, eg, one quarter of 12 is 3, because 1/2 of 12 = 6 and 1/2 of 6 = 3</li> </ul>		
Find quarters of sets or shapes (symbols)	1	Introducing quarters of objects, sets or shapes (symbols used)	<ul> <li>recognise objects, shapes or set shared into 4 equal parts; recognise that the same shape or object can be shared into 4 parts in different ways</li> <li>find 1/4, 2/4 and 3/4 of objects, shapes, lengths or sets</li> <li>find the whole given quarter(s)</li> <li>use symbols to represent fractions: 1/4, 2/4, 3/4, 4/4</li> <li>record quarters of sets as a number sentence, eg 1/4 of 12 = 3</li> </ul>		
Find halves and quarters (no symbols)	1	Finding halves and quarters of objects, shapes or sets (no symbols)	<ul> <li>recognise equivalence</li> <li>find halves and quarters of objects and shapes</li> <li>find halves and quarters of sets</li> <li>find the whole from a part</li> <li>find halves and quarters of uneven partitioned shapes</li> <li>use language 'one half', 'two halves', 'one quarter', 'two quarters' and so on</li> </ul>		
	2	Recognising equivalence between halves and quarters of objects, shapes or sets up to 1 (symbols used)	<ul> <li>relate halves and quarters and know that 1/2 is the same as 2/4</li> <li>know that there are 2 quarters in 1 half</li> <li>show equivalent halves and quarters using concrete materials and models.</li> </ul>		
Find halves and quarters (symbols)	Finding halves and quarters of 1 linear models or sets (symbols used)		<ul> <li>find halves and quarters of objects and shapes</li> <li>find halves and quarters of sets</li> <li>find the whole from a part</li> <li>find halves and quarters of uneven partitioned shapes</li> <li>use language 'one half', 'two halves', 'one quarter', 'two quarters' and so on</li> <li>use symbols to represent fractions: 1/2, 2/2, 1/4, 2/4, 3/4, 4/4</li> </ul>		
	2	Recognising equivalence between halves and quarters of linear models or sets (symbols used)	<ul> <li>relate halves and quarters and know that 1/2 is the same as 2/4</li> <li>know that there are 2 quarters in 1 half</li> <li>show equivalent halves and quarters using concrete materials and models.</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

			/NA033)	
		Quest: Fraction	ns and decimals (2)	
Learning Journey	Steps	Spine Nodes	Subnodes	
	1	Introducing eighths of objects or shapes (no fractional notation)	<ul><li>find eighths of objects and shapes</li><li>recognise equivalence with halves and quarters</li></ul>	
Find eighths of objects or shapes	2	Introducing eighths of objects or shapes	<ul> <li>find eighths of objects and shapes</li> <li>recognise equivalence with halves and quarters</li> <li>use the language of 'one eighth', 'two eighths' and so forth along with standard fractional notation</li> </ul>	
Find halves, quarters and eighths of shapes	1	Finding halves, quarters and eighths of objects or shapes (no fractional notation)	<ul> <li>recognise equivalence</li> <li>estimate the size of a fractional part before using, eg paper folding to check or estimate the size of the whole from the par</li> <li>find the whole from a part</li> <li>find halves, quarters and eighths of uneven partitioned shape:</li> <li>recognise that the larger number of parts means that the part are smaller</li> </ul>	
Investigate and	d descri	be number patterns formed k	by skip counting and patterns with objects (ACMNA018	
		Quest: Patter	ns and algebra (1)	
numeric 1		Identifying, extending and describing repeating numeric patterns	<ul> <li>identify and extend through investigation, numeric repeating patterns, eg 1, 2, 1, 2,</li> <li>describe numeric repeating patterns</li> </ul>	
Explore	1	Recognising and describing repeating patterns with objects and symbols	<ul> <li>recognise and describe repeating patterns using objects and symbols;- recognise and correct errors in patterns</li> </ul>	
repeating patterns with objects	2	Copying repeating patterns using objects and symbols	copy repeating patterns using objects and symbols	
objects	3	Continuing repeating patterns with objects and symbols	continue repeating patterns using objects and symbols	
Relate number and object patterns	1	Relating patterns with objects and symbols to number patterns	<ul> <li>describe and relate a pattern to the corresponding number pattern, eg circle, square, circle, square is a 'two pattern'</li> <li>skip count to count the total objects in a pattern, eg count the total number of objects in a 'two pattern' by skip counting the groups of objects in 2s</li> </ul>	
Explore number	1	Exploring skip counting patterns with multiples of 1s, 2s, 5s and 10s using concrete materials	<ul> <li>identify and describe patterns when skip counting forwards o backwards by 1s, 2s, 5s and 10s from any starting point, eg 'all these numbers end in five or zero'</li> <li>investigate and solve problems based on number patterns</li> </ul>	
patterns (1, 2, 5, 10)	2	Representing and describing number patterns (2s, 5s or 10s)	<ul> <li>represent number patterns (skip counting in multiples of 1s, 2 5s or 10s from any number) on a number line or number char-</li> <li>describe the number pattern represented, eg 'this number pattern goes up in 5s'</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

		Quest: Patter	ns and algebra (1)	
Learning Journey	Steps	Spine Nodes	Subnodes	
Additive and	1	Recognising and describing additive and subtractive number patterns (within 5)	recognise and describe given number patterns that increase or decrease, eg 'the numbers are going up'	
subtractive patterns (within	2	Copying additive and subtractive number patterns (within 5)	• copy given number patterns that increase or decrease, eg 1, 2, 3, 4, 20, 18, 16, 14,	
5)	3	Extending additive and subtractive number patterns (within 5)	• continue given number patterns that increase or decrease, eg 1, 2, 3, 4, 20, 18, 16, 14,	
Odd and even number patterns	1	Modelling odd and even number patterns up to 20	<ul> <li>model odd and even numbers using objects such as counters paired in 2 rows</li> <li>describe the pattern created using the terms 'odd' or 'even'</li> </ul>	
(up to 20)		patterns up to 20	numbers	
	Describ	e patterns with numbers and	l identify missing elements (ACMNA035)	
		Quest: Patteri	ns and algebra (2)	
Number patterns (1, 2, 5, 10, 25 up to 100)	1	Identifying and describing number patterns (1s, 2s, 5s, 10s, 25s) up to 100	• identify and describe growing and shrinking patterns generated by the repeated addition or subtraction of 1s, 2s, 5s, 10s or 25s on a number line or number chart	
Add or subtract patterns (within 10) up to 100	1	Extending, completing and describing simple additive or subtractive number patterns with 1 operation (within 10) up	• determine a missing number in a number pattern, eg 3, 7, 11, _, 19	
·		to 100	describe a number pattern in words, eg 'lt goes up by 3s'	
Sol	ve prob	lems by using number senten	ces for addition or subtraction (ACMNA036)	
Write simple number sentences	1	Finding the missing number to make an addition or subtraction number sentence true (up to 18)	<ul> <li>complete number sentences involving 1 operation of addition or subtraction by finding the missing number using a variety of tools, equipment and strategies, eg using guess and check, eg 5 + (box symbol) = 13 or 15 - (box symbol) = 9</li> </ul>	
	2	Writing number sentences to solve word problems (1-digit and 2-digit addition and subtraction)	represent a word problem as an addition or subtraction number sentence	



### **Understanding Practice and Fluency (UPF)**

Measure	and cor	mpare the lengths of pairs	of objects using uniform informal units (ACMMG019)
		Qu	est: Length (1)
Learning Journey	Steps	Spine Nodes	Subnodes
Explore informal units of length and distance	1	Exploring uniform informal units of length and distance	<ul> <li>identify appropriate uniform informal units to measure lengths and distances, eg paper clips instead of craft sticks to measure a pencil;- explain the relationship between the size of a unit and the number of units needed, eg more paper clips than craft sticks will be needed to measure the length of the desk</li> <li>record lengths using informal units, eg the pencil is units long</li> <li>recognise the need for uniform units and the need to place the units end-to-end without gaps or overlaps</li> </ul>
and distance	2	Measuring length using unit iteration	record lengths and distances by referring to the number and type     of uniform informal unit used
	3	Measuring lengths and distances with uniform informal units	<ul> <li>identify the length of an object or shape</li> <li>record lengths and distances by referring to the number and type of uniform informal unit used</li> </ul>
Compare and order lengths using informal units	1	Comparing and ordering the lengths of shapes and objects using uniform informal units	<ul> <li>identify the length of an object or shape</li> <li>compare and order 2 or more shapes or objects that cannot be moved or aligned, according to their lengths, using an appropriate uniform informal unit</li> </ul>
Formal units for length (cm)	1	Introducing formal units for length: centimetres	<ul> <li>recognise and model that there are 100 cm in 1 m ie 100 cm = 1 m</li> <li>estimate and use the centimetre as a unit to measure lengths, to the nearest centimetre, using a device with 1 cm markings, eg use a paper strip of length 10 cm</li> <li>compare lengths with the same standard unit</li> </ul>
		Measure and compare	areas using uniform informal units
			uest: Area (1)
Explore, measure, compare area (informal units)	1	Exploring the attribute of area	<ul> <li>define area as an attribute</li> <li>identify areas in the environment</li> <li>describe areas using everyday language, such as 'surface', 'inside', 'outside'</li> <li>understand that the area remains the same if a given area is divided up and rearranged into a new configuration (conservation)</li> </ul>
	2	Comparing areas using direct comparison	<ul> <li>compare areas by positioning one area over another area</li> <li>compare areas by tracing one area and placing it over the top another area</li> <li>describe one area as larger than, the same as (about the same as), or smaller than another area</li> </ul>
	3	Measuring area using informal units	<ul> <li>compare use of non-uniform units with uniform units to measure area</li> <li>tile units to completely cover an area</li> <li>consider effect of gaps and overlaps when measuring area</li> <li>recognise iteration and structure in arrangement of uniform informal units to measure the area</li> <li>identify features that determine whether chosen units will be good units to measure area;- ie units must be the same size, units need to tile without gaps or overlaps</li> <li>estimate areas in uniform informal units</li> </ul>



### **Understanding Practice and Fluency (UPF)**

Compare and order several shapes and objects based on area using appropriate uniform informal units (ACMMG037)				
		Qı	uest: Area (2)	
Learning Journey	Steps	Spine Nodes	Subnodes	
Compare and order areas (informal units)	1	Comparing and ordering areas using uniform informal units (indirect comparison)	<ul> <li>compare two areas by measuring using uniform informal units</li> <li>order three or more areas by measuring using uniform informal units</li> <li>make statements of comparison about the relative size of three areas, eg if A is larger than B and B is larger than C, then A is larger than C</li> </ul>	
Measure and estimate area	1	Measuring and estimating areas of rectangles using a square unit	<ul> <li>establish usefulness of using a square unit to find an area as it allows for an array structure and does not have gaps or overlaps</li> <li>compare the same area measured using different sized square unit</li> <li>understand that the larger the unit square, the smaller the number of units needed and likewise the smaller the square unit, the larger the number of units needed</li> </ul>	
using square units	Measuring and estimating 2 areas of rectilinear shapes using a square unit		<ul> <li>establish usefulness of using a square unit to find an area as it allows for an array structure and does not have gaps or overlaps</li> <li>compare the same area measured using different sized square unit</li> <li>understand that the larger the unit square, the smaller the number of units needed and likewise the smaller the square unit, the larger the number of units needed</li> </ul>	
Measure a	nd com	pare the capacities of pair	rs of objects using uniform informal units (ACMMG019)	
	1		use the terms 'full', 'empty' and 'about half-full', 'quarter full',     'more than', 'less than' to describe the amount of substance in a     container	
Explore volume and capacity using informal units	2	Exploring and explaining volume and capacity with uniform informal units	<ul> <li>use uniform informal units to measure the volume of containers; pack cubic units (eg blocks) into rectangular containers so that there are no gaps</li> <li>recognise and select appropriate uniform informal units to measure the volume/capacity of containers, eg using cups rather than teaspoons to fill a bucket</li> <li>explain the relationship between the size of a unit and the number of units needed, eg more cups than ice cream containers will be needed to fill a bucket</li> </ul>	
Measure volume and capacity (informal units)	1		record volumes/capacities by referring to the number and type of uniform informal unit used	
Compare and order volume/ capacity (informal units)	1	Comparing and ordering the volume and capacity of 2 or more containers using uniform informal units	<ul> <li>compare the capacities of 2 or more containers using appropriate uniform informal units, eg count the number of times a smaller container can be filled and emptied into the containers being measured</li> <li>order containers in terms of capacity</li> </ul>	
Compare and order volume using blocks	1	Comparing and ordering volumes of models made from blocks	<ul> <li>compare and order the volumes of 2 or more models by counting the number of blocks used in each model</li> <li>recognise that models with different appearances may have the same volume</li> </ul>	
Compare and order volume using displacement	1	Comparing and ordering volumes through displacement	compare and order the volumes of 2 or more objects by marking the change in water level when each is submerged	



### **Understanding Practice and Fluency (UPF)**

		Investigate	mass using a pan balance
			Quest: Mass (1)
Learning Journey	Steps	Spine Nodes	Subnodes
Compare and order mass using	1	Comparing and describing mass of 2 objects using a pan balance	<ul> <li>establish meaning of a 'level balance' and describe the 2 objects as having 'equal mass/weight'</li> <li>describe the results of imbalance of a pan balance using the terms 'heavier' and 'lighter'</li> </ul>
a pan balance	2	Ordering more than 2 objects by mass using a pan balance	order more than 2 objects by mass using a pan balance
Compare and order mass using informal units	1	Comparing and ordering masses using uniform informal units	<ul> <li>find differences in mass by measuring and comparing, eg 'The pencil has a mass equal to 3 blocks and a pair of plastic scissors has a mass of 6 blocks, so the scissors are 3 blocks heavier than the pencil'</li> <li>compare masses using simple multiples, eg twice and heavy, half as heavy</li> </ul>
		Name and order m	nonths and seasons (ACMMG040)
		Quest: Ti	me – using calendars (1)
Months of the	1	Introducing the months of the year	<ul> <li>name and order the months of the year</li> <li>determine the month before or after a given month</li> </ul>
year	2	Months of the year	recall the number of days there are in each month
Know the seasons	1	Introducing the seasons	<ul> <li>know that there are 4 seasons in a year</li> <li>name and order the seasons of the year</li> <li>know and recall the months for each season</li> <li>recognise that the seasons are opposite in the opposite hemisphere of the planet</li> </ul>
Use a caler	dar to i	dentify the date and de	termine the number of days in each month (ACMMG041)
Use a calendar	1	Introducing calendars	<ul> <li>identify elements of a conventional calendar (month, day, date)</li> <li>identify a day and date using a conventional calendar</li> <li>relate calendars to the parts of a written date</li> </ul>
to identify the date	2	Using a calendar to solve simple problems involving months	<ul> <li>locate any given month on a calendar</li> <li>use a calendar to determine the number of months between events</li> <li>use a calendar to determine which month comes before/after a given month</li> </ul>
		Tell time to t	he half-hour (ACMMG020)
		Quest: Ti	me - telling the time (1)
Tell time to the hour and half hour (analogue)	1	Telling time to the hour and half hour (analogue)	<ul> <li>observe and describe the coordinated movements of the hands on an analogue clock as time progresses in half-hour intervals</li> <li>describe the position or draw of the hands of an analogue clock when reading time to the half hour</li> <li>read time on analogue clocks to the half hour using the terms 'o'clock' and 'half past'</li> <li>position or draw the hands on an analogue clock to show time to the half-hour where the time is given using the terms 'o'clock' or 'half-past'</li> <li>relate hour and half hour times and the duration of a half hour to everyday events;- develop a personal reference for a half hour</li> </ul>



### **Understanding Practice and Fluency (UPF)**

		Tell tin	ne to the half-hour (ACMMG020)	
	Quest: Time – telling the time (1)			
Learning Journey	Steps	Spine Nodes	Subnodes	
Tell time to the hour and half hour (digital)	1	Telling time to the hour and half hour (digital)	<ul> <li>read time on 12-hour digital clocks to the half-hour using the terms 'o'clock' and 'half past'</li> <li>connect 12-hour digital displays for times to the half-hour to their corresponding display on an analogue clock</li> <li>record times on analogue clocks to the half-hour in 12-hour digital format</li> <li>relate hour and half hour times and the duration of a half hour to everyday events;- develop a personal reference for a half hour</li> <li>position or draw the hands on an analogue clock to show time to the half-hour where the time is given in 12-hour digital format</li> </ul>	
	D	escribe duration usi	ng months, weeks, days and hours (ACMMG021)	
		Que	est: Time – telling the time (2)	
Choose appropriate units of time	1	Choosing appropriate units for measuring time (day, hour, minute, second)	select the most suitable unit of time for a task (day, hour, minute or second)	
Use hours to measure time	1	Introducing formal units for time: hours	<ul> <li>establish the need for formal units (hours) to measure time</li> <li>identify situations where hours are an appropriate unit for measuring the duration of time</li> <li>identify the relationship between half hours and hours</li> <li>know that there are 24 hours in one day</li> <li>introduce the abbreviation h to record time in hours</li> <li>compare durations in hours</li> </ul>	
Use minutes to measure time	1	Introducing formal units for time: minutes	<ul> <li>develop a sense of the duration of 1 minute by experiencing activities with this duration</li> <li>identify situations where minutes are an appropriate unit for measuring the duration of time</li> <li>establish the need for formal units (minutes) to measure time</li> <li>identify the relationship between minutes and hours: know that 1 hour is 60 minutes;- that ½ hour is 30 minutes;- that a quarter of an hour is 15 minutes; and that three-quarters of an hour is 45 minutes</li> <li>read the time on digital clocks using the terms 'thirty' 'fifteen' 'forty-five' etc</li> <li>connect the duration of 1 minute to the coordinated movements of the hands of an analogue clock</li> <li>introduce the abbreviation min to record time in minutes</li> <li>compare and sequence durations in minutes</li> </ul>	
Use seconds to measure time	1	Introducing formal units for time: seconds	<ul> <li>identify situations where seconds are an appropriate unit for measuring the duration of time</li> <li>identify the relationship between minutes and seconds: know that 1 minutes is 60 seconds;- that ½ minute is 30 seconds</li> <li>connect the duration of 1 minute to the coordinated movements of the hands of an analogue clock</li> <li>compare and sequence durations in seconds</li> </ul>	
Compare hours, minutes and seconds	1	Comparing durations in hours, minutes and seconds	<ul> <li>compare and sequence durations given in a combination hours, minutes and seconds</li> <li>measure and compare time intervals in mixed units (h, min, s)</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

	Tell time to the quarter-hour using the language of 'past' and 'to' (ACMMG039)				
		Qu	est: Time - telling the time (2)		
Learning Journey	Steps	Spine Nodes	Subnodes		
Tell time to the half and quarter hour	1	Relating halves and quarters to telling time	<ul><li>identify quarters and halves on a clock face</li><li>relate 'past' and 'to' to the halves of a clock face</li></ul>		
	2	Telling time to the quarter hour (analogue)	<ul> <li>observe and describe the coordinated movements of the hands on an analogue clock as time progresses in quarter hour intervals</li> <li>describe the position or draw of the hands of an analogue clock when reading time to the quarter hour</li> <li>read time on analogue clocks to the quarter-hour using the terms 'o'clock', 'half past', 'quarter past' and 'quarter to' and relate to knowledge of fractions</li> </ul>		
	3	Telling time to the quarter hour (digital)	<ul> <li>read time on 12-hour digital clocks to the quarter-hour using the terms 'o'clock', 'half past', 'quarter past' and 'quarter to'</li> <li>position or draw the hands on an analogue clock to show time to the quarter-hour where the time is given using the terms 'o'clock' or 'quarter-past'</li> <li>record times on analogue clocks to the quarter-hour in 12-hour digital format</li> <li>position or draw the hands on an analogue clock to show time to the quarter-hour where the time is given in 12-hour digital format</li> </ul>		
		Qu	est: Time – using calendars (2)		
Use calendars to solve simple problems	1	Using calendars to solve problems	<ul> <li>locate any given date, including today's date, on a calendar</li> <li>use a calendar to locate the date to match a given description, eg if today is Monday 8th April, then what is the date on Thursday?;- find the date of the third Thursday in March</li> <li>use a calendar to determine the number of days, weeks or months until a future event or between events</li> <li>use a calendar to calculate and describe lengths of time in days/weeks</li> </ul>		
Pecogr	nise and	l classify familiar thr	ree-dimensional objects using obvious features (ACMMG022)		
- Iteeogi			st: Three-dimensional space (1)		
Explore	1	Introducing surfaces	<ul> <li>manipulate three-dimensional objects and identify the type and number of flat and curved surfaces, eg 'The prism has eight flat surfaces'</li> <li>sort three-dimensional objects by the type and number of flat and curved surfaces</li> </ul>		
surfaces and faces	2	Introducing faces	<ul> <li>identify and describe the number and shape of faces on a cube, rectangular prism or triangular prism</li> <li>select a three-dimensional object from a description of its faces, eg '6 square faces'</li> </ul>		
Recognise and describe spheres	1	Introducing spheres	<ul> <li>recognise spheres in the environment and drawings</li> <li>select spheres from other three-dimensional objects using a description, 'round and rolls';- name the shape</li> </ul>		
Recognise and describe cones	1	Introducing cones	<ul> <li>recognise cones in the environment and drawings, including different orientations</li> <li>manipulate and describe cones as having 1 flat surface and 1 curved surface</li> <li>select cones from other three-dimensional objects using a description, '1 flat surface and 1 curved surface'; name the shape</li> </ul>		
Recognise and describe cubes	1	Introducing cubes	<ul> <li>recognise cubes in the environment and drawings, including different orientations</li> <li>select cubes from other three-dimensional objects using a description, eg '6 square faces';- name the shape</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

Recogr	nise and	l classify familiar thr	ee-dimensional objects using obvious features (ACMMG022)
		Ques	st: Three-dimensional space (1)
Learning ourney	Steps	Spine Nodes	Subnodes
Dosognico			<ul> <li>recognise cylinders in the environment and drawings, including different orientations</li> </ul>
Recognise and describe cylinders	1	Introducing cylinders	<ul> <li>manipulate and describe cylinders as having 2 flat surfaces and 1 curved surface</li> </ul>
			• select cylinder from other three-dimensional objects using a description, eg '2 flat surfaces and 1 curved surface', name the shape
	1	Recognising and naming three-	<ul> <li>recognise common three-dimensional objects in the environment and drawings, including different orientations</li> </ul>
		dimensional objects	name common three-dimensional objects
Recognise, sort and name 3D objects	2	Sorting familiar three-dimensional objects — cones, cubes, spheres, cylinders, prisms	sort familiar three-dimensional objects using given attributes
	3	Comparing three- dimensional objects to everyday objects	• identify common three-dimensional objects in everyday objects, eg cans, balls, boxes
Recognise and		Introducing prisms	recognise prisms in the environment and drawings, including different orientations
describe prisms no formal	1		<ul> <li>manipulate and describe prisms as having identical bases and rectangular faces</li> </ul>
names)			• select prisms from other three-dimensional objects using a description, eg 'rectangular faces';- name the shape (as prism only)
		Describe the featur	es of three-dimensional objects (ACMMG043)
		Ques	t: Three-dimensional space (2)
Compare 2D shapes and 3D objects	1	Building three- dimensional structures	describe the two-dimensional shapes that the structure contains
-	1	Introducing edges on	• identify and count the edges on everyday objects and cones, cylinders, prisms, spheres and cubes
dentify faces, edges and	'	three-dimensional objects	<ul> <li>identify and count the vertices on everyday objects and cones, cylinders, prisms, spheres and cubes</li> </ul>
vertices on 3D objects	3	Identifying faces, edges, vertices of cones, cubes, prisms, cylinders and spheres	identify and count the faces, edges and vertices on everyday objects and cones, cylinders, prisms, spheres and cubes
		Describing the	<ul> <li>manipulate and describe the attributes of basic three-dimensional objects using attributes such as faces, edges, vertices, number and type of surfaces</li> </ul>
aces, edges,	1	attributes of cones, cubes, cylinders,	• select a three-dimensional object from a description, eg '6 faces, 12 edges and 8 vertices'
vertices and surfaces of 3D		spheres and prisms	recognise that flat surfaces of three-dimensional objects are two- dimensional shapes and name the shapes of these surfaces
objects	2	Sorting three- dimensional objects (cubes, prisms, spheres, cylinders)	sort three-dimensional objects according to particular attributes, eg the shape of the surfaces or number of edges



### **Understanding Practice and Fluency (UPF)**

Recog	nise an	d classify familiar tw	vo-dimensional shapes using obvious features (ACMMG022)	
	Quest: Two-dimensional space (1)			
Learning Journey	Steps	Spine Nodes	Subnodes	
Sort quadrilaterals from other 2D shapes	1	Introducing quadrilaterals	<ul> <li>recognise all regular and irregular closed 4-sided shapes as quadrilaterals</li> <li>sort quadrilaterals from other two-dimensional shapes</li> </ul>	
dentify, sort and name octagons	1	Introducing octagons	identify, sort and name octagons in different orientations, including octagons in their environment	
ldentify, sort and name pentagons	1	Introducing pentagons	identify, sort and name pentagons in different orientations, including pentagons in their environment	
ldentify, sort and name hexagons	1	Introducing hexagons	identify, sort and name hexagons in different orientations, including hexagons in their environment	
Identify and name simple 2D shapes	1	Identifying and naming two- dimensional shapes	<ul> <li>identify and name two-dimensional shapes including octagons, pentagons, circles, hexagons, triangles and quadrilaterals by their number of sides</li> <li>select a shape from a description of its features, eg number of sides or vertices</li> <li>identify and name shapes in pictures, designs and the environment</li> </ul>	
	2	Identifying and naming shapes embedded in pictures, designs and the environment	identify simple shapes embedded in pictures	
Compare, describe and sort simple 2D shapes	1	Comparing and describing two-dimensional shapes	<ul> <li>manipulate, compare and describe similarities and differences between two-dimensional shapes including octagons, pentagons, circles, hexagons, triangles and quadrilaterals</li> <li>identify and describe the number of sides</li> <li>sort regular and irregular two-dimensional shapes in various orientations including octagons, pentagons, circles, hexagons, triangles, quadrilaterals using a given attribute, eg number of sides or vertices</li> </ul>	
dentify vertical and horizontal ines	1	Introducing vertical and horizontal lines	identify and name vertical and horizontal lines in pictures and the environment	
dentify parallel ines	1	Introducing parallel lines	<ul> <li>identify and name parallel lines in pictures and the environment</li> <li>recognise that parallel lines can occur in orientations other than vertical and horizontal</li> </ul>	
Describe and	draw t	wo-dimensional sha	pes, with and without the use of digital technologies (ACMMG042	
		Que	st: Two-dimensional space (2)	
Represent and describe regular polygons	1	Representing and describing regular polygons	name two-dimensional shapes in different orientations, eg triangles, quadrilaterals, pentagons, hexagons, octagons and describe the number of angles and/or sides	



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

Investigate the effect of one-step slides and flips, with and without the use of digital technologies (ACMMG045)					
	Quest: Two-dimensional space (2)				
Learning Journey	Steps	Spine Nodes Subnodes			
	1	Introducing transformations of shapes: Slides (translations)	• identify and describe a 1-step slide of a shape using the term 'slide'		
Translations of	2		• identify and describe a one-step flip of a shape using the term 'flip'		
shapes (slides, flips, turns)			• identify a one-step slide or flip of a single shape and use the terms 'slide' and 'flip' to describe the movement of the shape		
	3	Transformations of shapes: Flips and slides	• identify a one-step slide or flip of a single shape and use the terms 'slide' and 'flip' to describe the movement of the shape		
		Silues	recognise that sliding or flipping a shape does not change its size or features		
			recognise that sliding or flipping a shape does not change its size or features		
		•	ibe half-turns and quarter-turns (ACMMG046)		
	transformations of shapes: Turns • identify and describe half-tu		<ul> <li>recognise and describe turns as 'clockwise' or 'anti-clockwise'</li> <li>identify and describe half-turns and quarter-turns</li> <li>identify and describe half-turns and quarter-turns</li> </ul>		
	(rotations)  • Identify and describe half-turns and quarter-turns  Give and follow directions to familiar locations (ACMMG023)				
			Quest: Position (1)		
	1	Describing position using more than 1 descriptor	<ul> <li>describe the location of objects in a given structure using more than 1 descriptor, including 'from the left' and 'from the right' and ordinal number words</li> <li>locate objects in a given structure given a description involving more than 1 descriptor, including 'from the left' and 'from the right' and ordinal number words</li> </ul>		
Position using left, right and ordinal	2	Establishing and understanding left and right from opposite direction	<ul> <li>describe the position of an object as to the left or right of a person facing in the same direction as themselves</li> <li>describe the position of an object as to the left or right of a person facing in the opposite direction to themselves</li> </ul>		
numbers	3	Following given directions	follow directions to position an object in a structure or picture		
	4	Describing the path from 1 location to another on drawings#language to include 'left' and 'right'	<ul> <li>use a diagram to give simple directions using only counting of squares and left or right</li> <li>create a path from 1 location to another</li> </ul>		
Interpret sim	nple ma	ps of familiar locati	ons and identify the relative positions of key features (ACMMG044)		
	Quest: Position (2)				
Read simple maps	1	Interpreting simple maps	<ul> <li>interpret simple maps of familiar locations and describe the location of specific features relative to other features</li> <li>describe, using landmarks and directional language, a path from 1 feature to another on a simple map</li> </ul>		
шарз	2	Following pathways on simple maps	follow and draw a path on a simple map given directions that use landmarks and directional language		
		· · · · · · · · · · · · · · · · · · ·	·		



### **Understanding Practice and Fluency (UPF)**

#### **Statistics and Probability**

	Choose simple questions and gather responses (ACMSP262)					
Quest: Data (1)						
Learning Journey	Steps	Spine Nodes	Subnodes			
Ask suitable questions for data collection	1	Asking questions and collecting simple data with support	choose a suitable question for a given matter of interest involving category data, eg 'How did the children in Room 3 come to school?'			
Complete tally charts	1	Introducing and completing tally charts	collect and sort data using a simple given tally chart			
Represent o	data wi		ings where one object or drawing represents one data value and cribe the displays (ACMSP263)			
Represent data in a simple display	1	Representing category or discrete data using simple displays	<ul> <li>use concrete materials or pictures of objects as symbols to create data displays where 1 object or picture represents 1 data value (one-to-one correspondence), eg use different-coloured blocks to represent different-coloured cars</li> <li>record data in prepared graphic organisers such as simple block charts, pictographs or other diagrams</li> </ul>			
Read simple data displays using objects	1	Interpreting basic data displays including tally charts, tables and data displays with concrete materials	describe information presented in tables, lists or other simple data displays using comparative language such as 'more than' and 'less than', eg 'There were more black cars than red cars'			
Identify a qu	estion	of interest based on	one categorical variable and gather data relevant to the question (ACMSP048)			
Answer questions related to simple data displays	1	Conducting a well- supported and basic statistical investigation using category data	answer questions and make simple statements related to the data gathered			
Create	displa	ys of data using lists,	tables and picture graphs and interpret them (ACMSP050)			
			<ul> <li>read and interpret data represented in a picture graph;- pose and answer simple summative and comparative questions, eg 'Which is the least favourite season?'</li> </ul>			
Read and interpret simple picture graphs	1	Introducing and reading picture graphs (up to 4 categories)	<ul> <li>choose an appropriate title for a display;- labels the axis</li> <li>identify misleading representations of data in a picture graph, eg where the symbol used to represent one item is shown in different sizes or where symbols are not equally spaced</li> <li>read and interpret data represented in a picture graph;- pose and answer</li> </ul>			
			simple summative and comparative questions, eg 'Which is the least favourite season?'			
Represent and read data in tables or lists	1	Representing and reading data displayed in tables or lists	<ul> <li>display category or numerical data using lists and tables</li> <li>pose questions and answer one-step and two-step questions, eg 'How many more students like reading than art?';- identify basic similarities and differences between categories;- make simple conclusions</li> </ul>			
Use a tally chart, table, picture graph		Introducing the statistical investigation process (tables, lists or picture graphs)	represent category data in a table, list or picture graph (one-to-one correspondence)			



#### **Understanding Practice and Fluency (UPF)**

#### **Statistics and Probability**

**Quest: Chance (1)** Learning **Steps Spine Nodes Subnodes** Journey Use the Exploring possible · use everyday language to describe the possible outcomes of familiar everyday outcomes of familiar activities and events, eg 'will happen', 'might/could happen', 'won't happen', 1 language of events and activities 'probably' chance Identify practical activities and everyday events that involve chance (ACMSP047) **Quest: Chance (2)** Using the basic • Identify practical activities and everyday events that involve chance, eg'l Use basic language of might play with my friend after school' probability 1 probability: · describe outcomes in everyday activities and events as being 'possible', impossible, possible, language

'impossible', 'likely' or 'unlikely' to happen

Identify outcomes of familiar events involving chance and describe them using everyday language, such as 'will happen', 'won't happen' or 'might happen' (ACMSP024)

	. 0 0.		likely, unlikely	'impossible', 'likely' or 'unlikely' to happen	
	Describe outcomes as 'likely' or 'unlikely' and identify some events as 'certain' or 'impossible' (ACMSP047)				
	Use basic probability language	2	Using the language of probability: possible and impossible	<ul> <li>identify and distinguish between 'possible' and 'impossible' events</li> <li>describe familiar events as being 'possible' or 'impossible', eg 'It is possible that it will rain today', 'It is impossible to roll a standard six-sided dice and get a 7'</li> </ul>	
		3	Using the language of probability: likely and unlikely	<ul> <li>describe possible outcomes in everyday activities and events as being 'likely' or 'unlikely' to happen</li> <li>compare familiar activities and events and describe them as being 'likely' or 'unlikely' to happen</li> </ul>	
		4	Using the language of probability: certain and uncertain	<ul> <li>identify and distinguish between 'certain' and 'uncertain' events</li> <li>describe familiar situations as being certain or uncertain, eg 'lt is uncertain what the weather will be like tomorrow', 'lt is certain that tomorrow is Saturday'</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

MA2-4NA applies place value to order, read and represent numbers of up to five digits					
Quest: (1) Numbers up to 5 digits					
	Learning Journeys Identifying and counting numbers to 4 digits				
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Identifying numbers before and after up to 4-digit numbers (within 10000)	<ul> <li>identify the number that comes before a given 2,-, 3- or 4-digit number up to 10000; describe this number as 'one more than'</li> <li>identify the number that comes after a given 2-, 3- or 4-digit number up to 10000; describe this number as 'one less than'</li> <li>identify the number that comes before or after a given 2-, 3- or 4-digit number up to 10000; describe this number as 'one more than' or 'one less than'</li> </ul>		
NA.A.1 Recognise, model, represent and order numbers	2	Counting by tens and hundreds using models, number lines and charts	<ul> <li>count forwards and backwards in tens, on and off the decade, with 2-digit, 3-digit and 4-digit numbers using number lines and number charts</li> <li>count forwards and backwards in hundreds, on the decade, with 3-digit and 4-digit numbers using number lines and number charts</li> <li>count forwards and backwards in hundreds, on and off the decade, with 3-digit and 4-digit numbers using number lines and number charts</li> </ul>		
to at least 10 000	3	Counting by tens and hundreds	<ul> <li>count forwards and backwards in tens, on and off the decade, with 2-digit, 3-digit and 4-digit numbers</li> <li>count forwards and backwards in hundreds, on the decade, with 3-digit and 4-digit numbers</li> <li>count forwards and backwards in hundreds, on and off the decade, with 3-digit and 4-digit numbers</li> </ul>		
	4	Finding numbers 10 or 100 before and after up to 1000	<ul> <li>find the number '10 before' or '10 after' a given 2-digit, 3-digit or 4-digit number on or off the decade using number lines and number charts</li> <li>find the number '100 before' or '100 after' a given 3-digit or 4-digit number on or off the decade using number lines and number charts</li> </ul>		
	Lea	rning Journeys Read	ing and representing numbers: up to 4 digits		
NA.A.1 Recognise,	1	Reading and writing 4-digit numbers using words and numerals	<ul> <li>write a given 4-digit number in words, eg 4567 as four thousand, four hundred and sixty-seven</li> <li>write the numerals for a 4-digit number given in words</li> </ul>		
model, represent and order numbers to at least 10 000	2	Representing 4-digit numbers using words, numerals and objects	<ul> <li>model a given 4-digit number using concrete materials, pictures or drawings</li> <li>write the numerals in words, eg 'seven thousand, three hundred and fifty three' for a 4-digit number represented using place value equipment or using pictures, drawings</li> </ul>		
	L	earning Journeys Co	omparing and ordering numbers to 10 000		
NA.A.1 Recognise, model, represent and order numbers to at least 10 000	1	Comparing numbers to 10000	<ul> <li>model and compare two 4-digit numbers using place value equipment</li> <li>compare two numbers of up to 4 digits and describe using the terms and symbols: greater than (&gt;) or less than (&lt;); explain the comparison using place value reasoning</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

MA2-4NA applies place value to order, read and represent numbers of up to five digits						
	Quest: (1) Numbers up to 5 digits					
	L	earning Journeys Co	omparing and ordering numbers to 10 000			
Content Descriptor	Steps	s Spine Nodes Subnodes				
NA.A.1 Recognise, model, represent and order numbers to at least 10 000	2	Ordering numbers to 10000	<ul> <li>order up to 4 consecutive 2-digit, 3-digit or 4-digit numbers within 1000 in ascending order or descending order; explain the reason for the order given</li> <li>order up to 4 non-consecutive 2-digit, 3-digit or 4-digit numbers within 1000 in ascending or descending order; explain the reason for the order given using place value reasoning</li> </ul>			
	L	earning Journeys Us	sing place value to partition: up to 4-digits			
NA.A.2 Apply place value to partition, rearrange and regroup numbers to at least 10 000 to assist calculations and solve problems	2	Using place value to partition 4-digit numbers  Identifying the place value of digits in 4-digit numbers	<ul> <li>use place value equipment to partition a given 4-digit number into thousands, hundreds, tens and ones</li> <li>describe a 4-digit number using words, eg 9523 as '9 thousands, 5 hundreds, 2 tens and 3 ones'</li> <li>write a 4-digit number in expanded notation, eg 7523 as 7000 + 500 + 20 + 3</li> <li>write the numeral for a number represented by expanded notation</li> <li>recognise zero as a placeholder</li> <li>write the numeral for a 4-digit number modelled using place value equipment</li> <li>identify the digit in the thousands, hundreds, tens or ones column for a given 4-digit number</li> <li>identify, record and model a number using place value clues, eg 'an 8 in the thousands, 5 in the hundreds and a 2 in the ones' as 8502</li> <li>recognise the role of zero as a placeholder</li> </ul>			
	3	Partitioning 4-digit numbers using non- standard partitioning	<ul> <li>create the smallest and largest numbers possible using 4 digits</li> <li>use place value equipment to partition a given 4-digit number using non-standard partitioning, eg 2375 as 2 thousands, 1 hundred and 275 ones or 2000 + 100 + 275</li> <li>model and identify a number from non-standard partitioning, eg recognise 3 hundreds, 4 tens and 27 ones or 300 + 40 + 27 as 367</li> </ul>			
		Learning Jour	neys Rounding numbers: 4 digits			
NA.A.2 Apply place value to partition, rearrange and regroup	1	Rounding numbers up to 10000 to the nearest 1000	<ul> <li>model a 4-digit number and recognise which thousand it is nearer to; explain reasoning</li> <li>round a 4-digit number to the nearest 1000; recognise the digit in the hundreds column as the key digit</li> </ul>			
numbers to at least 10 000 to assist calculations and solve problems	2	Rounding numbers up to 10000 to the nearest 10, 100 or 1000	round a 4-digit number to the nearest 10, 100 or 1000; explain the rounding			



### **Understanding Practice and Fluency (UPF)**

MA2-4NA applies place value to order, read and represent numbers of up to five digits				
Quest: (2) Numbers up to 5 digits				
	Lea	arning Journeys Com	paring and ordering numbers up to 5 digits	
Content Descriptor	Steps	Spine Nodes	Subnodes	
NA.A.3 Recognise, represent and	1	Comparing 5-digit numbers using words and symbols	<ul> <li>compare two 5-digit numbers using words and symbols &lt;, =, &gt;</li> </ul>	
order numbers to at least tens of thousands	2	Ordering numbers up to 5 digits	arrange numbers of up to 5 digits in ascending and descending order	
	Lea	rning Journeys Read	ing and representing numbers: up to 5 digits	
	1	Reading and writing numbers up to 5 digits	<ul> <li>apply an understanding of place value to read numbers up to 5 digits</li> <li>apply an understanding of place value to write numbers up to 5 digits</li> </ul>	
NA.A.3 Recognise, represent and order numbers to at least tens of thousands	2	Identifying the place value of digits in numbers up to 5 digits	<ul> <li>state the place value of digits in numbers of up to 5 digits</li> <li>pose and answer questions that extend place value understanding of numbers, eg 'What happens if I rearrange the digits in the number 12 345?', 'How can I rearrange the digits to make the largest number?'</li> <li>represent and describe whole numbers to 10 000 pictorially and symbolically</li> </ul>	
	3	Finding the number 1000 more or 1000 less than a given number	apply an understanding of place value to find the number 1000 more or 1000 less	
	L	earning Journeys Us	sing place value to partition: up to 5 digits	
NA.A.3	1	Using place value to partition 5-digit numbers	<ul> <li>use place value to partition numbers of up to 5 digits, eg 67 012 is 60 000 + 7000 + 10 + 2</li> </ul>	
Recognise, represent and order numbers to at least tens	2	Using non-standard partitioning with 5-digit numbers	• partition numbers of up to 5 digits in non-standard forms, eg 67 000 as 50 000 + 17 000	
of thousands	3	Understanding the relationship between place value positions	<ul> <li>recognise that in a multi-digit number a digit in 1 place represents 10 times as much as it represents in the place to its right</li> <li>recognise that in a multi-digit number a digit in 1 place represents 1/10 of what it represents in the place to its left</li> </ul>	
Learning Journeys Rounding numbers: 5 digits				
NA.A.3 Recognise, represent and order numbers to at least tens of thousands	1	Rounding 5-digit numbers	• round to the nearest 10, 100, 1000 or 10,000	



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and

MAZ-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers						
Quest: (1) Add/sub up to 5 digits						
	Learning Journeys Add/subtract: single digit numbers					
Content Descriptor	Steps	Spine Nodes	Subnodes			
	1	Recalling number bonds to 30	• use known facts and number patterns to recall bonds to 30 eg 18 + 2 = 20 so 28 + 2 = 30			
NA.B.1 Recall addition facts	2	Adding 3 or more single-digit numbers	<ul> <li>use appropriate strategies to add 3 or more single-digit numbers; including changing the order, doubles if appropriate, bridging to a ten</li> <li>explain and justify strategies used</li> </ul>			
for single- digit numbers and related subtraction	3	Adding and subtracting 3 or more single-digit numbers using compatible numbers	• use compatible numbers , eg 4 + 2 + 8 - 6 as 6 + 8 - 6 = 8			
facts to develop increasingly efficient mental strategies for computation	4	Creating and solving addition and subtraction word problems (within 1000)	<ul> <li>represent a word problem as an addition or subtraction number sentence</li> <li>solve simple addition and subtraction word problems in context including find the difference, find the sum, change unknown, start unknown</li> <li>explain and compare strategies used to solve addition and subtraction word problems</li> <li>create problems in contexts that involve addition and subtraction</li> </ul>			
	L	earning Journeys Add/subt	ract: 2 & 3-digit using jump strategy			
NA.B.1 Recall addition facts for single-	1	Adding 2-digit and 3-digit numbers using place value partitioning on a number line (jump strategy)	• model and solve the addition of a 2-digit and 3-digit number using an empty number line, eg 823 + 56 as 823 + 50 = 873, 873 + 6 = 879			
digit numbers and related subtraction facts to develop	2	Subtracting a 2-digit number from a 3-digit number using place value partitioning on a number line (jump strategy)	• model and solve the subtraction of a 2-digit number from a 3-digit number using an empty number line, eg 823 – 56 as 823 – 50 = 773, 773 – 6 = 767			
increasingly efficient mental strategies for computation	3	Adding and subtracting a 2-digit and 3-digit number using place value partitioning on a number line (jump strategy)	<ul> <li>model and solve the addition or subtraction of a 2-digit number from a 3-digit number using an empty number line, eg 823 – 56 as 823 – 50 = 773, 773 – 6 = 767</li> </ul>			



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers

five-digit numbers						
Quest: (1) Add/sub up to 5 digits						
Learning Journeys Add/subtract: place value partitioning 2 & 3-digit						
Content Descriptor	Steps	Spine Nodes	Subnodes			
NA.B.1 Recall addition facts	1	Adding 2-digit and 3-digit numbers mentally using place value understanding (jump strategy)	<ul> <li>mentally solve addition problems involving 2-digit and 3-digit numbers using a jump strategy, eg 823 + 56 as 823 + 50 = 873, 873 + 6 = 879</li> <li>record and explain the use of the strategy</li> <li>check calculations using the inverse operation</li> </ul>			
for single- digit numbers and related subtraction facts to develop increasingly efficient mental	2	Subtracting a 2-digit number from a 3-digit number mentally using place value understanding (jump strategy)	<ul> <li>mentally solve subtraction problems involving 2-digit and 3-digit numbers using place value partitioning, eg 823 – 56 as 823 – 50 = 773, 773 – 6 = 767</li> <li>record and explain the use of the strategy</li> <li>check calculations using the inverse operation</li> </ul>			
strategies for computation	3	Adding and subtracting a 2-digit and 3-digit number mentally using place value understanding (jump strategy)	<ul> <li>mentally solve addition and subtraction problems involving 2-digit and 3- digit numbers using place value partitioning, eg 823 - 56 as 823 - 50 = 773, 773 - 6 = 767</li> </ul>			
	Lea	rning Journeys Add/subtra	ct: bridging up to 10 using 2 & 3 digits			
	1	Bridging to ten to add two 2-digit numbers using models for support	<ul> <li>add to the nearest ten first then add the rest, using models for support, eg 28 + 17 as 28 + 2 = 30 and 30 + 15 = 45</li> <li>record and explain the use of the strategy</li> </ul>			
		Adding 2 numbers up to 3-digits using bridging to ten	<ul> <li>add up to two 3-digit numbers where the first number has a 7, 8, or 9 in the ones columns, by first adding to the * nearest ten and then adding the rest, eg 368 + 25 as 368 + 2 + 23</li> <li>record and explain the strategy using numerals, models and/or diagrams</li> </ul>			
NA.B.1 Recall addition facts for single-	2	Bridging to ten to subtract two 2-digit numbers using models for support	record and explain the use of the strategy			
digit numbers and related subtraction facts to develop increasingly		Subtracting 2 numbers up to 3-digits using bridging to ten	<ul> <li>subtract two numbers (up to 3-digits) where the first number has a 1, 2 or 3 in the ones columns, by first subtracting to the nearest ten and then subtracting the rest, eg 362 – 25 as 362 – 2 – 23</li> <li>record and explain the strategy using numerals, models and/</li> </ul>			
efficient mental strategies for computation		Bridging to ten to mentally add and subtract two 2-digit	<ul> <li>add or subtract to the nearest ten first then add or subtract the rest, using models for support, eg 28 + 17 as 28 + 2 = 30</li> </ul>			
		numbers	<ul><li>and 30 + 15 = 45</li><li>check calculations using the inverse operation</li></ul>			
	3	Adding and subtracting 2 numbers up to 3-digits using bridging to ten	• add or subtract two numbers (up to 3-digits) where the first number has a 7, 8, or 9 in the ones columns, by first adding to the nearest ten and then adding the rest, eg 368 + 25 as 368 + 2 + 23, or 362 - 25 as 362 - 2 - 23			
			<ul> <li>record and explain the strategy using numerals, models and/ or diagrams</li> </ul>			



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers					
Quest: (1) Add/sub up to 5 digits					
Learning Journeys Add/Subtract: Bridging					
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.B.1 Recall addition facts for single-digit numbers and related subtraction facts to develop increasingly efficient mental strategies for computation	1	Using a bridging strategy with start unknown or change unknown problems	<ul> <li>use a bridging strategy to solve addition and subtraction problems where the change is unknown, eg 29 + ? = 81</li> <li>use a bridging strategy to solve addition and subtraction problems where the start is unknown, eg ? + 29 = 81 becomes 29 + ? = 81</li> </ul>		
		Learning Journeys Add/s	subtract: partitioning 3-digits		
	1	Adding two 3-digit numbers using place value partitioning on a number line (jump strategy)	<ul> <li>model and solve the addition of two 3-digit numbers using an empty number line, eg 823 + 356 as 823 + 300 = 1123, 1123 + 50 = 1173, 1173 + 6 = 1179</li> </ul>		
NA.B.1 Recall addition facts for single-digit numbers and	2	Subtracting two 3-digit numbers using place value partitioning on a number line (jump strategy)	<ul> <li>model and solve the subtraction of two 3-digit numbers using an empty number line, eg 823 – 356 as 823 – 300 = 523, 523 – 50 = 473, 473 – 6 = 467</li> </ul>		
related subtraction facts to develop increasingly efficient mental strategies for	3	Adding and subtracting two 3-digit numbers using place value partitioning on a number line (jump strategy)	<ul> <li>model and solve the addition or subtraction of two 3-digit numbers using an empty number line, eg 823 – 356 as 823 – 300 = 523, 523 – 50 = 473, 473 – 6 = 467</li> </ul>		
computation	4	Adding and subtracting multi-digit numbers using place value partitioning	<ul> <li>partition the second number to add two multi-digit numbers (up to 4 digits), eg 1546 + 625 as 546 + 600 + 20 + 5; use standard or non-standard partitioning</li> <li>partition the second number to subtract two multi-digit numbers (up to 4 digits), eg 1546 - 625 as 546 - 600 - 20 - 5; use standard or non-standard partitioning</li> </ul>		
	L	earning Journeys Adding a	and subtracting 3-digit numbers		
NA.B.1 Recall addition facts for single-digit numbers and related subtraction facts to develop increasingly efficient mental strategies for computation	1	Adding up to 3-digit numbers mentally using place value understanding (jump strategy)	<ul> <li>solve the addition of two 3-digit numbers using a jump strategy, eg 823 + 356 as 823 + 300 = 1123, 1123 + 50 = 1173, 1173 + 6 = 1179</li> <li>explain and justify the use of the strategy</li> </ul>		
	2	Subtracting up to 3-digit numbers mentally using place value understanding (jump strategy)	<ul> <li>solve the subtraction of two 3-digit numbers using a jump strategy, eg 823 - 356 as 823 - 300 = 523, 523 - 50 = 473, 473 - 6 = 467</li> <li>explain and justify the use of the strategy</li> </ul>		
	3	Adding or subtracting up to 3-digit numbers mentally using place value understanding (jump strategy)	• solve the addition or subtraction of two 3-digit numbers using a jump strategy, eg 823 – 356 as 823 – 300 = 523, 523 - 50 = 473, 473 – 6 = 467		



### **Understanding Practice and Fluency (UPF)**

(split strategy)

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and

MAZ-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers					
	Quest: (1) Add/sub up to 5 digits				
	Le	arning Journeys Add/sul	btract: using place value (split model)		
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Adding a 2-digit and 3-digit number using place value models (split strategy)	<ul> <li>model the addition of a 2-digit and 3-digit number using a split strategy with or without crossing tens; use place value equipment, money or diagrams</li> <li>solve addition problems using a split strategy, eg 265 + 27 as 260 + 20 and 5 + 7, 280 + 12 = 292</li> <li>record and explain the use of the strategy</li> </ul>		
		Adding up to two 3-digit numbers mentally using place value understanding (split strategy)	<ul> <li>solve addition problems using a split strategy, eg 265 + 327 as 200 + 300, 60 + 20 and 5 + 7, 500 + 80 + 12 = 592</li> <li>record and explain the strategy using numerals, models and/or diagrams</li> </ul>		
NA.B.1 Recall addition facts for single-digit numbers and	2	Subtracting a 2-digit number from a 3-digit number using place value models (split strategy)	<ul> <li>model the subtraction of a 2-digit and 3-digit number using a split strategy; place value equipment, money or diagrams</li> <li>solve subtraction problems using a split strategy, eg 265 – 21 as 260 – 20 and 5 – 1, 240 + 4 = 244</li> <li>record and explain the use of the strategy</li> </ul>		
related subtraction facts to develop increasingly efficient mental strategies for computation		Subtracting two 3-digit numbers mentally using place value understanding (split strategy)	<ul> <li>solve subtraction problems using a split strategy, eg 548 – 127 as 500 – 100 and 40 – 20 and 8 – 7, 400 + 20 + 1 = 421</li> <li>record and explain the strategy using numerals, models and/or diagrams</li> </ul>		
Computation	3	Adding and subtracting 2-digit and 3-digit numbers using place value models (split strategy)  Adding and subtracting two 3-digit numbers	<ul> <li>model the addition or subtraction of a 2-digit and 3-digit number using a split strategy; place value equipment, money or diagrams</li> <li>solve addition and subtraction problems using a split strategy, eg 265 - 21 as 260 - 20 and 5 - 1, 240 + 4 = 244 record and explain the strategy using numerals, models and/or diagrams</li> <li>check calculations using the inverse operation</li> <li>solve addition and subtraction problems using a split strategy, eg 265 + 327 as 200 + 300, 60 + 20 and 5 + 7, 500 + 80 + 12 = 592</li> </ul>		
		mentally using place value understanding	<ul> <li>record and explain the strategy using numerals, models and/or diagrams</li> </ul>		

• check calculations using the inverse operation



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers

five-digit numbers					
Quest: (1) Add/sub up to 5 digits					
Learning Journeys Add/subtract: rounding & compensation 2-digit					
Steps	Spine Nodes	Subnodes			
	Introducing addition using rounding and compensating with two 2-digit numbers	<ul> <li>add two 2-digit numbers where 1 number is close to a ten (digit in the ones column is 7, 8 or 9)</li> <li>round 1 number to the next 10, carry out the addition and adjust the answer to compensate for the original rounding, eg 35 + 29 as 35 + 30 - 1</li> <li>record the strategy using numerals, models and/or diagrams and explain the need to compensate</li> </ul>			
1	Adding up to two 3-digit numbers using rounding and compensating	<ul> <li>add up to two 3-digit numbers where 1 number is close to a hundred (ends in 97, 98 or 99)</li> <li>round 1 number to the next 100, carry out the addition and adjust the answer to compensate for the original rounding, eg 398 + 23 as 400 + 23 - 2</li> <li>record the strategy using numerals, models and/or diagrams and explain the need to compensate</li> </ul>			
3	Introducing subtraction using rounding and compensating with two 2-digit numbers	<ul> <li>subtract two 2-digit numbers where 1 number is close to a ten</li> <li>round 1 number to the next 10, carry out the subtraction and adjust the answer to compensate for the original rounding, eg 33 – 19 as 33 – 20 + 1 or 81 – 35 as 80 – 35 + 1</li> <li>record the strategy using numerals, models and/or diagrams and explain the need to compensate</li> </ul>			
	Subtracting up to two 3-digit numbers using rounding and compensating	<ul> <li>subtract up to two 3-digit numbers where 1 number is close to a hundred (ends in 97, 98 or 99)</li> <li>round 1 number to the next 100, carry out the subtraction and adjust the answer to compensate for the original rounding, eg 398 - 23 as 400 - 23 + 2</li> <li>record the strategy using numerals, models and/or diagrams and explain the need to compensate</li> </ul>			
	Introducing addition and subtraction using rounding and compensating with two 2-digit numbers	<ul> <li>add or subtract two 2-digit numbers where 1 number is close to a ten (digit in the ones column is 7, 8 or 9)</li> <li>round 1 number to the next 10, carry out the addition or subtraction and adjust the answer to compensate for the original rounding, eg 33 - 19 as 33 - 20 + 1 or 81 - 35 as 80 - 35 + 1</li> <li>check calculations using the inverse operation</li> </ul>			
	Adding and subtracting up to two 3-digit numbers using rounding and compensating	<ul> <li>add or subtract up to two 3-digit numbers where 1 number is close to a hundred (ends in 97, 98 or 99)</li> <li>round 1 number to the next 100, carry out the addition or subtraction and adjust the answer to compensate for the original rounding, eg 398 + 23 as 400 + 23 - 2</li> </ul>			
4	Introducing addition using rounding and compensating when the change or start is unknown	<ul> <li>model with number lines and solve addition problems with two 2-digit numbers where the digits in the ones column for the known addend and result are close together, eg 23 + ? = 81 becomes 23 + 60 - 2</li> <li>explain and justify the use of the strategy</li> </ul>			
	Lear Steps	Learning Journeys Add/sul  Steps Spine Nodes  Introducing addition using rounding and compensating with two 2-digit numbers using rounding and compensating with two 2-digit numbers  Introducing subtraction using rounding and compensating with two 2-digit numbers  Subtracting up to two 3-digit numbers using rounding and compensating  Introducing addition and subtraction using rounding and compensating with two 2-digit numbers  Adding and subtraction using rounding and compensating up to two 3-digit numbers  Adding and subtracting up to two 3-digit numbers  Introducing addition using rounding and compensating up to two 3-digit numbers using rounding and compensating when the change or start is			



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers

five-digit numbers				
Quest: (1) Add/sub up to 5 digits				
		Learning Journey	s Add/subtract: to and from 100	
Content Descriptor	Steps	Spine Nodes	Subnodes	
NA.B.1 Recall addition facts for single-digit	1	Modelling pairs that add to 100	<ul> <li>use place value equipment to model pairs that add to 100, eg 63 and 37</li> <li>recognise that the ones make an extra ten when added</li> </ul>	
numbers and related subtraction facts to develop increasingly efficient mental	2	Adding to make 100	<ul> <li>find pairs of numbers that add to 100 (multiples of 5), eg 45 and 55</li> <li>find pairs of numbers that add to 100, eg 42 and 58</li> <li>find the missing number to add to 100 when 1 number is given</li> </ul>	
strategies for computation	3	Subtracting from 100	<ul> <li>subtract 1 number from 100 (multiple of 5), eg 100 – 35 = 65</li> <li>subtract 1 number from 100, eg 100 – 29 = 71</li> </ul>	
	Lear	ning Journeys Add/sul	btract: 1-digit numbers, 100, 1000 & 10000	
NA.B.1 Recall addition facts for single-digit numbers and related subtraction facts to develop increasingly efficient mental strategies for computation	1	Adding multiples of 100, 1000 and 10 000	<ul> <li>model the addition of hundreds and/or thousands using place value equipment or play money; relate these additions to adding ones, eg 4 + 3 = 7 so 4 thousands + 3 thousands = 7 thousands or 4000 + 3000 = 7000</li> <li>use known basic facts, eg 5 + 3 to add multiples of 100, 1000 or 10 000 using place value knowledge and pattern identification, eg 5 +</li> </ul>	
		Subtracting multiples of 100, 1000 and 10 000	<ul> <li>3 = 8, so 500 + 300 = 800, 5000 + 3000 = 8000 and 50 000 + 30 000 = 80 000</li> <li>model the subtraction of hundreds and/or thousands using place value equipment or play money; relate these additions to subtracting ones, eg 8 - 3 = 5 so 8 thousands - 3 thousands = 5 thousands or 8000 - 3000 = 5000</li> </ul>	
			<ul> <li>use known basic facts, eg 9 – 5 to subtract multiples of 100, 1000 or 10 000 using place value knowledge and pattern identification, eg 9 – 5 = 4, so 900 – 500 = 400, 9000 – 5000 = 4000 and 90 000 – 50 000 = 40 000</li> </ul>	
	3	Adding multiple single- digit numbers	• use the associative property of addition to make easier additions when possible, eg doubles or near doubles, pairs that add to a ten	
	Learni	ng Journeys Add/Subt	tract: non-standard/place value partitioning	
NA.B.1 Recall addition facts for single-digit numbers and related subtraction facts to develop increasingly efficient mental strategies for computation	1	Adding two 3-digit numbers using non- standard partitioning	<ul> <li>partition the second number using non-standard partitioning to add two 3-digit numbers, eg 1546 + 625 as 546 + 500 + 100 + 20 + 5</li> <li>record and explain the strategy using numerals, models and/or diagrams</li> </ul>	
	2	Subtracting two 3-digit numbers using non- standard partitioning	<ul> <li>partition the second number using non-standard partitioning to subtract two 3-digit numbers, eg 1546 – 625 as 546 – 500 – 100 – 20 –</li> <li>record and explain the strategy using numerals, models and/or diagrams</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers

five-digit numbers				
Quest: (1) Add/sub up to 5 digits				
Learning Journeys Add/Subtract: Choosing efficient strategies				
Content Descriptor	Steps	Spine Nodes	Subnodes	
NA.B.1 Recall addition facts for single-digit numbers and related subtraction facts to develop increasingly efficient mental strategies for computation	1	Choosing efficient addition strategies when adding 2-digit and 3-digit numbers	<ul> <li>solve 2-digit and 3-digit addition problems using efficient and effective strategies depending on the numbers in the problem, eg use rounding and compensating, jump strategies, split strategies, place value strategies or bridging strategies</li> <li>record and explain the strategy using numerals, models and/or diagrams</li> <li>check the solution using a different strategy; compare with own and others' strategies, discuss and compare the efficiency of strategies</li> </ul>	
	2	Choosing efficient subtraction strategies when subtracting 2-digit and 3-digit numbers	<ul> <li>solve 2-digit and 3-digit subtraction problems using efficient and effective strategies depending on the numbers in the problem, eg use rounding and compensating, jump strategies, split strategies, place value strategies or bridging strategies</li> <li>record and explain the strategy using numerals, models and/or diagrams</li> <li>check the solution using a different strategy; compare with own and others' strategies, discuss and compare the efficiency of strategies</li> </ul>	
	3	Choosing efficient addition and subtraction strategies when adding or subtracting 2-digit and 3-digit numbers	<ul> <li>solve 2-digit and 3-digit addition and subtraction problems using efficient and effective strategies depending on the numbers in the problem, eg use rounding and compensating, jump strategies, split strategies, place value strategies or bridging strategies</li> <li>record and explain the strategy using numerals, models and/or diagrams</li> <li>check the solution using a different strategy; compare with own and others' strategies, discuss and compare the efficiency of strategies</li> </ul>	
		Learning Journ	eys Add/Subtract: Estimating	
NA.B.1 Recall addition facts for single-digit numbers and related subtraction facts to develop increasingly efficient mental strategies for computation	1	Estimating additions	<ul> <li>round numbers to the nearest multiple of 100 to estimate additions, eg 546 + 789 as 500 + 800</li> <li>round numbers to the nearest multiple of 10 or 100 to estimate additions, eg 546 + 789 as 540 + 80</li> <li>explain the reason for the estimation used and whether the estimation is higher or lower than the actual answer</li> </ul>	
	2	Estimating subtractions	<ul> <li>round numbers to the nearest multiple of 100 to estimate subtractions, eg 546 - 189 as 500 - 200</li> <li>round numbers to the nearest multiple of 10 or 100 to estimate subtractions, eg 746 - 389 as 740 - 400</li> <li>explain the reason for the estimation used and whether the estimation is higher or lower than the actual answer</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers				
			Add/sub up to 5 digits	
	Lear	rning Journeys Relation	onship between addition and subtraction	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Recognising and using the inverse relationship between addition and subtraction	<ul> <li>determine, through investigation, the inverse relationship between addition and subtraction</li> <li>determine the missing number in addition and subtraction equations using a variety of tools and strategies, such as the inverse relationship between addition and subtraction (up to 2 digit with 2-digit addition or subtraction)</li> </ul>	
NA.B.2 Recognise and explain the connection between addition and subtraction	2	Recognising equivalent number sentences with 1-digit and 2- digit numbers	<ul> <li>complete number sentences involving addition and subtraction by calculating missing numbers using a variety of tools and strategies</li> <li>use inverse operations to complete number sentences</li> <li>ustify solutions when completing number sentences</li> </ul>	
	3	Judging the reasonableness of addition and subtraction answers (up to 3-digit answers)	use benchmarks of 'more than or less than' to help judge the reasonableness of answers	
		Learning Journe	ys Representing money values	
NA.B.3 Represent money values in multiple ways and	1	Using money to make purchases	<ul> <li>calculate the total cost of purchasing two items given their values and record the value in dollars and cents separately (no decimal point)</li> <li>determine the exact notes and coins needed to purchase two items given their values</li> </ul>	
count the change required for simple transactions to the nearest five cents	2	Calculating change when making purchases	<ul> <li>determine one or more notes and coins that have enough value to make a purchase of one or more items</li> <li>calculate the change required when making purchases using cash and record values in dollars and cents separately (no decimal point)</li> </ul>	
		Quest: (2)	) Add/sub up to 5 digits	
	Le	earning Journeys Rep	resenting problems using a bar model	
NA.B.4 Apply place value to partition, rearrange and regroup numbers to at least tens of thousands to assist calculations and solve problems	1	Representing addition problems using a bar model (within 1000)	<ul> <li>represent an addition problem where the result is unknown, eg 'Anna had 58 marbles. Sam gave her 27 more. How many marbles does Anna have now?'</li> <li>represent addition problems where the change or part is unknown, eg 'Anna has 58 marbles, how many more does she need to have 73? or Anna had 53 marbles. 17 were yellow. How many were red?'</li> <li>represent addition problems where the start is unknown, eg 'Anna had some marbles. Sam gave her 17 more. Now she has 53. How many did she have to start with?'</li> <li>solve addition problems represented on a bar model using</li> </ul>	

efficient mental strategies



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and

five-digit numbers					
	Quest: (2) Add/sub up to 5 digits				
	Le	earning Journeys Rep	resenting problems using a bar model		
Content Descriptor	Steps	Spine Nodes	Subnodes		
	2	Representing subtraction problems using a bar model (within 1000)	<ul> <li>represent subtraction problems where the result is unknown, ag 'Anna had 52 marbles. She gave 17 to Sam. How many marbles does she have left?'</li> <li>represent and solve subtraction problems where the change is unknown, eg 'Anna had 52 marbles. She gave some to Sam. Now she has 15 left. How many marbles did she give to Sam?'</li> <li>represent and solve subtraction problems where the start is</li> </ul>		
NA.B.4 Apply place value to partition, rearrange and			unknown, eg 'Anna gave 27 marbles to Sam. Now she has 5 marbles left. How many marbles did Anna begin with?'  • solve subtraction problems represented on a bar model using		
regroup numbers to at least tens			efficient mental strategies		
of thousands to assist calculations and solve			• represent and solve comparison problems where the difference is unknown, eg 'Anna has 13 plums. Sam has 7 plums. How many more plums does Anna have?'\		
problems	3	Representing comparison problems using a bar model (within 1000)	• represent and solve comparison problems where the referent is unknown, eg 'Anna has 43 marbles. She has 17 more than Sam. How many marbles does Sam have?'		
			<ul> <li>represent and solve subtraction problems where the comparison quantity is unknown, eg 'Sam has 17 marbles. Anna has 35 more marbles. How many marbles does Anna have?'</li> </ul>		
			solve comparison problems represented on a bar model using efficient mental strategies		
	Learn	ing Journeys Add/Sub	tract: Efficient strategies & word problems		
	1	Choosing efficient mental addition strategies with numbers up to five	<ul> <li>apply place value and partitioning to rearrange and regroup numbers to assist with calculations, eg use rounding and compensating, bar model, jump strategies, split strategies, place value strategies or bridging strategies</li> </ul>		
		digits	use a range of recording methods to solve addition problems, eg number sentences, empty number line, regrouping		
NA.B.4 Apply place value to partition, rearrange and regroup numbers to at least tens of thousands to	2	Solving one-step word problems using efficient mental addition strategies with numbers up to five digits	solve addition word problems using mental strategies		
of thousands to assist calculations and solve problems	3	Choosing efficient mental subtraction strategies with numbers up to five	apply place value and partitioning to rearrange and regroup numbers to assist with calculations, eg use rounding and compensating, jump strategies, split strategies, place value strategies or bridging strategies		
		digits	• use a range of recording methods to solve subtraction problems, eg number sentences, empty number line, regrouping		
	4	Solving word problems using efficient mental subtraction strategies with numbers up to five digits	solve subtraction word problems using mental strategies		



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers

five-digit numbers					
	Quest: (2) Add/sub up to 5 digits				
Learning Journeys Add/Subtract: pose problems, number ranges					
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.B.4 Apply place value to partition, rearrange and	1	Posing simple addition problems	<ul> <li>pose a simple word problem to represent an addition number sentence</li> <li>select number ranges that are appropriate for the context</li> </ul>		
regroup numbers to at least tens of thousands to assist calculations and solve problems	2	Posing simple subtraction problems	<ul> <li>pose a simple word problem to represent a subtraction number sentence; represent both 'take away' and 'comparison' problems</li> <li>select number ranges that are appropriate for the context; must take the smaller value away from the larger value</li> </ul>		
	Le	earning Journeys Add	dition: Algorithm (without regrouping)		
NA.B.4 Apply place value to partition, rearrange and regroup numbers to at least tens of thousands to assist calculations and solve problems	1	Using a formal written algorithm for addition calculations up to two-digit numbers (no regrouping)	<ul> <li>apply algorithms to solve problems without regrouping, with the same number of places and with a different number of places</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
	2	Using a formal written algorithm for addition calculations up to three-digit numbers (no regrouping)	<ul> <li>apply algorithms to solve problems without regrouping, with the same number of places and with a different number of places</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
	3	Using a formal written algorithm for addition calculations up to four-digit numbers (no regrouping)	<ul> <li>apply algorithms to solve problems without regrouping, with the same number of places and with a different number of places</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
	4	Using a formal written algorithm for addition calculations up to five-digit numbers (no regrouping)	<ul> <li>apply algorithms to solve problems without regrouping, with the same number of places and with a different number of places; include opportunities for students to write their own algorithms with digits in correct place value positions; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
		Learning Journeys A	ddition: Algorithm (with regrouping)		
NA.B.4 Apply place value to partition, rearrange and regroup numbers to at least tens of thousands to assist calculations and solve problems	1	Using a formal written algorithm for addition calculations up to two-digit numbers (with regrouping)	<ul> <li>apply algorithms to solve problems with regrouping in 1 or more places, with the same number of places and with a different number of places</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers

	five-digit numbers				
	Quest: (2) Add/sub up to 5 digits				
Learning Journeys Addition: Algorithm (with regrouping)					
Content Descriptor	Steps	Spine Nodes	Subnodes		
		Using a formal written algorithm for addition calculations with three-digit and one-digit numbers (with regrouping)	<ul> <li>apply algorithms to solve problems with regrouping; include opportunities for students to write their own algorithms with digits in correct place value positions; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
	2	Using a formal written algorithm for addition calculations with three-digit and two-digit numbers (with regrouping)	<ul> <li>apply algorithms to solve problems with regrouping in 1 or more places; include opportunities for students to write their own algorithms with digits in correct place value positions; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
NA.B.4 Apply place value to partition, rearrange and regroup numbers to at least tens of thousands to assist calculations and solve problems	3	Using a formal written algorithm for addition calculations of two three-digit numbers (with regrouping)	<ul> <li>apply algorithms to solve problems with regrouping in 1 or more places; include opportunities for students to write their own algorithms with digits in correct place value positions; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
		Using a formal written algorithm for addition calculations up to three-digit numbers (with regrouping)	<ul> <li>apply algorithms to solve problems with regrouping in 1 or more places, with the same number of places and with a different number of places; include opportunities for students to write their own algorithms with digits in correct place value positions; include word problems</li> <li>use estimation or reverse operation to check the reasonableness</li> </ul>		
	4	Using a formal written algorithm for addition calculations up to four-digit numbers (with regrouping)	<ul> <li>of solutions</li> <li>apply algorithms to solve problems with regrouping in 1 or more places, with the same number of places and with a different number of places; include opportunities for students to write their own algorithms with digits in correct place value positions; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
	5	Using a formal written algorithm for addition calculations up to five-digit numbers (with regrouping)	<ul> <li>apply algorithms to solve problems with regrouping in 1 or more places, with the same number of places and with a different number of places; include opportunities for students to write their own algorithms with digits in correct place value positions; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers					
	Quest: (2) Add/sub up to 5 digits				
	Lear	ning Journeys Addition: Al	gorithm (with/without regrouping)		
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Using a formal written algorithm for addition calculations of 3 or more addends up to two digits (with and without regrouping)	apply algorithms with 3 or more addends with the same number of places and with a different number of places		
NA.B.4 Apply place value to partition, rearrange and regroup numbers	2	Using a formal written algorithm for addition calculations of 3 or more addends up to 3 digits (with and without regrouping)	<ul> <li>apply algorithms with 3 or more addends with the same number of places and with a different number of places; include number range that involves regrouping more than 1 ten or hundred; include word problems</li> <li>use estimation to check the reasonableness of solutions</li> </ul>		
to at least tens of thousands to assist calculations and solve problems	3	Using a formal written algorithm for addition calculations of 3 or more addends up to four digits (with and without regrouping)	<ul> <li>apply algorithms with 3 or more addends with the same number of places and with a different number of places; include number range that involves regrouping more than 1 ten, hundred or thousand; include word problems</li> </ul>		
	4	Using a formal written algorithm for addition calculations of 3 or more addends up to 5 digits (with and without regrouping)	apply algorithms with 3 or more addends with the same number of places and with a different number of places; include number range that involves regrouping more than 1 in one or more places; include word problems		
	Lear	ning Journeys Subtraction:	: Algorithm (without decomposing)		
NA.B.4 Apply place value to partition, rearrange and regroup numbers to at least tens of thousands to assist calculations and solve problems	1	Using a formal written algorithm to record subtraction calculations involving up to twodigit numbers (without decomposing)	<ul> <li>apply algorithms to solve problems without trading (decomposing), with the same number of places for both numbers, with fewer places in the second number (subtrahend) and with and without 1 or more zeros in the first number (minuend); include opportunities for students to write their own algorithms with digits in correct place value positions and with the larger number first; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
	2	Using a formal written algorithm to record subtraction calculations involving up to threedigit numbers (without decomposing)	<ul> <li>apply algorithms to solve problems without trading (decomposing), with the same number of places for both numbers, with fewer places in the second number (subtrahend) and with and without 1 or more zeros in the first number (minuend); include opportunities for students to write their own algorithms with digits in correct place value positions and with the larger number first; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers

five-digit numbers					
Quest: (2) Add/sub up to 5 digits					
Learning Journeys Subtraction: Algorithm (without decomposing)					
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.B.4 Apply place value to partition, rearrange and regroup numbers to at least tens of thousands to assist calculations and solve problems	3	Using a formal written algorithm to record subtraction calculations involving up to fourdigit numbers (without decomposing)	<ul> <li>apply algorithms to solve problems without trading (decomposing), with the same number of places for both numbers, with fewer places in the second number (subtrahend) and with and without 1 or more zeros in the first number (minuend); include opportunities for students to write their own algorithms with digits in correct place value positions and with the larger number first; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
	4	Using a formal written algorithm to record subtraction calculations involving up to fivedigit numbers (without decomposing)	apply algorithms to solve problems without trading (decomposing), with the same number of places for both numbers, with fewer places in the second number (subtrahend) and with and without 1 or more zeros in the first number (minuend); include opportunities for students to write their own algorithms with digits in correct place value positions and with the larger number first; include word problems		
			use estimation or reverse operation to check the reasonableness of solutions		
	Lea	arning Journeys Subtractio	n: Algorithm (with decomposing)		
NA.B.4 Apply place value to partition, rearrange and regroup numbers to at least tens of thousands to assist calculations and solve problems	1	Using a formal written algorithm to record subtraction calculations involving up to twodigit numbers (with decomposing)	<ul> <li>apply algorithms to solve problems with trading (decomposing) in one or more places, with the same number of places for both numbers, with fewer places in the second number (subtrahend) and with and without one or more zeros in the first number (minuend); include opportunities for students to write their own algorithms with digits in correct place value positions and with the larger number first; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
	2	Using a formal written algorithm to record subtraction calculations involving up to threedigit numbers (with decomposing)	<ul> <li>apply algorithms to solve problems with trading (decomposing) in 1 or more places, with the same number of places for both numbers, with fewer places in the second number (subtrahend) and with and without 1 or more zeros in the first number (minuend); include opportunities for students to write their own algorithms with digits in correct place value positions and with the larger number first; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-5NA uses mental and written strategies for addition and subtraction involving two-, three-, four- and five-digit numbers

five-digit numbers					
	Quest: (2) Add/sub up to 5 digits				
	Learning Journeys Subtraction: Algorithm (with decomposing)				
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.B.4 Apply place value to partition, rearrange and regroup numbers to at least tens of thousands to assist calculations and solve problems	3	Using a formal written algorithm to record subtraction calculations involving up to fourdigit numbers (with decomposing)	<ul> <li>apply algorithms to solve problems with trading (decomposing) in 1 or more places, with the same number of places for both numbers, with fewer places in the second number (subtrahend) and with and without 1 or more zeros in the first number (minuend); include opportunities for students to write their own algorithms with digits in correct place value positions and with the larger number first; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
	4	Using a formal written algorithm to record subtraction calculations involving up to fivedigit numbers (with decomposing)	<ul> <li>apply algorithms to solve problems with trading (decomposing) in 1 or more places, with the same number of places for both numbers, with fewer places in the second number (subtrahend) and with and without 1 or more zeros in the first number (minuend); include opportunities for students to write their own algorithms with digits in correct place value positions and with the larger number first; include word problems</li> <li>use estimation or reverse operation to check the reasonableness of solutions</li> </ul>		
		Learning Journeys Add	/Subtract: Word problems		
NA.B.4 Apply place		Learning Journeys Add	Asubtract. Word problems		
value to partition, rearrange and regroup numbers to at least tens of thousands to assist calculations and solve problems	1	Solving addition and subtraction two-step problems in context (max sum 1000)	<ul> <li>read and interpret a word problem</li> <li>decide with operations and strategies to use and explain why</li> <li>solve an addition and subtraction two-step problem</li> </ul>		
		<b>Learning Journeys</b>	Add/Subtract: Money		
NA.B.4 Apply place value to partition, rearrange and regroup numbers to at least tens of thousands to assist	1	Using decimals to represent money	<ul> <li>recognise that 1 cent is one-hundredth of a dollar and connect decimal notation to money values in dollars and cents</li> <li>calculate the total value of a group of notes and coins and record this value using decimal notation and the symbol \$</li> <li>combine amounts of notes and coins to make a given amount of money in decimal notation</li> <li>use the symbols \$ and c correctly when recording amounts of money</li> </ul>		
calculations and solve problems	2	Using money: Addition and subtraction problems	<ul> <li>use addition and subtraction to solve a variety of problems involving purchases of two or more items, including calculating change, and record the value using a decimal point and the symbol \$</li> <li>use estimation to check the reasonableness of solutions to problems involving purchases and calculation of change</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

MA2-6NA uses mental and informal written strategies for multiplication and division					
	Quest: (1) Mult/div mental strategies				
	Learning Journeys Skip counting by 10 to 1000				
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Counting by skip counting forwards by 10s from any multiple of 10 to 1000			
NA.C.1 Recall multiplication facts of two, three, five and ten and related division facts	2	Counting by skip counting backwards by 10s from any multiple of 10 up to 1000	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count backwards by 10s from any multiple of 10 up to 1000</li> <li>skip count backwards by 10s from any multiple of 10 by memory and an understanding of the number sequence</li> <li>recognise an error in the skip counting sequence</li> </ul>		
division facts	3	Counting by skip counting forwards or backwards by 10s from any multiple of 10 up to 1000	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count forwards or backwards by 10s from any multiple of 10 up to 1000</li> <li>skip count forwards or backwards by 10s from any multiple of 10 by memory and an understanding of the number sequence</li> <li>recognise an error in the skip counting sequence</li> </ul>		
		Learning Journe	eys Skip counting by 2 to 1000		
NA.C.1 Recall multiplication facts	1	Counting by skip counting forwards by 2s from any multiple of 2 to 1000	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count forwards by 2s from any multiple of 2 up to 1000</li> <li>skip count forwards by 2s from any multiple of 2 by memory and an understanding of the number sequence</li> <li>recognise an error in the skip counting sequence</li> </ul>		
of two, three, five and ten and related division facts	2	Counting by skip counting backwards by 2s from any multiple of 2 up to 1000	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count backwards by 2s from any multiple of 2 up to 1000</li> <li>skip count backwards by 2s from any multiple of 2 by memory and an understanding of the number sequence</li> <li>recognise an error in the skip counting sequence</li> </ul>		
		Learning Journe	eys Skip counting by 5 to 1000		
	1	Counting by skip counting forwards by 5s from any multiple of 5 to 1000	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count forwards by 5s from any multiple of 5 up to 1000</li> <li>skip count forwards by 5s from any multiple of 5 by memory and an understanding of the number sequence</li> <li>recognise an error in the skip counting sequence</li> </ul>		
NA.C.1 Recall		Counting by skip counting backwards	use concrete materials, models, drawings, number lines/charts to skip count backwards by 5s from any multiple of 5 up to 1000		
multiplication facts of two, three, five and ten and related division facts		by 5s from any multiple of 5 up to 1000	<ul> <li>skip count backwards by 5s from any multiple of 5 by memory and an understanding of the number sequence</li> <li>recognise an error in the skip counting sequence</li> </ul>		
	3	Counting by skip counting forwards or backwards by 5s from any multiple of 5 up to 1000	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count forwards or backwards by 5s from any multiple of 5 up to 1000</li> <li>skip count forwards or backwards by 5s from any multiple of 5 by memory and an understanding of the number sequence</li> <li>recognise an error in the skip counting sequence</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

MA2-6NA uses mental and informal written strategies for multiplication and division				
	Quest: (1) Mult/div mental strategies			
		Learning Journe	eys Skip counting by 3 to 1000	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Counting by skip counting forwards by 3s from zero up to 30	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count by 3s from zero</li> <li>use rhythmic counting to count in 3s from zero</li> <li>recognise an error in the skip counting sequence</li> </ul>	
	2	Counting by skip counting backwards by 3s from 30	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count backwards by 3s from 30</li> <li>use rhythmic counting to count backwards in 3s from 30</li> <li>recognise an error in the skip counting sequence</li> </ul>	
NA.C.1 Recall multiplication facts	3	Counting by skip counting forwards by 3s from any multiple of 3 up to 30	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count by 3s from any multiple of 3</li> <li>use knowledge of the number sequence to count in 3s from any multiple of 3</li> <li>recognise an error in the skip counting sequence</li> </ul>	
of two, three, five and ten and related division facts	4	Counting by skip counting backwards by 3s from any multiple of 3 from 30	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count backwards by 3s from 30</li> <li>use knowledge of the number sequence to count in backwards in 3s from any multiple of 3</li> <li>recognise an error in the skip counting sequence</li> </ul>	
	counting forwards by 3s zero up to 30  Counting by skip counting forward backwards by 3s	Counting by skip counting forwards or backwards by 3s from zero up to 30	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count by 3s</li> <li>use rhythmic counting to count in 3s</li> <li>recognise an error in the skip counting sequence</li> </ul>	
		Counting by skip counting forwards or backwards by 3s from any multiple of 3 from zero to 30	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count by 3s</li> <li>use knowledge of the number sequence to count forwards or backwards in 3s from any multiple of 3</li> <li>recognise an error in the skip counting sequence</li> </ul>	
		Learning Jo	urneys Skip counting by 4	
NA.C.1 Recall multiplication facts of two, three, five and ten and related division facts	1	Counting by skip counting forwards by 4s from zero up to 40	<ul> <li>use concrete materials, models, drawings, number lines/charts to skip count by 4s from zero</li> <li>use rhythmic counting to count in 4s from zero</li> <li>recognise an error in the skip counting sequence</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

MA2-6NA uses mental and informal written strategies for multiplication and division				
		Quest: (1) M	fult/div mental strategies	
		Learning Journeys	Multiplication/Division facts for 2	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Recalling multiplication facts for 2	recall the 2 multiplication facts	
NA.C.1 Recall	2	Using multiplication facts for 2	solve and create multiplication problems in context (using multiplication facts for 2), including word problems	
multiplication facts of two, three, five and ten and related	3	Recalling the division facts for 2	• recall the division facts for 2	
division facts	4	Using division facts for 2	solve and create division problems in context (using multiplication facts for 2), including word problems	
	5	Multiplying and dividing by 2	<ul> <li>recall the multiplication and division facts for 2</li> <li>solve and create multiplication and division problems in context (using multiplication facts for 2), including word problems</li> </ul>	
		Learning Journeys	Multiplication/Division facts for 10	
	1	Recalling the multiplication facts for 10	• recall the 10 multiplication facts	
NA.C.1 Recall	2	Using multiplication facts for 10	<ul> <li>solve and create multiplication problems in context (using multiplication facts for 10), including word problems</li> </ul>	
multiplication facts of two, three, five and ten and related	3	Recalling the division facts for 10	recall the division facts for 10	
division facts	4	Using division facts for 10	<ul> <li>solve and create division problems in context (using multiplication facts for 10), including word problems</li> </ul>	
	5	Multiplying and dividing by 10	<ul> <li>recall the multiplication and division facts for 10</li> <li>solve and create multiplication and division problems in context (using multiplication facts for 10), including word problems</li> </ul>	
		Learning Journeys	Multiplication/Division facts for 5	
	1	Recalling multiplication facts for 5	recall the 5 multiplication facts	
NA.C.1 Recall multiplication facts of two, three, five and ten and related division facts	2	Using multiplication facts for 5	<ul> <li>solve and create multiplication problems in context (using multiplication facts for 5), including word problems</li> </ul>	
	3	Recalling the division facts for 5	• recall the division facts for 5	
	4	Using division facts for 5	solve and create division problems in context (using multiplication facts for 5), including word problems	
	5	Multiplying and dividing by 5	<ul> <li>recall the multiplication and division facts for 5</li> <li>solve and create multiplication and division problems in context (using multiplication facts for 5), including word problems</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

MA2-6	MA2-6NA uses mental and informal written strategies for multiplication and division				
	Quest: (1) Mult/div mental strategies				
	ı	earning Journeys M	ultiplication/Division facts for 2, 5, 10		
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Multiplying by 2s, 5s and 10s	<ul> <li>recall the multiplication facts for 2s, 5s and 10s</li> <li>solve multiplication problems with 2, 5 or 10, including word problems; use the multiplication symbol</li> </ul>		
NA.C.1 Recall multiplication facts of two, three, five and ten and related	2	Dividing by 2s, 5s and 10s	<ul> <li>recall the division facts for 2s, 5s and 10s</li> <li>solve division problems with 2, 5 or 10, including word problems; use the division symbol</li> </ul>		
and ten and related division facts	3	Multiplying and dividing by 2s, 5s and 10s	<ul> <li>recall the multiplication facts and related division facts for 2s, 5s and 10s</li> <li>solve multiplication and division problems with 2, 5 or 10, including word problems; use the multiplication symbol</li> </ul>		
		Learning Journeys	Multiplication/Division facts for 3		
	1	Exploring multiplication by 3	<ul> <li>relate multiplication by 3 to doubles and 1 more group; model and describe, eg '3 groups of 4 is the same as double 4 and one more group of 4'</li> <li>explore patterns of the multiplication facts for 3 on a number chart</li> <li>model the 2 related multiplication facts, eg 3 x 4 and 4 x 3</li> </ul>		
	2	Recalling multiplication facts for 3	• recall the multiplication facts for 3		
NA.C.1 Recall multiplication facts		Using multiplication facts for 3	solve and create multiplication problems in context (using multiplication facts for 3), including word problems		
of two, three, five and ten and related division facts	3	Dividing by 3	<ul> <li>model and describe the related multiplication and division facts for 3 using models, drawings or manipulatives, eg 5 x 3 = 15 and 15 divided by 3 = 5</li> <li>relate division to how many (whole) times the divisor goes into the dividend</li> </ul>		
		Recalling the division facts for 3	• recall the division facts for 3		
	4	Using division facts for 3	<ul> <li>solve and create division problems in context (using multiplication facts for 3), including word problems</li> </ul>		
	5	Multiplying and dividing by 3	<ul> <li>recall the multiplication facts and related division facts for 3</li> <li>solve multiplication and division problems with 3, including word problems</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

MA2-6I	MA2-6NA uses mental and informal written strategies for multiplication and division				
	Quest: (1) Mult/div mental strategies				
		Learning Journeys	Multiplication word problems		
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Writing and solving simple multiplication word problems (within 100)	<ul> <li>pose appropriate multiplication problems (up to 10 x 10)</li> <li>solve multiplication word problems and explain using language, action, drawings, models</li> <li>compare their own and others' methods of solution</li> </ul>		
			solve fair share multiplication or division problems (with unknown in any position), eg '20 flowers are to be placed in 4 bunches, how many flowers will be in each bunch?'		
NA.C.2 Represent	2	Solving multiplication problems using fair shares or equal grouping (within 100)	• solve equal grouping multiplication or division problems (with unknown in any position), eg 'There are 9 tables in a cafeteria. Each table has 5 chairs. What is the total number of chairs in the cafeteria?'		
and solve problems involving multiplication using			• write equations using a symbol, eg a box or a blank, to represent the unknown number		
efficient mental and			compare their own and others' methods of solution		
written strategies and appropriate digital technologies	3	Solving multiplication and division problems involving arrays (within 100)	• solve multiplication and division problems (with the unknown in any position) involving arrays, eg 'A rectangular egg carton has 3 rows and 4 columns of eggs. How many eggs are there?'		
			• write equations using a symbol, eg a box or a blank, to represent the unknown number		
			compare their own and others' methods of solution		
	4	Solving multiplication and division problems	<ul> <li>solve multiplication and division problems involving comparisons eg 'Anna has 3 times as much money as David. David has \$6. How much money does Anna have?'</li> </ul>		
		involving comparisons (within 100)	• write equations using a symbol, eg a box or a blank, to represent the unknown number		
			compare their own and others' methods of solution		
		Learning Journeys Wo	rd problems and missing numbers		
	1	Finding the missing number to make a multiplication number sentence true (2, 5, 10 facts)	<ul> <li>complete number sentences involving 1 operation of multiplication by finding the missing number using a variety of tools, equipment and strategies, eg 3 x? = 30 or? X 2 = 18 or 5 x 3 =?</li> </ul>		
NA.C.2 Represent and solve problems involving multiplication using efficient mental and written strategies and appropriate digital technologies	2	Finding the missing number to make a division number sentence true (2, 5, 10 facts)	• complete number sentences involving 1 operation of division by finding the missing numb using a variety of tools, equipment and strategies eg $40 \div 10 = ?$ , or $35 \div ? = 7$ or $? \div 2 = 9$		
	3	Solving simple two- step word problems with addition and subtraction (max sum of 100)	<ul> <li>read and represent a two-step word problem using a letter for the unknown quantity</li> <li>solve the problem using a variety of tools, models and strategies</li> </ul>		
	4	Solving two-step word problems with the four operations (2, 5, 10 multiplication facts)	<ul> <li>use the four operations to solve two-step word problems</li> <li>represent an unknown quantity with a letter</li> <li>solve the problem using a variety of tools, models and strategies</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

MA2-6NA uses mental and informal written strategies for multiplication and division				
Quest: (2) Mult/div mental strategies				
		Learning Journeys Mu	ultiplication/Division facts for 4	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Recalling multiplication facts for 4	• recall the multiplication facts for 4	
	'	Using multiplication facts for 4	solve and create multiplication problems in context (using multiplication facts for 4), including word problems	
NA.C.3 Recall		Dividing by 4	<ul> <li>model and describe the related multiplication and division facts for 4 using models, drawings or manipulatives, eg 4 x 3 = 12 and 12 divided by 3 = 4</li> </ul>	
multiplication facts up to 10 × 10 and related division	2		relate division to how many (whole) times the divisor goes into the dividend	
facts		Recalling division facts for 4	• recall the division facts for 4	
	3	Using division facts for 4	solve and create division problems in context (using multiplication facts for 4), including word problems	
	4	Multiplying and dividing by 4	<ul> <li>recall the multiplication facts and related division facts for 4</li> <li>solve multiplication and division problems with 4, including word problems</li> </ul>	
		Learning Journeys Mul	tiplication/Division facts up to 5	
	1	Multiplying by 2, 5, 3 and 4 (1 - 10)	<ul> <li>recall the multiplication facts for 2s, 5s, 3s and 4s</li> <li>solve multiplication problems with 2, 5, 3 and 4, including word problems</li> </ul>	
NA.C.3 Recall multiplication facts up to 10 × 10 and	2	Dividing by 2, 5, 3 and 4 (1 - 10)	<ul> <li>recall the division facts for 2s, 5s, 3s and 4s</li> <li>solve division problems with 2, 5, 3 and 4, including word problems</li> </ul>	
related division facts	3	Multiplying and dividing by 2, 5, 3 and 4 (1 - 10)	<ul> <li>recall the multiplication and division facts for 2s, 5s, 3s and 4s</li> <li>solve multiplication and division problems with 2, 5, 3 and 4, including word problems</li> </ul>	
	4	Recalling multiplication facts to 5 x 5	• recall multiplication facts to 5 x 5	
	Lear	ning Journeys Multiplica	ation and division facts and properties	
	1	Relating multiplication	<ul> <li>model and describe the fact families for 2, 3, 4, 5 and 10 multiplication facts, eg 3 x 4 = 12, 4 x 3 = 12, 12 divided by 3 = 4 and 12 divided by 4 equals 3</li> </ul>	
NA.C.3 Recall multiplication facts up to 10 × 10 and related division	ı	and division facts through fact families	• explain why a rectangular array can be read as a division in 2 ways by forming vertical or horizontal groups, eg 12 $\div$ 3 = 4 or 12 $\div$ 4 = 3	
		Recalling multiplication	<ul><li>recall facts in order</li><li>recall facts in random order</li></ul>	
facts	2	facts up to 10 × 10 with automaticity	<ul> <li>recall facts in random order</li> <li>create a table or simple spreadsheet to record multiplication facts</li> </ul>	
	3	Using the commutative property of multiplication up to 10 x 10	• use the commutative property of multiplication, eg $7 \times 9 = 9 \times 7$	



### **Understanding Practice and Fluency (UPF)**

MA2-6NA uses mental and informal written strategies for multiplication and division				
	Quest: (2) Mult/div mental strategies			
	Lear	rning Journeys Exploring	g multiplication/division for 6 up to 60	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Exploring multiplication by 6 up to 60	<ul> <li>use concrete materials, models, drawings, number lines/ charts to skip count by 6 from zero; explore patterns of the multiplication facts for 6 on a number chart</li> <li>relate multiplication by 6 to double multiplication by 3</li> </ul>	
	2	Recalling and using multiplication facts for 6 (up to 60)	<ul> <li>recall the multiplication facts for 6</li> <li>solve multiplication problems with 6 including word problems</li> </ul>	
NA.C.3 Recall multiplication facts up to 10 × 10 and related division facts	3	Dividing by 6 up to 60	<ul> <li>model and describe the related multiplication and division facts for 6 using models, drawings or manipulatives, eg 6 x 3 = 18 and 18 divided by 3 = 6</li> <li>relate division to how many (whole) times the divisor goes into the dividend</li> </ul>	
	4	Recalling and using division facts for 6 up to 60	<ul><li>recall the division facts for 6</li><li>solve division problems with 6 including word problems</li></ul>	
	5	Multiplying and dividing by 6 up to 60	<ul> <li>recall the multiplication facts and related division facts for 6</li> <li>solve multiplication and division problems with 6, including word problems</li> </ul>	
	Lear	rning Journeys Exploring	g multiplication/division for 7 up to 70	
	1	Exploring multiplication by 7 up to 70	<ul> <li>use concrete materials, models, drawings, number lines/ charts to skip count by 7 from zero; explore patterns of the multiplication facts for 7 on a number chart</li> </ul>	
	2	Recalling and using multiplication facts for 7 (up to 70)	<ul> <li>recall the multiplication facts for 7</li> <li>solve multiplication problems with 7 including word problems</li> </ul>	
NA.C.3 Recall multiplication facts up to 10 × 10 and related division facts	3	Dividing by 7 up to 70	<ul> <li>model and describe the related multiplication and division facts for 7 using models, drawings or manipulatives, eg 7 x 3 = 21 and 21 divided by 3 = 7</li> <li>relate division to how many (whole) times the divisor goes into the dividend</li> </ul>	
	4	Recalling and using division facts for 7 up to 70	<ul> <li>recall the division facts for 7</li> <li>solve division problems with 7 including word problems</li> </ul>	
	5	Multiplying and dividing by 7 up to 70	<ul> <li>recall the multiplication facts and related division facts for 7</li> <li>solve multiplication and division problems with 7, including word problems</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

MA2-6NA uses mental and informal written strategies for multiplication and division			
		Quest: (2) Mult	t/div mental strategies
	Lear	ning Journeys Exploring	g multiplication/division for 8 up to 80
Content Descriptor	Steps	Spine Nodes	Subnodes
	1	Exploring multiplication by 8 up to 80	<ul> <li>use concrete materials, models, drawings, number lines/ charts to skip count by 8 from zero; explore patterns of the multiplication facts for 8 on a number chart</li> <li>relate multiplication by 8 to double multiplication by 4</li> </ul>
	2	Recalling and using multiplication facts for 8 (up to 80)	<ul> <li>recall the multiplication facts for 8</li> <li>solve multiplication problems with 8 including word problems</li> </ul>
NA.C.3 Recall multiplication facts up to 10 × 10 and related division facts	3	Dividing by 8 up to 80	<ul> <li>model and describe the related multiplication and division facts for 8 using models, drawings or manipulatives, eg 8 x 3 = 24 and 24 divided by 3 = 8</li> <li>relate division to how many (whole) times the divisor goes into the dividend</li> </ul>
	4	Recalling and using division facts for 8 up to 80	<ul><li>recall the division facts for 8</li><li>solve division problems with 8 including word problems</li></ul>
	5	Multiplying and dividing by 8 up to 80	<ul> <li>recall the multiplication facts and related division facts for 8</li> <li>solve multiplication and division problems with 8, including word problems</li> </ul>
	Lear	ning Journeys Exploring	g multiplication/division for 9 up to 90
	1	Exploring multiplication by 9 up to 90	<ul> <li>use concrete materials, models, drawings, number lines/ charts to skip count by 9 from zero; explore patterns of the multiplication facts for 9 on a number chart</li> <li>relate multiplication by 9 to multiplication by 10 (multiply by 10 and then subtract the extra group)</li> </ul>
NA C 2 Possil	2	Recalling and using multiplication facts for 9 (up to 90)	<ul> <li>recall the multiplication facts for 9</li> <li>solve multiplication problems with 9 including word problems</li> </ul>
NA.C.3 Recall multiplication facts up to 10 × 10 and related division facts	3	Dividing by 9 up to 90	<ul> <li>model and describe the related multiplication and division facts for 9 using models, drawings or manipulatives, eg 9 x 3 = 27 and 27 divided by 3 = 9</li> <li>relate division to how many (whole) times the divisor goes into the dividend</li> </ul>
	4	Recalling and using division facts for 9 up to 90	<ul> <li>recall the division facts for 9</li> <li>solve division problems with 9 including word problems</li> </ul>
	5	Multiplying and dividing by 9 up to 90	<ul> <li>recall the multiplication facts and related division facts for 9</li> <li>solve multiplication and division problems with 9, including word problems</li> </ul>



### **Understanding Practice and Fluency (UPF)**

MA2-6NA uses mental and informal written strategies for multiplication and division			
Quest: (2) Mult/div mental strategies			
		<b>Learning Journeys</b> Usir	ng facts to multiply using 2-digits
Content Descriptor	Steps	Spine Nodes	Subnodes
NA.C.4 Develop efficient mental and	1	Representing and using known facts to solve multiplication and division problems with multiples of 10 and 100	<ul> <li>represent with models/diagrams and use known facts and place value understanding to solve multiplication problems with multiples of 10 or 100, eg 3 x 6 = 18 so 3 x 600 = 1800</li> <li>use known facts and place value understanding to solve division problems with multiples of 10 or 100, eg 18 ÷ 6 = 3 so 1800 ÷ 600 = 3</li> <li>explain and justify the use of the strategy</li> </ul>
written strategies, and use appropriate digital technologies, for multiplication and for division where there is no	2	Representing and using known facts to multiply two 2-digit multiples of 100	<ul> <li>represent with models/diagrams and use known facts and place value understanding to multiply 2 multiples of 100, eg 300 x 400 = 3 x 4 = 12 so 300 x 400 = 1200</li> <li>know that multiplying by 100 shifts the digits 2 places to the left</li> </ul>
remainder	3	Representing and using known facts to multiply 2-digit numbers by 100	<ul> <li>represent with models/diagrams and use known facts and place value understanding to multiply 2-digit numbers by 100, eg 13 x 100 = 10 x 100 + 3 x 100</li> <li>know that multiplying by 100 shifts the digits 2 places to the left</li> </ul>
	Le	arning Journeys Using f	acts to divide 3-digit numbers by 10
NA.C.4 Develop efficient mental and written strategies, and use appropriate digital technologies, for multiplication and for division where there is no remainder	1	Representing and using known facts to divide 3-digit numbers by 10	<ul> <li>represent with models/diagrams and use known facts and place value understanding to divide 2-digit numbers by 10, eg 460 ÷10 = 46</li> <li>know that dividing by 10 shifts the digits 1 place to the right</li> </ul>
		Learning Journeys Mult	tiplication strategies using 1-digit
	1	Representing and multiplying two 1-digit numbers using rounding and compensating	<ul> <li>represent with models/diagrams and use known facts to solve multiplication problems by adding on or taking off, eg 5 × 10 is 50, so 5 × 9 is 5 less, which is 45</li> <li>explain and justify the use of the strategy</li> </ul>
NA.C.4 Develop efficient mental and written strategies, and use appropriate digital technologies, for multiplication and for division where there is no remainder	2	Representing and multiplying two 1-digit numbers using doubling and related facts	<ul> <li>represent with models/diagrams and use the relationship between multiplication facts, eg the multiplication facts for 6 are double the multiplication facts for 3</li> <li>explain and justify the use of the strategy</li> </ul>
	3	Representing and multiplying two 1-digit numbers using repeated doubling	<ul> <li>represent with models/diagrams and use doubling and repeated doubling as a strategy to multiply by 2, 4 and 8, eg 7 × 8 is double 7, double again and then double again</li> <li>explain and justify the use of the strategy</li> </ul>
	4	Representing and multiplying two 1-digit numbers using factorising	<ul> <li>represent with models/diagrams and split factors, eg 5 × 8 is the same as 5 × 2 × 4, which becomes 10 × 4</li> <li>explain and justify the use of the strategy</li> </ul>



### **Understanding Practice and Fluency (UPF)**

MA2-6NA uses mental and informal written strategies for multiplication and division				
	Quest: (2) Mult/div mental strategies			
	L	earning Journeys Using	the conventions of multiplication	
Content Descriptor	Steps	Spine Nodes	Subnodes	
NA.C.4 Develop efficient mental and written strategies, and use appropriate digital technologies, for multiplication and for division where there is no remainder	1	Using the conventions of multiplication number sentences	<ul> <li>use the term 'product' to describe the result of multiplying 2 or more numbers</li> <li>use the equals sign to record equivalent number relationships involving multiplication, and to mean 'is the same as', rather than to mean to perform an operation</li> </ul>	
		Learning Journeys M	lultiples and factors up to 100	
NA.C.4 Develop efficient mental and written strategies, and use appropriate digital technologies,	1	Introducing multiples up to 100	find 'multiples' for a given whole number	
for multiplication and for division where there is no remainder	2	Introducing factors for numbers up to 100	<ul> <li>determine 'factors' for a given whole number</li> <li>connect number relationships involving multiplication to factors of a number</li> </ul>	
		Learning Jou	urneys Inverse facts	
NA.C.4 Develop efficient mental and written strategies, and use appropriate digital technologies, for multiplication and for division where there is no remainder	1	Using inverse facts	<ul> <li>relate multiplication facts to their inverse division facts</li> <li>relate division facts to their inverse multiplication facts</li> </ul>	
		Learning Journeys Pra	ctising multiplication strategies	
NA.C.4 Develop efficient mental and written strategies, and use appropriate digital technologies, for multiplication and for division where there is no remainder	1	Multiplying 3 or more single-digit numbers using the commutative and associative properties	<ul> <li>apply the commutative property of multiplication</li> <li>explore and apply the associative property of multiplication, eg 2 × 3 × 5 = 2 × 5 × 3 = 10 × 3 = 30</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

MA2-6NA uses mental and informal written strategies for multiplication and division				
	Quest: (2) Mult/div mental strategies			
	Learı	ning Journeys Multiplyin	g 2-digit numbers by a 1-digit number	
Content Descriptor	Steps	Spine Nodes	Subnodes	
NA.C.4 Develop efficient mental and	1	Representing and multiplying a 2-digit number by a 1-digit number using place value understanding and the distributive law	<ul> <li>represent and use place value to solve a multiplication fact, eg multiplying the tens and then the units, eg 7 × 19: 7 tens + 7 nines is 70 + 63, which is 133</li> <li>explain and justify the use of the strategy</li> </ul>	
written strategies, and use appropriate digital technologies, for multiplication and for division where there is no	2	Multiplying a 2-digit number by a 1-digit number using an area model	<ul><li>use area model to solve multiplication problems</li><li>explain and justify the use of the strategy</li></ul>	
remainder	3	Representing and multiplying a 2-digit number by a 1-digit number using doubling and related facts	<ul> <li>represent and use doubling to multiply a 2-digit and 1-digit number, eg 41 × 6 is 41 × 3, which is 123, and then double to obtain 246</li> <li>explain and justify the use of the strategy</li> </ul>	
	Lea	arning Journeys Multiply	ring 2-digits using repeated addition	
NA.C.4 Develop efficient mental and written strategies, and use appropriate digital technologies, for multiplication and for division where there is no remainder	1	Representing and multiplying a 2-digit number by a 2, 4 or 8 using doubling and repeated doubling	<ul> <li>represent and use repeated doubling as a strategy to multiply, eg 23 × 2 is double 23, 23 × 4 is double 23 and double again, 23 × 8 is double 23, double again and double again</li> <li>explain and justify the use of the strategy</li> </ul>	
		Learning Journeys Mult	tiplying 2-digits using factorising	
NA.C.4 Develop efficient mental and written strategies, and use appropriate digital technologies, for multiplication and for division where there is no remainder	1	Representing and multiplying a 2-digit number by a 1-digit number using factorising (the associative property)	<ul> <li>represent and use factorising (factorise the larger number), eg 18 × 4 = 9 × 2 × 4 = 9 × 8 = 72</li> <li>explain and justify the use of the strategy</li> </ul>	
Learning Journeys Selecting effective multiplication strategies				
NA.C.4 Develop efficient mental and written strategies, and use appropriate digital technologies, for multiplication and for division where there is no remainder	1	Selecting efficient strategies to solve multiplication problems	<ul> <li>select and use a variety of mental and informal written strategies to solve multiplication problems</li> <li>apply the inverse relationship of multiplication and division to justify answers</li> <li>check the answer to a word problem using digital technologies</li> <li>record mental strategies accurately</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

MA2-6NA uses mental and informal written strategies for multiplication and division					
	Quest: (2) Mult/div mental strategies				
	Learn	ing Journeys Develop st	trategies for division with no remainder		
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.C.4 Develop efficient mental and written strategies, and use appropriate digital technologies, for multiplication and for division where there is no remainder	1	Describing comparisons using the language of multiplication	• describe comparisons using the language of multiplication, eg $35 = 5 \times 7$ as $35$ is $5$ times as many as $7$ and $7$ times as many as $5$		
	Lea	rning Journeys Dividing	a 2-digit number by a 1 digit number		
NA.C.4 Develop efficient mental and	1	Dividing a 2-digit number by a 1-digit number using the inverse relationship of multiplication and division (no remainders)	• divide a 2-digit number by a 1-digit number using the inverse relationship of multiplication and division, eg 63 $\div$ 9 = 7 because $7 \times 9 = 63$		
written strategies, and use appropriate digital technologies, for multiplication and for division where there is no	2	Dividing a 2-digit number by a 1-digit number using halving and repeated halving (no remainders)	<ul> <li>use halve to divide by 2</li> <li>use halve, halve to divide by 4</li> <li>use halve, halve, halve to divide by 8</li> </ul>		
remainder	3	Dividing a 2-digit number by a 1-digit number using related facts (no remainders)	use related facts to divide a 2-digit number by a 1-digit number, eg to divide by 5, first divide by 10 and then multiply by 2		
		Learning Journeys Ro	emainders in division problems		
NA.C.5 Use mental strategies and informal recording methods for division with remainders	1	Introducing remainders in division problems	<ul> <li>model division, including where the answer involves a remainder, using concrete materials</li> <li>explain why a remainder is obtained in answers to some division problems</li> <li>use mental strategies to divide a 2-digit number by a 1-digit number in problems for which answers include a remainder</li> <li>record remainders to division problems in words</li> <li>interpret the remainder in the context of a word problem</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

MA2-71	MA2-7NA represents, models and compares commonly used fractions and decimals			
	Quest: (1) Common fractions & decimals			
		Learning Journeys Usi	ng fractions: halves and quarters	
Content Descriptor	Steps	Spine Nodes	Subnodes	
NA.D.1 Model and represent unit	1	Finding halves and quarters or objects, shapes or sets (symbols used)	<ul> <li>find halves and quarters of objects and shapes</li> <li>find halves and quarters of sets</li> <li>find the whole from a part</li> <li>find halves and quarters of uneven partitioned shapes</li> <li>use language 'one half', 'two halves', 'one quarter', 'two quarters' and so on</li> <li>use symbols to represent fractions: 1/2, 2/2, 1/4, 2/4, 3/4, 4/4</li> </ul>	
fractions, including 1/2, 1/4,1/3 and 1/5 and their multiples, to a complete whole	2	Counting up to 10 in halves and quarters (symbols used)		
to a complete whole	3	Finding halves, quarters and eighths of objects or shapes	<ul> <li>recognise equivalence</li> <li>estimate the size of a fractional part before using, eg paper folding to check or estimate the size of the whole from the part</li> <li>find the whole from a part</li> <li>find halves, quarters and eighths of uneven partitioned shapes</li> <li>use symbols for halves, quarters and eighths</li> <li>recognise larger denominator = smaller parts</li> </ul>	
		Learning Journeys	Numerator and demonimator	
NA.D.1 Model and represent unit fractions, including 1/2, 1/4,1/3 and 1/5 and their multiples, to a complete whole	1	Introducing the terms numerator and denominator	<ul> <li>read and write symbols to represent fractions</li> <li>use the terms denominator and numerator to describe a fraction</li> </ul>	
	Lea	arning Journeys Using f	ractions: halves, thirds and quarters	
NA.D.1 Model and represent unit fractions, including 1/2, 1/4,1/3 and 1/5 and their multiples, to a complete whole	1	Introducing thirds	<ul> <li>find thirds of objects, shapes and lengths</li> <li>find thirds of sets</li> <li>estimate the size of a fractional part before using eg paper folding to check or estimate the size of the whole from the part</li> <li>find the whole from a part</li> <li>use language 'one third', 'two thirds', 'three thirds'</li> <li>use symbols to represent: 1/3, 2/3, 3/3</li> </ul>	
	2	Finding halves, thirds or quarters of shapes using partitioning	recognise that equal shares are not always the same shape	



### **Understanding Practice and Fluency (UPF)**

MA2-7NA represents, models and compares commonly used fractions and decimals					
	Quest: (1) Common fractions & decimals				
		Learning Journeys U	sing fractions: thirds and sixths		
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.D.1 Model and represent unit fractions, including 1/2, 1/4,1/3 and 1/5 and their multiples, to a complete whole	1	Introducing sixths	<ul> <li>find sixths of objects and shapes</li> <li>find sixths of sets</li> <li>estimate the size of a fractional part before using, eg paper folding to check or estimate the size of the whole from the part</li> <li>find the whole from a part</li> <li>use language 'one sixth', 'two sixths', 'three sixths'</li> <li>use symbols to represent: 1/6, 2/6, 3/6</li> <li>understand the relationship between thirds and sixths</li> </ul>		
	2	Finding thirds and sixths of objects, shapes and sets	<ul> <li>recognise equivalence</li> <li>find thirds and sixths of objects, shapes and lengths</li> <li>find thirds and sixths of sets (using models)</li> <li>find the whole from a part</li> <li>find thirds and sixths of uneven partitioned shapes</li> <li>use language 'one third', 'two thirds', 'three thirds'</li> <li>use fractional notation</li> </ul>		
		Learning Journe	eys Using fractions: fifths		
NA.D.1 Model and represent unit fractions, including 1/2, 1/4,1/3 and 1/5 and their multiples, to a complete whole	1	Introducing fifths	<ul> <li>estimate the size of a fractional part before using, eg paper folding to check or estimate the size of the whole from the part</li> <li>find fifths of objects, shapes and lengths</li> <li>find fifths of sets</li> <li>find the whole from a part</li> <li>use language 'one fifth', 'two fifths', 'three fifths' and so on</li> <li>use symbols to represent fractions 1/5, 2/5</li> </ul>		
		Learning Jour	neys Counting in thirds		
NA.D.2 Count by quarters, halves and thirds, including with mixed	1	Counting in thirds on a number line up to 1	<ul> <li>represent fractions on a number line (in simple cases, eg identify 2/3 on a number line that already shows divisions in thirds)</li> </ul>		
numerals; locate and represent these fractions on a number line	2	Counting in thirds on a number line up to 3	<ul> <li>count in proper and improper fractions on a number line</li> <li>identify whole number equivalence 3/3 = 1, 6/3 = 2</li> </ul>		
	Learning Journeys Using mixed numbers on a number line				
NA.D.2 Count by quarters, halves and thirds, including with mixed numerals; locate and represent these fractions on a number line	1	Counting and representing mixed numerals on a number line up to 3 (thirds)	<ul> <li>count in mixed numerals on a number line up to 3</li> <li>locate and represent mixed numerals on a number line, including on a partially-completed number line</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

MA2-7NA represents, models and compares commonly used fractions and decimals			
		Quest: (2) Comr	non fractions & decimals
		Learning Journe	eys Investigating fractions
Content Descriptor	Steps	Spine Nodes	Subnodes
NA.D.3 Investigate equivalent fractions used in contexts	1	Investigating simple equivalent fractions less than 1 using concrete materials and/or models (denominators 2, 3, 4, 5, 6, 8, 10)	<ul> <li>use models such as number lines, fraction strips, fraction walls to identify equivalent fractions</li> <li>use concrete materials or models to show equivalent fractions, eg folding a strip of paper</li> </ul>
	2	Investigating equivalent fractions up to and including 1 whole using area models (denominators 2, 4 and 8; 3 and 6; 5 and 10 and 100)	<ul> <li>model, compare and represent the equivalence of fractions with related denominators by redividing the whole, * using identical area models fraction walls and bar models</li> </ul>
		Learning Journ	eys Using decimal tenths
NA.D.4 Recognise that the place value system can be extended to tenths and hundredths, and make connections between fractions and decimal notation	1	Introducing decimal notation	<ul> <li>identify decimal fractions in everyday use</li> <li>understand that the decimal point is a mark that identifies the ones place, and indicates the change from whole numbers to parts of a whole read decimal fractions correctly, ie 'six point nine' understand that any numbers after the decimal point represent part of a whole</li> </ul>
	2	Introducing decimal tenths	<ul> <li>recognise that the place value system can be extended to tenths</li> <li>represent tenths using concrete materials and written representations</li> <li>recognise that tenths arise from dividing an object into 10 equal parts</li> <li>recognise that tenths arise from dividing a one-digit number or quantity by 10</li> <li>identify decimals on a number line</li> <li>represent decimals using models and place value equipment such as base ten and arrow cards, place value grid, hundred square</li> </ul>
	3	Comparing and ordering decimal tenths	<ul> <li>compare and order tenths using &gt;, &lt; and =</li> </ul>
	4	Counting in decimal tenths	<ul> <li>count forwards and backwards by tenths from any decimal number expressed to 1 decimal place, using concrete</li> <li>materials and number lines, eg use base ten materials to represent 3.7 and count forward: 3.8, 3.9, 4.0, 4.1,</li> </ul>



### **Understanding Practice and Fluency (UPF)**

MA2-7NA represents, models and compares commonly used fractions and decimals					
Quest: (2) Common fractions & decimals					
		Learning Journeys	Using decimal hundredths		
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Introducing decimal hundredths	<ul> <li>recognise that the place value system can be extended to tenths and hundredths</li> <li>recognise that hundredths arise when dividing an object by 100 and dividing tenths by 10</li> <li>state the place value of digits in decimal numbers of up to 2 decimal places</li> <li>read decimal fractions correctly, ie 'six point one nine' rather than 'six point nineteen'</li> </ul>		
NA.D.4 Recognise that the place value system can be	2	Counting in decimal hundredths	count forwards and backwards by hundredths from any decimal number expressed to 2 decimal place, using concrete materials and number lines		
extended to tenths and hundredths, and make connections between fractions and decimal notation	3	Modelling and representing decimal fractions up to 2 decimal places	<ul> <li>model decimal fractions using concrete materials</li> <li>represent decimal fractions, eg as fractions (tenths and hundredths), on number lines, using hundreds grids, in place value models and charts</li> </ul>		
	4	Comparing and ordering decimal hundredths	compare numbers with the same number of decimal places up to 2 decimal places		
		Comparing decimal fractions up to 2 decimal places	<ul> <li>compare numbers with a different number of decimal places up to 2 decimal places using &gt;, &lt; and =</li> </ul>		
	5	Connecting decimal fractions to common fractions involving hundredths	understand the relationship between decimal fractions and common fractions involving hundredths		
		Learning Journeys Par	rtitioning decimal hundredths		
NA.D.4 Recognise that the place value system can be extended to tenths and hundredths, and make connections between fractions and decimal notation	1	Partitioning decimal hundredths less than 1	<ul> <li>use place value to partition decimals of up to 2 decimal places, eg 5.37 = 5 + 3/10 + 7/100</li> <li>use place value charts and expanders to link decimal fractions to place value, eg base 10 blocks, hundreds grids</li> </ul>		
	2	Partitioning decimal hundredths more than 1	<ul> <li>partition decimals of up to 2 decimal places in non-standard forms, eg 5.37 = 5 + 37/100</li> <li>use place value charts and expanders to link decimal fractions to place value, eg base 10 blocks, hundreds grids</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

MA2-7I	NA repr	esents, models and cor	mpares commonly used fractions and decimals
		Quest: (2) Com	mon fractions & decimals
	Learnin	g Journeys Connecting	decimal fractions and common fractions
Content Descriptor	Steps	Spine Nodes	Subnodes
NA.D.4 Recognise that the place value system can be extended to tenths and hundredths, and make connections between fractions and decimal notation	1	Connecting decimal fractions to common fractions involving tenths	<ul> <li>understand the relationship between decimal fractions and common fractions involving tenths</li> <li>recognise and apply decimal notation to express whole numbers and tenths as decimals, eg 0.1 is the same as 1/10</li> <li>investigate equivalences using various methods, eg use a number line or a calculator to show that 1/2 is the same as 0.5 and 5/10</li> </ul>
	2	Connecting decimal fractions to common fractions involving tenths and hundredths  Connecting decimal	<ul> <li>understand the relationship between decimal fractions and common fractions involving tenths and hundredths</li> <li>recognise and apply decimal notation to express whole numbers, tenths and hundredths as decimals, eg 0.1 is the same as 1/10</li> <li>investigate equivalences using various methods, eg use a number line or a calculator to show that 1/2 is the same as 0.5 and 5/10</li> </ul>
	3	fractions to common fractions involving halves, fifths, tenths and hundredths Connecting decimal fractions to common fractions	<ul> <li>understand the relationship between decimal fractions and common fractions involving halves, fifths, tenths and hundredths</li> <li>understand the relationship between decimal fractions and common fractions</li> </ul>
MA2-8NA genera			en numbers, generates number patterns, and completes ces by calculating missing values
		Quest: (1) Pat	tterns & missing values
	Learni	ng Journeys Describing	s, continuing & creating number patterns
NA.E.1 Describe, continue and create number patterns resulting from performing addition or subtraction	1	Identifying and creating additive number patterns (3s, 4s, 6s, 7s, 8s, 9s, from any starting point within 100)	<ul> <li>identify additive number patterns, eg patterns that increase in 3s, 4s, 6s, 7s, 8s and 9s from any starting point</li> <li>describe the rule for a forwards (additive) number pattern, eg 'lt goes up by 3s'</li> <li>continue and create an additive number pattern</li> </ul>
	2	Identifying and creating subtractive number patterns (3s, 4s, 6s, 7s, 8s, 9s, from any starting point within 100)	<ul> <li>identify subtractive number patterns, eg patterns that decrease by 3s, 4s, 6s, 7s, 8s and 9s from any starting point</li> <li>describe the rule for a backwards (subtractive) number pattern, eg 'It goes down by 3s'</li> <li>continue and create a subtractive number pattern represented in numbers, on a number line or expressed in words, eg 'make a pattern that starts at 20 and shrinks by subtracting 2 each time'</li> </ul>



### **Understanding Practice and Fluency (UPF)**

MA2-8NA generalises properties of odd and even numbers, generates number patterns, and completes simple number sentences by calculating missing values						
Quest: (1) Patterns & missing values						
	Learning Journeys Describing, continuing & creating number patterns					
Content Descriptor	Steps	Spine Nodes	Subnodes			
NA.E.1 Describe, continue and create number patterns resulting from performing addition or subtraction	3	Identifying and creating additive and subtractive number patterns (3s, 4s, 6s, 7s, 8s, 9s, from any starting point within 100)	<ul> <li>identify additive or subtractive number patterns on a number line, hundreds chart or calendar, eg patterns that increase in 3s, 4s, 6s, 7s, 8s and 9s from any starting point</li> <li>describe the rule for a forwards (additive) or backwards (subtractive) number pattern, eg 'It goes up by 3s'</li> <li>continue and create an additive or subtractive number pattern represented in numbers, on a number line or expressed in words, eg 'make a pattern that starts at 0 and grows by adding 7 each time'</li> </ul>			
		Learning Journeys Ex	xploring odd and even numbers			
	1	Investigating odd and even numbers	<ul> <li>model odd and even numbers of up to 2 digits using arrays with 2 rows</li> <li>compare and describe the difference between models of even numbers and models of odd numbers recognise the connection between even numbers and the multiplication facts for 2</li> </ul>			
NA.E.2 Investigate the conditions required for a	2	Identifying odd and even numbers	<ul> <li>recognise the significance of the final digit of a whole number in determining whether a given number is even or odd</li> <li>identify even or odd numbers of up to 4 digits</li> </ul>			
number to be even or odd and identify even and odd numbers	3	Identifying odd and even number patterns (add in number lines and number charts)	<ul> <li>model even and odd numbers of up to 20 using arrays with 2 rows</li> <li>compare and describe the difference between the models of odd and even numbers</li> <li>recognise the connection between even numbers, doubles and the 2 times-tables; demonstrate the connection with words, models or numerals</li> <li>use the final digit of a whole number to determine whether a given number is even or odd (up to four digits)</li> </ul>			
		Quest: (2) Pat	tterns & missing values			
	Learnin	g Journeys Using numb	per sentences to find unknown quantities			
NA.E.3 Use equivalent number sentences involving addition and subtraction to find unknown quantities	1	Using inverse operations to complete addition and/or subtraction number sentences (2-digit numbers)	<ul> <li>complete number sentences involving addition and subtraction by calculating missing numbers, eg find the missing numbers:         □ + 55 = 83, □ - 15 = 19</li> <li>use inverse operations to complete number sentences</li> <li>justify solutions when completing number sentences</li> </ul>			
	2	Finding missing numbers where there are addition and/or subtraction operations on both sides of the equals sign	<ul> <li>find the missing number in a number sentence involving operations of addition or subtraction on both sides of the equals sign, eg 8+□=6+7</li> </ul>			



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-8NA generalises properties of odd and even numbers, generates number patterns, and completes simple number sentences by calculating missing values

simple number sentences by calculating missing values					
Quest: (2) Patterns & missing values					
	Learning Journeys Odd and even numbers				
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.E.4 Investigate and use the properties of even and odd numbers	1	Using the properties of odd and even numbers	<ul> <li>investigate and generalise the result of adding, subtracting and multiplying pairs of even numbers, pairs of odd numbers, or one even and one odd number, eg even + odd = odd, odd × odd = odd</li> <li>explain why the result of a calculation is even or odd with reference to the properties of the numbers used in the calculation</li> <li>predict whether the answer to a calculation will be even or odd by using the properties of the numbers in the calculation</li> <li>investigate the place value of digits within odd and even numbers</li> </ul>		
		Learning Journeys In	nvestigating multiple sequences		
NA.E.5 Investigate number sequences involving multiples of 3, 4, 6, 7, 8 and 9	1	Investigating number sequences involving multiples of 3, 4, 6, 7, 8 and 9	<ul> <li>generate number patterns using multiples of 3, 4, 6, 7, 8 and 9</li> <li>investigate visual number patterns on a number chart</li> <li>find missing terms in a number sequence</li> </ul>		
		Learning Journeys	s Exploring number patterns		
NA.E.6 Explore and describe number patterns resulting from performing multiplication	1	Exploring number patterns resulting from performing multiplication	<ul> <li>find a higher term in a number pattern resulting from performing multiplication, given the first few terms, eg determine the next term in the pattern 4, 8, 16, 32, 64,</li> <li>describe how the next term in a number pattern is calculated, eg 'Each term in the pattern is double the previous term'</li> <li>find missing terms in a number sequence</li> </ul>		
	L	earning Journeys Expr	essing equations as word problems		
NA.E.7 Solve word problems by using number sentences involving multiplication or	1	Expressing given one- step word problems as a multiplication or division number sentences and solving	<ul> <li>represent and solve multiplication and division word problems (up to 10 x 10 multiplication ad division facts) using number sentences with a symbol for the unknown, eg 'Anne spent \$28 dollars on tickets to a show for her friends. If 7 friends are coming to the show, what was the cost of each ticket?'</li> <li>discuss whether it is more appropriate to represent the problem using x or ÷ in order to calculate the solution</li> </ul>		
division where there is no remainder	2	Expressing given one- step equations as word problems	<ul> <li>express given addition or subtraction equations as word problems (up to 2 digit with 2-digit addition or subtraction)</li> <li>express given multiplication or division equations as word problems (using multiplication facts up to 10 x 10)</li> </ul>		



#### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA2-8NA generalises properties of odd and even numbers, generates number patterns, and completes simple number sentences by calculating missing values

#### Quest: (2) Patterns & missing values Learning Journeys Solving word problems involving mult and div Content **Spine Nodes Steps Subnodes** Descriptor Solving two-step multiplication and/ or division word • solve two-step word problems in context involving multiplication problems, including and division; choose the appropriate operation correspondence problems NA.E.7 Solve word problems Solving multi-step solve multi-step word problems involving multiplication and by using number 2 multiplication and/or sentences involving division represent unknown with a letter division word problems multiplication or division where there is no remainder • select and use a variety of mental and informal written strategies to solve division problems Selecting efficient • apply the inverse relationship of multiplication and division to 3 strategies to solve justify answers division problems check the answer to a word problem using digital technologies record mental strategies accurately



#### **Understanding Practice and Fluency (UPF)**

Introducing formal

units for length:

millimetres

5

#### Measurement and Geometry

MA2-9MG measures, records, compares and estimates lengths, distances and perimeters in metres,

#### centimetres and millimetres, and measures, compares and records temperatures Quest: (1) Measuring length and temperature Learning Journeys Comparing, ordering and measuring length Content **Spine Nodes** Subnodes Descriptor Comparing lengths 1 in metres and compare lengths and distances using metres and centimetres centimetres Ordering lengths 2 in metres and order lengths and distan ces using metres and centimetres centimetres estimate lengths and check by measuring; explain strategies used to estimate lengths and distances, such as by \* referring to a known length, eg 'My handspan is 10 cm and my desk is 8 handspans long, Estimating and so my desk is about 80 cm long' 3 measuring to the • measure lengths and distances to the nearest centimetre using a nearest centimetre centimetre ruler • record lengths and distances using the abbreviation for centimetres MG.A.1 Measure, order and compare estimate and measure lengths and distances using metres and objects using centimetres familiar metric units Measuring in • explain strategies used to estimate lengths and distances, such as by of length referring to a known length, eg 'My handspan is 10 cm and my desk 4 metres and is 8 handspans long, so my desk is about 80 cm long' centimetres record lengths and distances using abbreviations for metres and centimetres, eg 1 m 25 cm

measure length

mm or 53 mm

nearest millimetre using a ruler

· compare lengths with the same standard unit

• recognise the need for a formal unit smaller than the centimetre to

 develop a personal reference for the approximate length of 1 mm • recognise and model that there are 10 mm in 1 cm, ie 10 mm = 1 cm

• estimate and use the millimetre as a unit to measure lengths to the

• record lengths using the abbreviation for millimetres (mm), eg 5 cm 3



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA2-9MG measures, records, compares and estimates lengths, distances and perimeters in metres, centimetres and millimetres, and measures, compares and records temperatures

centimetres and millimetres, and measures, compares and records temperatures					
Quest: (2) Measuring length and temperature					
Learning Journeys Using metric units to measure length					
Content Descriptor	Steps	Spine Nodes	Subnodes		
MG.A.2 Use scaled instruments to measure and compare lengths	1	Using scaled instruments to measure length	<ul> <li>select and use an appropriate device to measure lengths and check accuracy of estimations</li> <li>explain why 2 students may obtain different measures for the same length</li> </ul>		
	2	Selecting appropriate units of measurement: metres, centimetres, millimetres	<ul> <li>explore the appropriateness of units when measuring length</li> <li>select and justify the most appropriate metric unit to measure given lengths and distances</li> </ul>		
	3	Converting between metres and centimetres (whole numbers only)	<ul> <li>describe 1 m as 100 cm</li> <li>convert between metres and centimetres using whole numbers, eg 3 m is the same as 300 cm</li> <li>record measurement equivalents in a table</li> <li>explain the relationship between the size of a unit and the number of units needed</li> </ul>		
	4	Converting between centimetres and millimetres (whole numbers only)	<ul> <li>describe 1 m as 100 cm</li> <li>convert between metres and centimetres using whole numbers, eg 3 m is the same as 300 cm</li> <li>record measurement equivalents in a table</li> <li>explain the relationship between the size of a unit and the number of units needed</li> </ul>		
		Learning Jo	urneys Length and 3D objects		
MG.A.2 Use scaled instruments to measure and compare lengths	1	Applying length to attributes of three-dimensional objects	<ul> <li>recognise the features of a three-dimensional object associated with length that can be measured</li> <li>describe the length, height and width of a three-dimensional object</li> </ul>		
		Learning Jo	urneys Introducing perimeter		
MG.A.2 Use scaled instruments to measure and compare lengths	1	Introducing perimeter	<ul> <li>use the term 'perimeter' to describe the total distance around a two-dimensional shape</li> <li>estimate and measure the perimeters of two-dimensional shapes</li> <li>describe when a perimeter measurement might be used in everyday situations</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA2-9MG measures, records, compares and estimates lengths, distances and perimeters in metres, centimetres and millimetres, and measures, compares and records temperatures

centimetres and millimetres, and measures, compares and records temperatures				
Quest: (2) Measuring length and temperature				
Learning Journeys Reading temperature				
Content Descriptor	Steps	Spine Nodes	Subnodes	
MG.A.3 Use scaled instruments to measure and compare temperatures	1	Using the language of temperature	<ul> <li>identify benchmarks for freezing, cold, cool, warm, hot and boiling temperatures (water)</li> <li>identify benchmarks for cold, cool, warm and hot temperatures (air)</li> </ul>	
	2	Introducing thermometers	<ul> <li>estimate temperature using personal reference</li> <li>use a standard thermometer to determine whether temperature is rising or falling</li> <li>relate thermometers to the number line</li> <li>introduce the unit of degrees to record temperatures</li> <li>recognise and read temperatures in everyday situations, eg weather report, cooking</li> </ul>	
	3	Measuring temperature	<ul> <li>recognise the need for formal units to measure temperature</li> <li>use a thermometer to measure and compare temperatures to the nearest degree Celsius</li> <li>record temperatures to the nearest degree Celsius using the symbol for degrees (°)</li> <li>use a digital or analogue thermometer to take and record daily temperature readings</li> </ul>	
MA2-10MG measu	res. reco	ords, compares and	d estimates areas using square centimetres and square metres	
			1) Area: square cm and m	
			neys Using formal units for area	
MG.B.1 Recognise and use formal units to measure and estimate the areas of rectangles	1	Introducing formal units for area: the square centimetre	<ul> <li>establish the need for a formal unit to measure area and introduce square centimetres</li> <li>develop a sense of the area of 1 square centimetre and identify surfaces that have area 'about 1 square centimetre', 'less than 1 square centimetre' and 'greater than 1 square centimetre'</li> <li>identify everyday situations where square centimetres are an appropriate unit for measuring area</li> <li>introduce the abbreviation cm^2 for recording area in square centimetres</li> </ul>	
	2	Introducing formal units for area: the square metre	<ul> <li>recognise the need for a larger formal unit to measure area and introduce square metres</li> <li>develop a sense of the area of 1 square metre and identify surfaces that have area 'about 1 square metre', 'less than 1 square metre' and 'greater than 1 square metre'</li> <li>identify everyday situations where square metres are an appropriate unit for measuring the area, eg floor of a room</li> <li>recognise that a square metre need not be square in shape, eg cut a piece of cardboard that is 1 metre by 1 metre in half and join the shorter ends to make an area that is 2 metres by half a metre</li> <li>introduce the abbreviation m^2 for measuring area in square metres</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA2-10MG measures, records, compares and estimates areas using square centimetres and square metres				
Quest: (1) Area: square cm and m				
		Learning Journey	vs Using formal units for area	
Content Descriptor	Steps	Spine Nodes	Subnodes	
MG.B.1 Recognise and use formal units to measure and estimate the areas of rectangles	3	Estimating and measuring areas of rectangles using efficient strategies and counting in square centimetres or metres	<ul> <li>measure the area of rectangles (including squares) using square centimetres and/or square metres (both tiling and using grid overlay) using whole number side lengths only</li> <li>estimate areas of rectangles (including squares) in square centimetres and/or square metres and then check by measuring</li> <li>develop efficient strategies for counting square centimetres/ metres when measuring areas of rectangles</li> <li>draw possible rectangles on a grid to represent a given whole number rectangular area</li> </ul>	
		Quest: (2) A	Area: square cm and m	
	Lear	<b>ning Journeys</b> Solving	word problems involving mult and div	
MG.B.2 Compare the areas of regular and irregular shapes by informal means	1	Measuring areas of rectilinear figures by decomposing into rectangles and counting units	<ul> <li>recognise area as additive</li> <li>decompose rectilinear figures into rectangles to find their area by tiling or using a grid overlay</li> </ul>	
	2	Estimating and comparing areas of non-rectilinear shapes using a square grid	<ul> <li>use a square grid to approximate and compare the areas of non-rectilinear shapes</li> <li>compare how different placements of the grid make approximation easier or more difficult</li> <li>find and explain the area of irregular shapes by counting squares or part squares</li> </ul>	
	3	Approximating and comparing areas of non-rectilinear shapes using a square centimetre grid	<ul> <li>use a square-centimetre grid to approximate and compare the areas of non-rectilinear shapes</li> <li>compare how different placements of the grid make approximation easier or more difficult</li> <li>find and explain the area of irregular shapes by counting squares or part squares</li> </ul>	
	Learning Journeys Comparing objects using familiar metric units			
MG.B.3 Compare objects using familiar metric units of area	1	Comparing and ordering rectangular areas using counting of standard metric units	<ul> <li>compare two areas by measuring using standard metric units</li> <li>order three or more areas by measuring using standard metric units</li> <li>choose the most appropriate unit cm<sup>2</sup> or m<sup>2</sup> and justify selection</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA2-11MG measures, records, compares and estimates volumes and capacities using litres, millilitres and cubic centimetres

cubic centimetres					
Quest: (1) Volume/capacity: L, mL, cubic cm					
	Learning Journeys Measure, order and compare units of volume				
Content Descriptor	Steps	Spine Nodes	Subnodes		
MG.C.1 Measure, order and compare objects using familiar metric units of capacity	1	Introducing formal units for volume and capacity: litres	<ul> <li>recognise and explain the need for formal units to measure volume and capacity</li> <li>develop a personal reference for one litre and fractions of 1 litre (quarters and halves); relate the litre to familiar everyday containers, eg milk cartons</li> <li>recognise that one-litre containers can be a variety of shapes</li> <li>record volumes and capacities using the abbreviation for litres (L)</li> </ul>		
	2	Estimating, comparing and measuring in litres	<ul> <li>estimate and measure capacities to the nearest litre</li> <li>compare and order 2 or more containers by capacity measured in litres, including the capacity of commercially packaged objects whose capacity is stated in litres</li> <li>record volumes and capacities using the abbreviation for litres (L)</li> </ul>		
		Learning Jou	rneys Measuring volume		
MG.C.1 Measure, order and compare objects using familiar metric units of capacity	1	Using unit cubes to measure volume	measure volumes by counting unit cubes, using cubic centimetres, cubic inches, cubic feet and improvised units		
	2	Estimating and measuring volume using cubic centimetre blocks	<ul> <li>use the cubic centimetre as a unit to measure volumes by packing small containers with cubic-centimetre blocks and describing in terms of layers, eg '2 layers of 10 cubic-centimetre blocks'</li> <li>construct three-dimensional objects using cubic-centimetre blocks and count the blocks to determine the volumes of the objects; devise and explain strategies for counting blocks</li> <li>compare the volumes of 2 or more objects made from cubic-centimetre blocks by counting blocks record volumes using the abbreviation for cubic centimetres (cm^3)</li> </ul>		
	3	Using cubic centimetres to measure volume	<ul> <li>measure the volumes of rectangular containers by packing them with cubic-centimetre blocks</li> <li>explain the advantages and disadvantages of using cubic-centimetre blocks as a unit to measure volume</li> <li>describe arrangements of cubic-centimetre blocks in containers in terms of layers</li> <li>connect the layers of blocks with multiplying the dimensions</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA2-11MG measures, records, compares and estimates volumes and capacities using litres, millilitres and

MAZ-IIMG measures, records, compares and estimates volumes and capacities using litres, millilitres and cubic centimetres					
	Quest: (2) Volume/capacity: L, mL, cubic cm				
		Learning Journey	s Measuring capacity in millilitres		
Content Descriptor	Steps	Spine Nodes	Subnodes		
MG.C.3 Use scaled instruments to measure and compare capacities 3	1	Introducing standard measurements in millilitres	<ul> <li>know that a standard cup is 250 ml and a standard teaspoon is 5 ml</li> <li>recognise standard measurements in everyday contexts such as cooking</li> </ul>		
	2	Introducing formal units for volume and capacity: millilitres	<ul> <li>recognise the need for a formal unit smaller than the litre to measure volume and capacity</li> <li>recognise that there are 1000 millilitres in 1 litre, ie 1000 millilitres = 1 litre</li> <li>relate the millilitre to familiar everyday containers and familiar informal units, eg 250 mL fruit juice containers, 1 teaspoon is approximately 5 mL</li> </ul>		
	3	Reading scales with 100 millilitre markings	<ul> <li>read a scale where every 100 ml is marked and labelled</li> <li>read a scale where every 100 ml is marked and half and I litre are labelled</li> <li>read a scale where every 100 ml is marked and every other 100 ml is labelled</li> </ul>		
	4	Measuring with millilitres to the nearest 100 ml	<ul> <li>use the millilitre as a unit to measure volume and capacity, using a device calibrated in millilitres (read to the nearest 100ml with every 100ml or every other 100ml marked)</li> <li>record volumes and capacities using the abbreviation for millilitres (mL)</li> <li>estimate the capacity of a container in millilitres and check by measuring (measure to the nearest 100ml with every 100ml or every other 100ml marked)</li> <li>compare and order the capacities of 2 or more containers measured in millilitres</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA2-12MG measures, records, compares and estimates the masses of objects using kilograms and grams				
Quest: (1) Mass: kg and g				
Learning Journeys Using the kilogram to measure mass				
Content Descriptor	Steps	Spine Nodes	Subnodes	
MG.D.1 Measure, order and compare objects using familiar metric units of mass	1	Introducing formal units for mass: the kilogram	<ul> <li>establish the need for formal units to measure mass and introduce the kilogram</li> <li>develop a sense of the mass of 1 kilogram and identify objects that have mass 'about 1 kilogram', 'less than 1 kilogram', 'greater than 1 kilogram', eg a litre of milk is about 1 kilogram, a standard pack of flour is 1 kilogram</li> <li>identify everyday situations where kilograms are an appropriate unit for measuring the mass</li> <li>introduce the abbreviation 'kg' for recording mass in kilograms</li> </ul>	
	2	Measuring mass in kilograms	<ul> <li>compare and order 2 or more objects by mass measured to the nearest kilogram using carried scales</li> <li>estimate the number of objects that have a total mass of 1 kilogram and check by measuring</li> <li>estimate mass using a personal reference for a kilogram</li> <li>record mass using the abbreviation 'kg'</li> <li>compare masses using uniform informal units and the symbols &gt;, =, &lt;</li> <li>compare masses using simple scaling by integers, eg 'five times as heavy'</li> </ul>	
		Q	uest: (2) Mass: kg and g	
		Learning Journe	eys Measuring in grams and kilograms	
MG.D.2 Use scaled instruments to measure and compare masses	1	Investigating mass in packaging	<ul> <li>interpret information about mass on commercial packaging</li> <li>estimate the mass of a substance in a partially-filled container/packet from the information on the label</li> </ul>	
	2	Introducing formal units for mass: the gram	<ul> <li>establish the need for a smaller unit of mass and introduce the gram, including that 1000 grams = 1 kilogram</li> <li>develop a sense of the mass of standard everyday objects in grams, eg an egg is about 50 grams</li> <li>identify everyday situations where grams are an appropriate unit for measuring the mass</li> <li>introduce the abbreviation 'g' for recording mass in grams and record masses</li> <li>calculate the number of grams in a whole number of kilograms</li> <li>interpret simple fractions (¼, ½, ¾) of a kilogram and relate these to the number of grams</li> </ul>	
	3	Measuring in grams	<ul> <li>estimate mass using personal references for grams and 'guess and check'</li> <li>measure mass in grams by using and interpreting varied scales and images of scales</li> <li>record mass in grams using the appropriate abbreviation (g)</li> </ul>	
	4	Measuring in grams and kilograms	<ul> <li>estimate mass using personal references for grams and kilograms</li> <li>choose appropriate standard units to estimate and measure (g/kg)</li> <li>measure mass in grams and kilograms by using and interpreting varied scales</li> <li>record mass in grams, kilograms and mixed units using the appropriate abbreviations (g), (kg), eg 5 kg and 500 g</li> </ul>	



## **Understanding Practice and Fluency (UPF)**

MA2-13MG rea	ds and	records time in on	ne-minute intervals and converts between hours, minutes and seconds
		Quest: (1)	Time: minutes, hours, seconds
		Learning Jour	rneys Telling the time to the minute
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.E.1 Tell time to the minute and investigate the relationship between units of time	1	Telling time to the minute (analogue)	<ul> <li>read time on analogue clocks to the minute using the terms 'o'clock', 'past' and 'to', including 'half-past', 'quarter past' and 'quarter to'</li> <li>observe and describe the position or draw of the hands of an analogue clock when reading time to the minute, including the hour hand, minute hand and second hand</li> <li>position or draw the hands on an analogue clock to show time to the minute where the time is given using the terms 'o'clock', 'past' and 'to', including 'half-past', 'quarter past' and 'quarter to'</li> </ul>
	2	Telling time to the minute (digital)	<ul> <li>read time on 12-hour digital clocks to the minute using the terms 'o'clock', 'past' and 'to', including 'half-past', 'quarter past' and 'quarter to' and write in words</li> <li>record times on analogue clocks to the minute in 12-hour digital format</li> <li>position or draw the hands on an analogue clock to show time to the minute where the time is given in 12-hour digital format</li> <li>connect 12-hour digital displays for times the minute to their corresponding display on an analogue clock</li> </ul>
		Quest: (2)	Time: minutes, hours, seconds
	Le	earning Journeys	Converting time and solving time problems
MG.E.2 Convert between units of time	1	Converting between units of time (multiplicative conversions only)	<ul> <li>calculate the number of seconds in a whole number of minutes</li> <li>calculate the number of minutes in a whole number of hours</li> <li>calculate the number of days in a whole number of weeks</li> <li>calculate the number of months in a whole number of years</li> <li>solve problems involving conversion between units of time</li> </ul>
		Learnir	ng Journeys Using AM and PM
MG.E.3 Use am and pm notation and solve simple time problems	1	Using am and pm notation	<ul> <li>know that there are 24 hours in a day</li> <li>recognise that midday/noon divides the day into two equal parts of 12 hours each</li> <li>establish the need to distinguish between times in the first 12 hours of the day and the second 12 hours of the day, and introduce am and pm notation</li> <li>know and record midday/noon as 12 pm and 12:00 pm, and midnight as 12 am and 12:00 am</li> <li>use am and pm notation to record times in relation to midday/noon and midnight</li> <li>read times written using am and pm notation using 'past', 'to', morning, afternoon, evening and night appropriately', eg 3:40 pm is 'twenty to four in the afternoon'</li> </ul>
	2	Solving problems relating to elapsed time involving the four operations (to five minutes)	use the 4 operations to solve word problems involving intervals of time including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA2-13MG reads and records time in one-minute intervals and converts between hours, minutes and
seconds

seconds				
Quest: (2) Time: minutes, hours, seconds				
Learning Journeys Read and interpret timetables				
Content Descriptor	Steps	Spine Nodes	Subnodes	
MG.E.4 Read and interpret simple timetables, timelines and calendars	1	Using timetables (12-hour time)	<ul> <li>use real-world timetables (12-hour time only) to determine arrival time given the desired departure time, * including when the exact departure time is not listed exactly in the timetable, ie needing to use an earlier departure time</li> <li>use real-world timetables (12-hour time only) to determine departure time given the desired arrival time, including when the arrival time is not listed exactly in the timetable</li> <li>create timetables using given information</li> </ul>	
	2	Introducing timelines	• interpret the sequence of events on a timeline (understanding of scale not expected)	
		Learr	ning Journeys Writing dates	
MG.E.4 Read and interpret simple timetables, timelines and calendars	1	Writing dates	identify a day/date on a calendar and write the date using the appropriate notation eg 11/5/17	
MA2-14MG make			d names three-dimensional objects, including prisms, pyramids, nd spheres, and describes their features	
			t: (1) Features of 3D objects	
			urneys Exploring prisms and nets	
	1	Introducing rectangular prisms	<ul> <li>manipulate and describe the attributes of rectangular prisms</li> <li>recognise that a cube is a special kind of rectangular prism</li> <li>recognise rectangular prisms in the environment and drawings</li> </ul>	
	2	Exploring prisms	<ul> <li>manipulate and describe the attributes of prisms</li> <li>recognise that a cube is a special kind of prism</li> <li>recognise prisms in the environment and drawings</li> </ul>	
MG.F.1 Make		Comparing, sorting and naming prisms and pyramids	<ul> <li>compare and sort prisms and pyramids by their geometric properties, eg number of edges, number of vertices</li> <li>describe and name prisms and pyramids by the shape of their base</li> </ul>	
models of three- dimensional objects and describe key features	3	Comparing three- dimensional objects including pyramids, prisms, cones, spheres and cylinders	<ul> <li>describe similarities and differences between prisms (including cubes), pyramids, cylinders, cones and spheres, eg surfaces, faces, edges and vertices</li> <li>recognise and describe the use of three-dimensional objects in a variety of contexts, eg buildings, packaging</li> <li>identify and name three-dimensional objects as prisms (including cubes), pyramids, cylinders, cones and spheres</li> </ul>	
	4	Making basic models of three- dimensional objects	<ul> <li>use a variety of materials to make models of prisms (including cubes), pyramids, cylinders, cones and spheres, given a three-dimensional object, picture or photograph to view</li> <li>identify and describe the two-dimensional shapes that can be found in a three-dimensional object, eg build a structure using concrete materials and describe it using geometric terms so that a partner will be able to build it</li> </ul>	

build it



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA2-14MG makes, compares, sketches and names three-dimensional objects, including prisms, pyramids, cylinders, cones and spheres, and describes their features

cylinders, cones and spheres, and describes their features					
Quest: (1) Features of 3D objects					
Learning Journeys Rectangular prism nets					
Content Descriptor	Steps	Spine Nodes	Subnodes		
MG.F.1 Make models of three-	1	Introducing nets of rectangular prisms	<ul> <li>deconstruct everyday packages that are prisms (including cubes) to create nets, eg cut up tissue boxes</li> <li>make connections between nets and the two-dimensional shapes of the faces</li> <li>recognise that a net requires each face to be connected to at least 1 other face</li> <li>investigate, make and identify the variety of nets that can be used to create a particular prism, such as the variety of nets that can be used to make a cube</li> </ul>		
dimensional objects and describe key features	2	Introducing nets of prisms	<ul> <li>deconstruct everyday packages that are prisms (including cubes) to create nets, eg cut up tissue boxes</li> <li>make connections between nets and the two-dimensional shapes of the faces</li> <li>recognise that a net requires each face to be connected to at least 1 other face</li> <li>investigate, make and identify the variety of nets that can be used to create a particular prism, such as the variety of nets that can be used to make a cube</li> <li>compare two-dimensional shapes to parts of three-dimensional objects in the environment</li> </ul>		
		Ques	t: (2) Features of 3D objects		
		Learnin	g Journeys Identifying prisms		
MG.F.2 Investigate and represent three-dimensional objects using drawings	1	Identifying prisms in the environment	<ul> <li>identify prisms (including cubes) in the environment and from drawings, photographs and descriptions</li> <li>investigate types of prisms used in commercial packaging and give reasons for some being more commonly used</li> </ul>		
	2	Drawing prisms	<ul> <li>sketch prisms (including cubes), attempting to show depth</li> <li>compare their own drawings of prisms (including cubes), with other drawings and photographs</li> <li>draw prisms (including cubes), using a computer drawing tool, attempting to show depth</li> <li>draw different views of an object constructed from connecting cubes on isometric grid paper</li> </ul>		
	3	Representing prisms with models	interpret given isometric drawings to make models of three-dimensional objects using connecting cubes		
	4	Introducing nets of prisms	draw and describe nets for rectangular and triangular prisms		



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA2-14MG makes, compares, sketches and names three-dimensional objects, including prisms, pyramids, cylinders, cones and spheres, and describes their features

cylinders, cones and spheres, and describes their features				
		Ques	t: (2) Features of 3D objects	
Learning Journeys Identifying pyramids				
Content Descriptor	Steps	Spine Nodes	Subnodes	
MG.F.2 Investigate and represent	1	Identifying pyramids in the environment	<ul> <li>identify pyramids in the environment and from drawings, photographs and descriptions</li> <li>investigate types of pyramids used in commercial packaging and give reasons for some being more commonly used</li> </ul>	
three-dimensional objects using drawings	2	Drawing pyramids	<ul> <li>sketch pyramids, attempting to show depth</li> <li>compare their own drawings of pyramids, with other drawings and photographs</li> <li>draw pyramids, using a computer drawing tool, attempting to show depth</li> </ul>	
		Learning	Journeys Prisms and pyramids	
MG.F.2 Investigate and represent three-dimensional objects using drawings	1	Constructing prisms and pyramids from given nets	construct prisms and pyramids from given nets	
		Learning	Journeys Identifying cylinders	
MG.F.2 Investigate and represent three-dimensional objects using drawings	1	Identifying cylinders in the environment	<ul> <li>identify cylinders in the environment and from drawings, photographs and descriptions</li> <li>investigate types of cylinders used in commercial packaging and give reasons for some being more commonly used</li> </ul>	
	2	Drawing cylinders	<ul> <li>sketch cylinders, attempting to show depth</li> <li>compare their own drawings of cylinders, with other drawings and photographs</li> <li>draw cylinders, using a computer drawing tool, attempting to show depth</li> </ul>	
		Learnir	ng Journeys Identifying cones	
MG.F.2 Investigate and represent three-dimensional	1	Identifying cones in the environment	<ul> <li>identify cones in the environment and from drawings, photographs and descriptions</li> <li>investigate types of cones used in commercial packaging and give reasons for some being more commonly used</li> </ul>	
objects using drawings	2	Drawing cones	<ul> <li>sketch cones, attempting to show depth</li> <li>compare their own drawings of cones, with other drawings and photographs</li> <li>draw cones, using a computer drawing tool, attempting to show depth</li> </ul>	
	Learning Journeys Identifying spheres			
MG.F.2 Investigate and represent three-dimensional objects using drawings	1	Identifying spheres in the environment	<ul> <li>identify spheres in the environment and from drawings, photographs and descriptions</li> <li>investigate types of spheres used in commercial packaging and give reasons for some being more commonly used</li> </ul>	
	2	Drawing spheres	<ul> <li>sketch spheres, attempting to show depth</li> <li>compare their own drawings of spheres, with other drawings and photographs</li> <li>draw spheres, using a computer drawing tool, attempting to show depth</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA2-15MG manipulates, identifies and sketches two-dimensional shapes, including special quadrilaterals,

THE TOTAL THAT	parates,		d describes their features
		Ques	t: (1) Features of 2D shapes
	Learn	ing Journeys Com	paring and identifying two-dimensional shapes
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.G.1 Compare and describe features of two- dimensional shapes, including the special quadrilaterals	1	Comparing and describing two-dimensional shapes, including special quadrilaterals	<ul> <li>identify and name a shape given a description of its features</li> <li>sort two-dimensional shapes using given attributes, eg number of sides, number of parallel sides</li> <li>compare similarities and differences between two-dimensional shapes, including the special quadrilaterals</li> </ul>
	2	Identifying regular and irregular two-dimensional shapes	<ul> <li>identify a regular shape from a group of irregular shapes, eg a regular pentagon in a group of irregular pentagons</li> <li>explain the difference between regular and irregular two-dimensional shapes</li> <li>identify and name two-dimensional shapes presented as either regular or irregular shapes in different orientations</li> </ul>
	3	Drawing and constructing regular and irregular two-dimensional shapes	<ul> <li>draw regular and irregular two-dimensional shapes in different orientations</li> <li>construct regular and irregular two-dimensional shapes from a variety of materials, eg cardboard, straws, pattern blocks</li> <li>recognise that a triangle cannot be constructed from 3 lengths of a material if the sum of the lengths of the 2 shorter sides is less than the length of the longest side</li> <li>solve problems requiring the greatest or least number of two-dimensional shapes needed to compose a larger shape in a variety of ways</li> </ul>
	Lea	rning Journeys Co	mparing features of two-dimensional shapes
MG.G.1 Compare and describe features of two- dimensional shapes, including the special quadrilaterals	1	Comparing the strengths of two-dimensional constructions	<ul> <li>construct 3-sided and 4-sided frames using various materials; compare the rigidity of the frames</li> <li>explore the use of a brace in a 4-sided frame; explain how the brace makes the frame more rigid</li> </ul>
	2	Classifying plane shapes by their spatial features	classify plane shapes by the nature and number of sides, angles and symmetry; including parallel/perpendicular sides, right, obtuse, acute angles
	3	Sorting plane shapes by their spatial features	<ul> <li>sort a group of plane shapes by their spatial features</li> <li>identify how a group of plane shapes has been sorted/classified</li> </ul>



## **Understanding Practice and Fluency (UPF)**

MA2-15MG manipulates, identifies and sketches two-dimensional shapes, including special quadrilaterals, and describes their features				
Quest: (1) Features of 2D shapes				
		Learning Jour	neys Recognising lines of symmetry	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Recognising line symmetry in the environment	<ul> <li>observe and describe symmetry informally in everyday objects, pictures, designs and shapes</li> <li>identify shapes that are symmetrical and are not symmetrical by folding to test for symmetry</li> <li>sort objects, pictures, designs and/or shapes according to whether they are symmetrical or not</li> <li>draw a single line of symmetry on given pictures, designs and shapes</li> </ul>	
MG.G.2 Identify symmetry in the environment 2	2	Recognising line symmetry of shapes	<ul> <li>define the line of symmetry of a two-dimensional shape as a line across which the shape can be folded into 2 matching parts</li> <li>identify a line of symmetry in two-dimensional shapes</li> <li>sort two-dimensional shapes according to whether they are symmetrical or not</li> </ul>	
	3	Drawing lines of symmetry on given designs and shapes	<ul> <li>recognise that some designs and shapes may have more than 1 line of symmetry</li> <li>identify and draw all lines of symmetry on designs and shapes</li> <li>determine the total number of lines of symmetry on designs and shapes</li> <li>determine whether or not a given line through designs and shapes is a line of symmetry</li> </ul>	
		Ques	t: (2) Features of 2D shapes	
	ı	Learning Journeys	Composing and decomposing 2D shapes	
MG.G.3 Compare and describe two-dimensional shapes that result from combining and splitting common shapes, with and without the use of digital technologies	1	Composing and decomposing two-dimensional shapes	<ul> <li>create two-dimensional shapes by combining and splitting common shapes</li> <li>follow instructions to create a common shape using a specified set of 2 or more common shapes</li> <li>describe and/or name the shape formed by combining and splitting common shapes</li> <li>compare the area of combined and split shapes and their components</li> <li>investigate the range of combinations that can be used to combine or split common shapes</li> </ul>	
		Learning Jou	rneys Introducing transformations	
MG.G.4 Create symmetrical patterns, pictures and shapes, with and without the use of digital technologies	1	Introducing transformations: Slides (translations)	<ul> <li>describe the process of performing a 'slide' and the similarities and differences between the original shape and the shape after it has undergone a 'slide'</li> <li>identify and describe a one-step slide of a shape using the term 'slide'</li> <li>perform a one-step slide of a shape using physical materials and record the result without the use of digital technology</li> <li>perform a one-step slide of a shape and record the result using digital technology</li> <li>predict and draw the result of a one-step slide on a given shape</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA2-15MG manipulates, identifies and sketches two-dimensional shapes, including special quadrilaterals,

mAz-15MG manipulates, identifies and sketches two-dimensional snapes, including special quadrilaterals, and describes their features					
Quest: (2) Features of 2D shapes					
Learning Journeys Introducing transformations					
Content Descriptor	Steps	Spine Nodes	Subnodes		
	2	Introducing transformations: Flips (reflections)	<ul> <li>describe the process of performing a 'flip' and the similarities and differences between the original shape and the shape after it has undergone a 'flip'</li> <li>identify and describe a one-step flip of a shape using the term 'flip'</li> <li>perform a one-step flip of a shape using physical materials and record the result without the use of digital technology</li> <li>perform a one-step flip of a shape and record the result using digital technology</li> <li>predict and draw the result of a one-step flip on a given shape</li> </ul>		
MG.G.4 Create symmetrical patterns, pictures and shapes, with and without the use of digital technologies	3	Introducing transformations: Turns (rotations)	<ul> <li>describe the process of performing a 'turn' and the similarities and differences between the original shape and the shape after it has undergone a 'turn' about a centre of rotation</li> <li>recognise and describe turns as 'clockwise' or 'anti-clockwise'</li> <li>identify and describe one-step quarter turns, half turns and three-quarter turns of a shape using the terms 'quarter turn', 'half turn', 'three-quarter turn'</li> <li>perform one-step quarter turns, half turns and three-quarter turns of shapes using physical materials and record the results without the use of digital technology</li> <li>perform one-step quarter turns, half turns and three-quarter turns of a shape and perform a one-step flip of a shape, recording the results using digital technology</li> <li>predict and draw the result of one-step quarter turns, half turns and three-quarter turns on a given shape</li> <li>explore and describe the number of half turns and quarter turns required for a full-turn</li> </ul>		
	Le	earning Journeys	Creating and drawing summertical designs		
MG.G.4 Create symmetrical patterns, pictures and shapes, with and without the use of digital technologies	1	Creating and drawing symmetrical designs and shapes	<ul> <li>create symmetrical designs using physical materials</li> <li>create symmetrical shapes using physical materials</li> <li>draw symmetrical designs and shapes without the use of digital technology</li> <li>create symmetrical designs and shapes using digital technology</li> </ul>		
	2	Completing symmetrical designs	complete symmetrical designs and shapes given their line of symmetry and one half of the design or shape		
		Learning Jo	ourneys Recognising tessellations		
MG.G.4 Create symmetrical patterns, pictures and shapes, with and without the use of digital technologies	1	Recognising tessellations	<ul> <li>recognise and describe transformations in tessellating designs consisting of a single shape</li> <li>create and record tessellating designs using transformations on a single shape</li> <li>determine whether a shape will or will not tessellate</li> </ul>		



## **Understanding Practice and Fluency (UPF)**

MA2-16MC identifies, describes, compares and classifies angles				
Quest: (1) Angle introduction				
Learning Journeys Identifying and comparing angles				
Content Descriptor	Steps	Spine Nodes	Subnodes	
MG.H.1 Identify angles as measures of turn and compare angle sizes in everyday situations	1	Introducing right angles	<ul> <li>identify right angles on two-dimensional shapes and three-dimensional objects</li> <li>identify right angles in pictures, designs and the environment</li> <li>identify right angles in line diagrams</li> <li>use and interpret the symbol   in diagrams to represent a right angle</li> <li>define perpendicular lines and identify them in pictures, designs and the environment</li> <li>recognise that a pair of perpendicular lines form 4 right angles</li> </ul>	
	2	Comparing angles informally	<ul> <li>compare angles directly by placing 1 angle over another</li> <li>compare angles indirectly by using a hinged angle measurer</li> </ul>	
		Learnin	g Journeys Introducing angles	
MG.H.1 Identify angles as measures of turn and compare angle sizes in everyday situations	1	Introducing the concept of angles up to 180°	<ul> <li>understand and describe angles as an amount of turning, openings</li> <li>identify angles in everyday situations, eg door openings, designs, between the arms of a clock</li> <li>recognise that angles are formed whenever 2 lines meet or when 2 rays meet at a common endpoint</li> </ul>	
Quest: (2) Angle introduction				
		Learnir	g Journeys Classifying angles	
	2	Classifying angles in relation to a right angle	classify angles as 'less than a right angle', 'about the same as a right angle', 'greater than a right angle'	
MG.H.2 Compare angles and classify them as equal to, greater than or less than a right angle	3	Classifying angles as acute, right or obtuse	<ul> <li>identify and name angles as acute, right or obtuse</li> <li>categorise angles as acute, right or obtuse</li> <li>draw and create angles of a given size: acute, right, obtuse (no protractors)</li> </ul>	
	4	Classifying angles as acute, right, obtuse, straight, reflex or a revolution	<ul> <li>understand and describe angles greater than or equal to 180°</li> <li>identify and name angles as acute, right, obtuse, straight, reflex and revolution</li> <li>categorise angles as acute, right, obtuse, straight, reflex and revolution</li> <li>draw and create angles of a given size: acute, right, obtuse, straight, reflex and revolution (no protractors)</li> </ul>	



#### **Understanding Practice and Fluency (UPF)**

directions

#### **Measurement and Geometry**

MA2-17MG uses simple maps and grids to represent position and follow routes, including using compass directions Quest: (1) Simple maps & grids Learning Journeys Interpreting and creating referenced maps Content **Steps Spine Nodes** Subnodes Descriptor · establish that grid referencing on maps allows for more accurate description of features/locations understand the structure (letter then number, horizontal then vertical) Interpreting grid 1 and meaning of grid references (everything in that grid square) referenced maps • use grid references to describe features/locations on maps • identify features/locations on maps given their gird reference MG.I.1 Create and interpret simple • draw grid referenced maps of familiar locations such as the classroom, grid maps to school or local area Creating grid show position and 2 referenced maps use technology to create grid referenced maps of familiar locations such pathways as the classroom, school or local area draw a path from 1 feature to another on a grid referenced map given the Drawing pathways grid reference of each feature on grid referenced 3 use grid references to describe a path from 1 feature to another on a grid maps referenced map Quest: (2) Simple maps & grids **Learning Journeys** Using legends and reading maps • establish the need for legends on maps with and without grid referencing • use the legend of a map to determine the feature located at a given grid Using legends on 1 maps • use the legend of a map to determine the grid reference for a given feature • understand, locate and label the 4 cardinal compass directions on a compass rose: north (N), south (S), east (E) and west (W) Introducing connect the 4 cardinal compass directions to features of the local area cardinal compass from their particular location directions MG.I.2 Use simple determine the direction of other cardinal compass directions when given scales, legends one of the cardinal compass directions and directions Describing to interpret • recognise that north (N) is typically represented by an arrow on a map locations on information use the 4 cardinal compass directions to describe the location of one 3 contained in basic maps using feature in relation to another on a map that has an arrow representing cardinal compass maps north directions • follow a sequence of 2 or more directions to find a location within a safe Following and zone of the school giving cardinal 4 compass give a sequence of 2 or more directions for a another person to find a directions location within a safe zone of the school • draw a route on a map given a sequence of directions involving cardinal Drawing routes directions and landmarks on maps using 5 cardinal compass use cardinal directions and landmarks to describe a route between 2

locations on a map



## **Understanding Practice and Fluency (UPF)**

Onest (2) Circular and Amida	
directions	
MA2-17MG uses simple maps and grids to represent position and follow routes, including using compass	

MAZ 171113 uses	directions			
Quest: (2) Simple maps & grids				
Learning Journeys Solving measurement problems				
Content Descriptor	Steps	Spine Nodes	Subnodes	
MG.I.2 Use simple scales, legends and directions to interpret information contained in basic maps	1	Using multiplication and division to solve measurement and scaling problems (within 100)	<ul> <li>solve simple rates problems using multiplication and division (within 100), eg 'Teesha made 3 cards in 1 hour. How many cards can she make in 3 hours?'</li> <li>write equations using a symbol, eg a box or a blank, to represent the unknown number compare their own and others' methods of solution</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

#### **Statistics and Probability**

data displays, including tables, picture graphs and column graphs					
Quest: (1) Display & interpret data					
Learning Journeys Introducing the statistical investigation process					
Content Descriptor	Steps	Spine Nodes	Subnodes		
SP.A.1 Identify questions or issues for categorical variables; identify data sources and plan methods of data collection and recording	1	Introducing the statistical investigation process (including line plots)	<ul> <li>determine what data to gather in order to investigate a question of interest, eg colour, mode of transport, gender, type of animal, sport</li> <li>collect data through questioning and record the data using tally marks</li> <li>dentify categories of data and use them to sort data, eg sort data collected on attendance by day of the week and into boys and girls present</li> <li>represent numerical or category data in a table, list or picture graph (one-to-one correspondence)</li> <li>record observations based on data collected and displayed in a list, table, picture graph or line plot</li> </ul>		
	2	Introducing the statistical investigation process (tables, lists, picture graphs or bar graphs)	<ul> <li>determine what data to gather in order to investigate a question of interest, eg colour, mode of transport, gender, type of animal, sport</li> <li>collect data through questioning and record the data using tally marks</li> <li>identify categories of data and use them to sort data, eg sort data collected on attendance by day of the week and into boys and girls present</li> <li>represent category data in a table, list, bar graph or picture graph (one-to-one correspondence)</li> <li>record observations based on data collected and displayed in a list, table, picture graph, or simple bar graph</li> </ul>		
		Lear	ning Journeys Category data		
SP.A.1 Identify questions or issues for categorical variables; identify data sources and plan methods of data collection and recording	1	Posing questions related to category data	<ul> <li>pose questions about a matter of interest to obtain information that can be recorded in categories</li> <li>adjust statistical questions to ensure their suitability</li> <li>recognise that data can be collected by the user or others; identify possible sources of data collected by others, eg newspapers, government data-collection agencies, sporting agencies, environmental groups</li> <li>pose questions based on category data recorded by others</li> </ul>		
	2	Collecting and recording category data	<ul> <li>predict and create a list of categories for efficient data collection in relation to a matter of interest, eg 'Which breakfast cereal is the most popular with members of our class?'</li> <li>collect data by conducting a simple survey and create a list or table (with and without digital technology) to organise the data, eg collect data on the number of each colour of lollies in a packet</li> <li>compare collection and recording methods</li> </ul>		
		Learning	Journeys Statistical Investigations		
SP.A.2 Collect data, organise it into categories, and create displays using lists, tables, picture graphs and simple column graphs, with and without the use of digital technologies	1	Constructing and interpreting tables	<ul> <li>represent given or collected categorical data in tables using appropriate headings and structure</li> <li>interpret data in tables to solve problems; answer comparative and summative questions</li> </ul>		
	2	Conducting a simple statistical investigation (tables, lists, picture graphs, bar graphs)	<ul> <li>determine what data to gather in order to investigate a statistical question collect, record and sort data</li> <li>represent category data in a table, list, picture graph or column graph (including many-to-one correspondence)</li> <li>make a simple concluding statement based on data collected</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Statistics and Probability**

data displays, including tables, picture graphs and column graphs							
Quest: (1) Display & interpret data							
	Learning Journeys Representing and interpreting information						
Content Descriptor	Steps	os Spine Nodes Subnodes					
	1	Introducing and reading data in column graphs with one-to-one correspondence	<ul> <li>become familiar with the structure and layout of a basic column graph including title, labels on each axis, equal spacing</li> <li>answer one-step and two-step questions, eg, 'How many more students like reading than art?'; identify basic similarities and differences between categories; make simple conclusions</li> <li>recognise and remedy errors in column graphs</li> </ul>				
SP.A.2 Collect data, organise it into categories, and create displays using lists, tables, picture graphs and simple column graphs, with and	2	Representing and reading data in a given column graph with one-to-one correspondence	<ul> <li>complete a vertical or horizontal column graph (one-to-one correspondence); choose the correct title for a bar graph</li> <li>answer one-step and two-step questions, eg, 'How many more students like reading than art?'; identify basic similarities and differences between categories; make simple conclusions</li> <li>agree or disagree with simple statements made by others related to data in a column graph</li> </ul>				
without the use of digital technologies	3	Representing and reading data displayed in tables or lists	<ul> <li>display category or numerical data using lists and tables</li> <li>pose questions and answer one-step and two-step questions, eg 'How many more students like reading than art?'; identify basic similarities and differences between categories; make simple conclusions</li> </ul>				
	4	Representing and reading category data in a table	<ul> <li>represent primary or secondary data in a given table using appropriate headings and layout</li> <li>interpret data in a table; ask and answer summative and comparative questions</li> </ul>				
		Learning	Journeys Comparing data displays				
SP.A.3 Interpret and compare data displays	1	Comparing basic data displays (tables, lists, picture graphs, column graphs)	<ul> <li>represent the same data set using more than one type of display (tables, lists, picture graphs or column graphs) and compare the displays</li> <li>discuss the advantages and/or disadvantages of different representations of the same data</li> <li>describe information and make conclusions about data presented in different data displays, eg 'Football is the most popular sport for students in Year 3 at our school'</li> </ul>				



### **Understanding Practice and Fluency (UPF)**

#### **Statistics and Probability**

data displays, including tables, picture graphs and column graphs							
Quest: (2) Display & interpret data							
Learning Journeys Select and trial methods for data collection							
Content Descriptor	Steps	Spine Nodes	Subnodes				
	1	Creating and refining a survey	<ul> <li>create a survey and related recording sheet, considering the appropriate organisation of categories for data collection; predict possible responses</li> <li>identify questions and issues relevant to given categorical data, matches statistical questions with given data sets; recognises statistical questions that are clearly unsuitable</li> <li>choose effective ways to collect and record data for an investigation, eg creating a survey with a scale of 1 to 5 to indicate preferences</li> <li>refine survey questions as necessary after a small trial</li> <li>discuss and decide the most suitable question to investigate a particular matter of interest, eg by narrowing the focus of a question</li> </ul>				
SP.A.4 Select and trial methods for data collection, including survey questions and recording sheets	2	Conducting and evaluating a survey	<ul> <li>conduct a survey to collect categorical data</li> <li>discuss and determine possible improvements to the questions or recording sheet</li> <li>compare the effectiveness of different methods of collecting and recording data</li> <li>discuss the advantages and/or disadvantages of open-ended questions in a survey, compared to questions with predetermined categories</li> </ul>				
	3	Collecting and sorting data	<ul> <li>plan methods of data collection (eg, surveying or questioning, when to ask, who to ask) and efficient ways of * recording data (eg, tables and tally charts); identify issues with data collection and refines the process as appropriate</li> <li>recognise that data can come from other sources, eg governmental agencies, sports, environmental agencies</li> <li>sort data into the correct categories; enter data into the correct cells in a table; create a table in a spreadsheet (digital recording); recognise when data has been sorted incorrectly</li> </ul>				
	Learn	ing Journeys Col	lumn graphs using many-to-one correspondence				
SP.A.5 Construct suitable data displays, with and without the use of digital technologies, from given or collected data; include tables, column graphs and picture graphs where one picture can represent many data values	1	Introducing column graphs with many-to-one correspondence	<ul> <li>determine the scale on a column graph</li> <li>read and interpret data in a column graph with many-to-one correspondence</li> <li>recognise and remedy errors or unsuitable scales in a column graph</li> </ul>				
	2	Representing data in column graphs using many-to-one correspondence	<ul> <li>represent given or collected categorical data in column graphs</li> <li>discuss and determine a suitable scale of many-to-one correspondence to draw graphs for large data sets and state the key used</li> <li>use grid paper to assist in drawing graphs that represent data using a scale of many-to-one correspondence</li> <li>use data in a spreadsheet to create column graphs with appropriately labelled axes</li> <li>mark equal spaces on axes, name and label axes, and choose appropriate titles for graphs</li> <li>interpret data in column graph; ask and answer questions related to the data in the display; draw conclusions</li> </ul>				



### **Understanding Practice and Fluency (UPF)**

#### **Statistics and Probability**

data displays, including tables, picture graphs and column graphs					
Quest: (2) Display & interpret data					
Learning Journeys Picture graphs with many-to-one correspondence					
Content Descriptor	Steps	Spine Nodes	Subnodes		
SP.A.5 Construct suitable data displays, with and without the use of	1	Introducing picture graphs with many-to-one correspondence	<ul> <li>interpret the key on a picture graph with many-to-one correspondence</li> <li>read and interpret data in a picture graph with many-to-one correspondence</li> <li>recognise and remedy errors or unsuitable scales in a picture graph</li> </ul>		
digital technologies, from given or collected data; include tables, column graphs and picture graphs where one picture can represent many data values	2	Representing data in picture graphs using many-to-one correspondence	<ul> <li>represent given or collected categorical data in picture graphs</li> <li>discuss and determine a suitable scale of many-to-one correspondence to draw graphs for large data sets and state the key used</li> <li>use grid paper to assist in drawing graphs that represent data using a scale of many-to-one correspondence</li> <li>mark equal spaces on axes, name and label axes, and choose appropriate titles for graphs</li> <li>interpret data in a picture graph; ask and answer questions related to the</li> </ul>		
			data in the display; draw conclusions		
	L	earning Journeys	Evaluating and comparing data displays		
SP.A.6 Evaluate the effectiveness of different displays in illustrating data features, including variability	1	Evaluating and comparing data displays	<ul> <li>interpret and evaluate the effectiveness of various data displays found in media and in factual texts, where displays represent data using a scale of many-to-one correspondence</li> <li>identify and discuss misleading representations of data</li> <li>discuss and compare features of data displays, including considering the number and appropriateness of the categories used, eg a display with only three categories (blue, red, other) for car colour is not likely to be useful</li> <li>discuss the advantages and disadvantages of different representations of the same categorical data, eg column graphs compared to picture graphs that represent data using scales of many-to-one correspondence</li> </ul>		
MA2-19	SP desc	ribes and compa	res chance events in social and experimental contexts		
		Ques	t: (1) Explore chance events		
		Learning Jouri	neys Conducting chance experiments		
SP.B.1 Conduct chance experiments, identify and describe possible outcomes, and recognise variation in results	1	Introducing chance experiments (with equal outcomes)	<ul> <li>use the term 'outcome' to describe any possible result of a chance experiment</li> <li>predict and list all possible outcomes in a chance experiment, eg list the outcomes when 3 pegs are randomly selected from a bag containing an equal number of pegs of 2 colours</li> <li>predict the number of times each outcome should occur in a chance experiment involving a set number of trials</li> </ul>		
	2	Conducting chance experiments (with equal outcomes)	<ul> <li>predict and list all possible outcomes in a chance experiment, eg list the outcomes when 3 pegs are randomly selected from a bag containing an equal number of pegs of 2 colours</li> <li>keep a tally and graph the results of a chance experiment</li> <li>explain any differences between expected results and actual results in a chance experiment; make statements that acknowledge 'randomness' in a situation, eg 'The spinner could stop on any colour'</li> </ul>		



## **Understanding Practice and Fluency (UPF)**

#### **Statistics and Probability**

MA2-19SP describes and compares chance events in social and experimental contexts						
	Quest: (1) Explore chance events					
Learning Journeys Conducting chance experiments						
Content Descriptor	Steps	Spine Nodes	Subnodes			
SP.B.1 Conduct chance experiments, identify and describe possible outcomes, and recognise variation in results	3		<ul> <li>use the term 'outcome' to describe any possible result of a chance experiment</li> <li>predict and list all possible outcomes in a chance experiment, eg describe the probability of spinning red when you spin a spinner that has 1/2f shaded yellow, 1/4 shaded blue and 1/4 shaded red</li> <li>predict the number of times each outcome should occur in a chance</li> </ul>			
	4	Conducting chance experiments (with unequal outcomes)	<ul> <li>experiment involving a set number of trials</li> <li>predict and list all possible outcomes in a chance experiment, eg describe the probability of spinning red when you spin a spinner that has 1/2 shaded yellow, 1/4 shaded blue and 1/4 shaded red</li> <li>keep a tally and graph the results of a chance experiment</li> <li>explain any differences between expected results and actual results in a chance experiment; make statements that acknowledge 'randomness' in a situation, eg 'The spinner could stop on any colour'</li> </ul>			
	5	Introducing chance situations	<ul> <li>predict and record all possible combinations in a chance situation, eg list all possible outfits when choosing from three different T-shirts and 2 different pairs of shorts</li> <li>record and explain possible combinations using a list, table or diagram</li> <li>repeat a chance experiment several times and discuss why the results vary</li> </ul>			
		Quest: (2	2) Explore chance events			
	Lea	rning Journeys De	escribing the chance of events occurring			
SP.B.2 Describe possible everyday	1	Describing the chances of everyday events occurring	<ul> <li>use the terms 'equally likely', 'likely' and 'unlikely' to describe the chance of everyday events occurring compare the chance of familiar events occurring and describe the events as being 'more likely' or 'less likely' to occur than each other</li> <li>order events from least likely to most likely to occur</li> </ul>			
events and order their chances of occurring		Describing the chances of events occurring in simple chance experiments	compare the likelihood of obtaining particular outcomes in a simple chance experiment			
	L	earning Journeys	Exploring everyday events occurring			
SP.B.3 Identify everyday events where one occurring cannot happen if the other happens	1	Exploring everyday events that cannot occur simultaneously	identify and discuss everyday events that cannot occur at the same time			
	Lea	rning Journeys Ide	entifying the chance of events occurring			
SP.B.4 Identify events where the chance of one occurring will not be affected by the occurrence of the other	1	Identifying events where the chances of occurring are independent of other events	<ul> <li>identify and discuss events where the chance of 1 event occurring will not be affected by the occurrence of the other</li> <li>explain why subsequent events are independent</li> <li>compare independent events with dependent events</li> </ul>			



## **Understanding Practice and Fluency (UPF)**

MA3-4NA orders,	reads a	nd represents intege	rs of any size and describes properties of whole numbers
		Quest: (1) Num	nber properties & integers
	Lea	arning Journeys Reco	gnise, represent and order numbers
Content Descriptor	Steps	Spine Nodes	Subnodes
	1	Reading and writing numbers of any size	<ul><li>apply an understanding of place value to read numbers of any size</li><li>apply an understanding of place value to write numbers of any size</li></ul>
	2	Comparing 2 numbers of any size	• compare 2 numbers of any size using words and symbols <, =, >
	2	Ordering numbers of any size	arrange numbers of any size in ascending and descending order
		Identifying the place	state the place value of digits in numbers of any size
NA.A.1 Recognise, represent and order	3	Identifying the place value of numbers of any size	• recognise different abbreviations of numbers used in everyday contexts, eg \$35 M represents \$35 000 000
numbers to at least		arry size	• use place value understanding to count by 10,000 and 100,000
tens of millions	4	Using place value to partition numbers of any size	use place value understanding and models to partition numbers of any size
		Using non-standard partitioning with numbers of any size	partition numbers of any size in non-standard forms
	5	Rounding numbers to a specified place value	• round numbers to a specified place value, eg round 5 461 883 to the nearest million
		Learning Journ	neys Multiples and Factors
NA.A.2 Identify and	1	Finding factors for whole numbers up to 100	<ul> <li>determine all 'factors' of a given whole number up to 100</li> <li>determine the 'highest common factor' (HCF) of 2 whole numbers</li> </ul>
describe factors and multiples of whole numbers and	2	Finding multiples up to 100	<ul> <li>determine 'multiples' of a given whole number</li> <li>determine the 'lowest common multiple' (LCM) of 2 whole numbers</li> </ul>
use them to solve problems	3	Solving problems using factors and multiples	• solve problems using knowledge of factors and multiples, eg 'There are 48 people at a party. In how many ways can you set up the tables and chairs, so that each table seats the same number of people and there are no empty chairs?'
		Quest: (2) Nun	nber properties & integers
		Learning Journeys	Square and Triangular numbers
NA.A.4 Identify and describe properties	1	Describing square numbers	model square numbers and record each number group in numerical and diagrammatic form
of prime, composite, square and triangular numbers	2	Describing triangular numbers	model triangular numbers and record each number group in numerical and diagrammatic form



## **Understanding Practice and Fluency (UPF)**

MA3-4NA orders, reads and represents integers of any size and describes properties of whole numbers						
	Quest: (2) Number properties & integers					
Learning Journeys Investigating Integers						
Content Descriptor	Steps	Spine Nodes	Subnodes			
NA.A.3 Investigate everyday situations	1	Investigating integers in context	interpret integers in everyday contexts, eg temperature count forwards and backwards with positive and negative whole numbers, including through 0 (in context)			
that use integers; locate and represent these numbers on a	2	Investigating integers  • recognise the location of negative whole numbers in relation and place them on a number line				
number line	3	Interpreting integers in context	use a model to interpret intervals across zero (in context)			
		Learning Journeys	Prime and composite numbers			
NA.A.4 Identify and describe properties of prime, composite,	1	Introducing prime and composite numbers	know and recall all prime numbers up to 19			
square and triangular numbers	2	Identifying prime and composite numbers	determine whether a number is prime, composite or neither			
MA3-5NA selects a	nd app	lies appropriate strat	egies for addition and subtraction with counting numbers of any size			
		Quest: (1) Add	l/sub numbers of any size			
		Learning Journey	s Adding numbers of any size			
	1	Using a formal written algorithm for addition calculations involving numbers of any size (no regrouping)	apply algorithms to solve problems without regrouping, with the same number of places and with a different number of places; include opportunities for students to write their own algorithms with digits in correct place value positions; include word problems			
NA.B.1 Use efficient mental and written strategies and apply appropriate digital technologies to solve problems	2	Using a formal written algorithm for addition calculations involving numbers of any size (with regrouping)	apply algorithms to solve problems with regrouping in 1 or more places, with the same number of places and with a different number of places; include opportunities for students to write their own algorithms with digits in correct place value positions; include word problems			
	3	Using a formal written algorithm for addition calculations of 3 or more addends up to any size (with and without regrouping)	apply algorithms with 3 or more addends with the same number of places and with a different number of places; include opportunities for students to write their own algorithms with digits in correct place value positions; include word problems			
		Learning Journeys	Subtracting numbers of any size			
NA.B.1 Use efficient mental and written strategies and apply appropriate digital technologies to solve problems	1	Using a formal written algorithm to record subtraction calculations involving numbers of any size (without decomposing)	• apply algorithms to solve problems without trading (decomposing), with the same number of places for both numbers, with fewer places in the second number (subtrahend) and with and without 1 or more zeros in the first number (minuend); include opportunities for students to write their own algorithms with digits in correct place value positions and with the larger number first; include word problems			



### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA3-5NA selects and applies appropriate strategies for addition and subtraction with counting numbers of any size

of any size					
Quest: (1) Add/sub numbers of any size					
Learning Journeys Subtracting numbers of any size					
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.B.1 Use efficient mental and written strategies and apply appropriate digital	2	Using a formal written algorithm to record subtraction calculations involving numbers of any size (with decomposing)	<ul> <li>apply algorithms to solve problems with trading (decomposing) in 1 or more places, with the same number of places for both numbers, with fewer places in the second number (subtrahend) and with and without 1 or more zeros in the first number (minuend); include opportunities for students to write their own algorithms with digits in correct place value positions and with the larger number first; include word problems</li> </ul>		
technologies to solve problems	3	Using equal adjustments to subtract up to 3-digit numbers	model and solve subtraction problems using equal adjustments		
	Lear	ning Journeys Addin	g and subtracting numbers of any size		
NA.B.1 Use efficient mental and written	1	Representing addition or subtraction problems using a bar model	use a bar model as a tool to represent an addition or subtraction problem		
strategies and apply appropriate digital technologies to solve problems	2	Applying efficient strategies for addition and subtraction calculations involving numbers of any size	add 3 or more numbers with different numbers of digits		
	Le	arning Journeys Che	cking with estimation and rounding		
NA.B.2 Use estimation and rounding to check the reasonableness of answers to calculations		Checking accuracy of addition and subtraction calculations	<ul> <li>check solutions to problems by using the inverse operation</li> <li>use estimation to check the reasonableness of answers to addition and subtraction calculations</li> </ul>		
		Quest: (2) Add	d/sub numbers of any size		
	Lea	arning Journeys Add	ition and subtraction word problems		
NA.B.4 Select and apply efficient mental	1	Solving addition word problems involving numbers of any size	<ul> <li>select and apply efficient mental strategies to solve word problems</li> <li>select and apply efficient written strategies to solve word problems</li> <li>use a calculator to solve word problems</li> <li>interpret words that indicate the required operation</li> <li>justify the choice of strategy for a given calculation</li> </ul>		
and written strategies and appropriate digital technologies to solve problems involving addition and	2	Solving subtraction word problems involving numbers of any size	<ul> <li>select and apply efficient mental strategies to solve word problems</li> <li>select and apply efficient written strategies to solve word problems</li> <li>use a calculator to solve word problems</li> </ul>		
subtraction with whole numbers	3	Solving word problems requiring both addition and subtraction involving numbers of any size	<ul> <li>select and apply efficient mental strategies to solve word problems</li> <li>select and apply efficient written strategies to solve word problems</li> </ul>		



## **Understanding Practice and Fluency (UPF)**

MA3-7N	MA3-7NA compares, orders and calculates with fractions, decimals and percentages						
	Quest: (1) Mult/div & order of operations						
Learning Journeys Multiplication using multiples of 10							
Content Descriptor	Steps	Spine Nodes	Subnodes				
NA.C.1 Solve problems involving multiplication of large numbers by one- or	1	Using known facts to multiply 1-digit numbers with multiples of 1000	<ul> <li>use known facts and place value understanding to solve multiplication problems with multiples of 1000, eg 3 x 6 = 18 so 3 x 6000 = 18 000</li> </ul>				
two-digit numbers using efficient mental and written strategies and appropriate digital technologies	2	Using known facts to multiply 1-digit numbers with multiples of 10 000	<ul> <li>use known facts and place value understanding to solve multiplication problems with multiples of 1000, eg 3 x 6 = 18 so 3 x 60 000 = 180 000</li> </ul>				
	Learn	ing Journeys Mult: rour	nding, compensating and partitioning				
NA C4 C. I	1	Multiplying 1-digit and 2-digit numbers using rounding and compensating	• use known facts to solve multiplication problems by adding on or taking off, eg 5 $\times$ 100 is 500, so 5 $\times$ 99 is 5 less, which is 495				
NA.C.1 Solve problems involving multiplication of large numbers by one- or	2	Using partitioning to double or halve any number (up to 4-digits)	<ul> <li>use models and diagrams to support partitioning to double or halve any number (up to 4-digits), eg 58 halved as half of 50 + half of 8, or double 58 as double 50 + double 8</li> </ul>				
two-digit numbers using efficient mental and written strategies and appropriate	3	Using compensation to double or halve any number (up to 4-digits)	<ul> <li>use models and diagrams to support the use of compensation to double or halve any number (up to 4-digits), eg double 398 as double 400 and subtract 4, or half of 398 as half of 400 and subtract 1</li> </ul>				
digital technologies	4	Using partitioning or compensation to double or halve any number (up to 4-digits)	use partitioning or compensation to double or halve any number (up to 4-digits)				
	I	earning Journeys Mult	t: doubling, halving and thirding				
		Multiplying using doubling	• use the relationship between multiplication facts, eg the multiplication facts for 6 are double the multiplication facts for 3				
	4		• use doubling as a strategy to multiply by 2, eg 70 × 2 is double 70				
	1	Multiplying by 2, 4 or 8	• use double-double as a strategy to multiply by 4, eg 70 × 4 is double-double 70 which is 280				
NA C1 Solve		using repeated doubling	<ul> <li>use doubling as a strategy to multiply by 8, eg 70 × 8 is double- double-double 70 which is 560</li> </ul>				
NA.C.1 Solve problems involving multiplication of large numbers by one- or two-digit numbers using efficient mental and written strategies and appropriate digital technologies	2	Using doubling and halving to solve multiplication problems with 2-digit and 1-digit numbers	• mentally adjust a multiplication problem by doubling one factor and halving the other, eg 24 x 6 as 12 x 12				
	3	Using doubling and halving to solve multiplication problems with a 1-digit number and a 1 or 2-digit number	• mentally adjust a multiplication problem by doubling one factor and halving the other, eg 24 x 50 as 12 x 100				
	4	Using doubling and halving or thirding and trebling to solve multiplication problems	<ul> <li>mentally adjust a multiplication problem using doubling and halving or thirding and trebling where appropriate, eg 18 x 3 as 6 x 9 or 24 x 6 as 12 x 12</li> </ul>				



## **Understanding Practice and Fluency (UPF)**

MA3-7NA compar	es, orde	ers and calculates with fractions	s, decimals and percentages
	Qu	est: (1) Mult/div & order of oper	ations
Le	arning	Journeys Multiplying using the	split method
Content Descriptor	Steps	Spine Nodes	Subnodes
NA.C.1 Solve problems involving multiplication of large numbers by one- or two-digit numbers	1	Multiplying 3-digit numbers by 1-digit numbers using split method	multiply the hundreds, then the tens and then the ones
using efficient mental and written strategies and appropriate digital technologies	2	Multiplying 4-digit numbers by 1-digit numbers using split method	multiply the thousands, then the hundreds, then the tens and then the ones
	Learr	ning Journeys Multiplying by fa	ctorising
NA.C.1 Solve problems involving multiplication of large numbers	1	Multiplying by factorising (using the distributive property)	• split factors, eg 50 × 8 is the same as 50 × 2 × 4, which becomes 100 × 4
by one- or two-digit numbers using efficient mental and written strategies and appropriate digital technologies	2	Factorising to multiply a 2-digit number by a 2-digit number	• factorise to multiply a 2-digit number by a 2-digit number, eg 12 × 25 = 3 × 4 × 25 = 3 × 100 = 300
L	earning	Journeys Multiplying using an	area model
NA.C.1 Solve problems involving	1	Multiplying 3-digit numbers by 1-digit numbers using an area model	use an area model for 3-digit by 1-digit multiplication
multiplication of large numbers by one- or two-digit numbers using efficient mental and written strategies and appropriate digital	2	Multiplying 4-digit numbers by 1-digit numbers using an area model	use an area model for 4-digit by 1-digit multiplication
technologies	3	Multiplying 2-digit numbers by 2-digit numbers using an area model	use an area model for 2-digit by 2-digit multiplication
Lea	rning J	ourneys Multiplying using form	nal algorithms
	1	Multiplying 2-digit numbers by 1-digit numbers using the expanded algorithm	multiply the ones, then the tens, with and without regrouping
		Multiplying 3-digit numbers by 1-digit numbers using the expanded algorithm	multiply the ones, then the tens, then the hundreds, with and without regrouping
		Multiplying 4-digit numbers by 1-digit numbers using the expanded algorithm	multiply the ones, then the tens, then the hundreds and then the thousands, with and without regrouping
NA.C.1 Solve problems involving multiplication of large numbers		Multiplying 2-digit numbers by 1-digit numbers using the contracted algorithm	multiply the ones, then the tens, with and without regrouping
by one- or two-digit numbers using efficient mental and written strategies and appropriate digital	2	Multiplying 3-digit numbers by 1-digit numbers using the contracted algorithm	multiply the ones, then the tens, then the hundreds, with and without regrouping
technologies		Multiplying 4-digit numbers by 1-digit numbers using the contracted algorithm	multiply the ones, then the tens, then the hundreds and then the thousands, with and without regrouping
	3	Multiplying 2-digit numbers by 2-digit numbers using the extended form of the formal algorithm	multiply 2-digit by 2-digit numbers using extended form, with and without regrouping
	J	Multiplying 3-digit numbers by 2-digit numbers using the extended form of the formal algorithm	multiply 3-digit by 2-digit numbers using extended form, with and without regrouping



## **Understanding Practice and Fluency (UPF)**

MA3-7NA co	mpares,	orders and calculates with fra	actions, decimals and percentages			
		Quest: (1) Mult/div & order o	f operations			
Learning Journeys Multiplication word problems						
Content Descriptor	Steps	Spine Nodes	Subnodes			
NA.C.1 Solve problems involving multiplication of large numbers by one-or two-digit numbers using efficient mental and written strategies and appropriate digital technologies	1	Solving multiplication word problems	<ul> <li>apply appropriate mental strategies to solve multiplication word problems</li> <li>apply appropriate written strategies to solve multiplication word problems</li> </ul>			
	L	earning Journeys Division usi	ng partitioning			
NA.C.2 Solve problems involving division by a one-digit number, including those that result in a remainder	1	Dividing a 3-digit number by a 1-digit number using partitioning	partition a 3-digit number to divide			
L	earning	Journeys Extended division -	no remainders or zeros			
	1	Dividing a 2-digit number by a 1-digit divisor using the extended algorithm, no remainders or zeros in answers	apply the written algorithm to divide a 2-digit number by a 1-digit number, without remainders and without zeros in the answer			
NA.C.2 Solve problems involving division by a one-	2	Dividing a 3-digit number by a 1-digit divisor using the extended algorithm, no remainders or zeros in answers	apply the written algorithm to divide a 3-digit number by a 1-digit number, without remainders and without zeros in the answer			
digit number, including those that result in a remainder	3	Dividing a 4-digit number by a 1-digit divisor using the extended algorithm, no remainders or zeros in answers	apply the written algorithm to divide a 4-digit number by a 1-digit number, without remainders and without zeros in the answer			
	4	Solving problems involving division of a 2-digit number by a one-digit number, with no remainders	recognise and use different notations to indicate division			
	Lea	arning Journeys Extended divi	sion - remainders			
	1	Dividing a 2-digit number by a 1-digit divisor using the extended algorithm, with remainders but without zeros in answers	apply the written algorithm to divide a 2-digit number by a 1-digit number, with remainders but without zeros in the answer			
NA.C.2 Solve problems involving division by a one-digit number, including	2	Dividing a 3-digit number by a 1-digit divisor using the extended algorithm, with remainders but without zeros in answers	apply the written algorithm to divide a 3-digit number by a 1-digit number, with remainders but without zeros in the answer			
those that result in a remainder	3	Dividing a 4-digit number by a 1-digit divisor using the extended algorithm, with remainders but without zeros in answers	apply the written algorithm to divide a 4-digit number by a 1-digit number, with remainders but without zeros in the answer			
	4	Solving problems involving division of a 2-digit number by a 1-digit number, with remainders	record remainders as fractions and decimals			



## **Understanding Practice and Fluency (UPF)**

MA3-7NA co	mpares,	orders and calculates with fract	ions, decimals and percentages			
Quest: (1) Mult/div & order of operations						
Lear	ning Jo	urneys Extended division - with a	and without remainders			
Content Descriptor	Steps	Spine Nodes	Subnodes			
	1	Dividing a 2-digit number by a 1-digit divisor using the extended algorithm, with and without remainders and zeros in answers	apply the written algorithm to divide a 2-digit number by a 1-digit number, with and without remainders and zeros in the answer			
NA.C.2 Solve problems involving division by a one-	2	Dividing a 3-digit number by a 1-digit divisor using the extended algorithm, with and without remainders and zeros in answers	apply the written algorithm to divide a 3-digit number by a 1-digit number, with and without remainders and zeros in the answer			
digit number, including those that result in a remainder	3	Dividing a 4-digit number by a 1-digit divisor using the extended algorithm, with and without remainders and zeros in answers	apply the written algorithm to divide a 4-digit number by a 1-digit number, with and without remainders and zeros in the answer			
	4	Solving problems involving the division of a number with 3 or more digits by 1 digit, with no remainder	<ul> <li>divide the hundreds, then the tens, and then the ones</li> <li>use the formal algorithm</li> </ul>			
Le	arning	Journeys Contracted division - no	o remainders or zeros			
	1	Dividing a 2-digit number by a 1-digit divisor using the contracted algorithm, no remainders or zeros in answers	apply the written algorithm to divide a     2-digit number by a 1-digit number, without     remainders and without zeros in the answer			
NA.C.2 Solve problems involving division by a one-digit number, including those that result in a remainder	2	Dividing a 3-digit number by a 1-digit divisor using the contracted algorithm, no remainders or zeros in answers	apply the written algorithm to divide a     3-digit number by a 1-digit number, without     remainders and without zeros in the answer			
Terrialituei	3	Dividing a 4-digit number by a 1-digit divisor using the contracted algorithm, no remainders or zeros in answers	apply the written algorithm to divide a     4-digit number by a 1-digit number, without     remainders and without zeros in the answer			
Le	arning	Journeys Contracted division - no	o remainders or zeros			
	1	Dividing a 2-digit number by a 1-digit divisor using the contracted algorithm, with remainders but without zeros in answers	apply the written algorithm to divide a 2-digit number by a 1-digit number, with remainders but without zeros in the answer			
NA.C.2 Solve problems involving division by a one-	2	Dividing a 3-digit number by a 1-digit divisor using the contracted algorithm, with remainders but without zeros in answers	apply the written algorithm to divide a 3-digit number by a 1-digit number, with remainders but without zeros in the answer			
digit number, including those that result in a remainder	3	Dividing a 4-digit number by a 1-digit divisor using the contracted algorithm, with remainders but without zeros in answers	apply the written algorithm to divide a 4-digit number by a 1-digit number, with remainders but without zeros in the answer			
	4	Solving problems involving the division of a number with 3 or more digits by 1 digit, with remainders	<ul> <li>divide the hundreds, then the tens, and then the ones</li> <li>use the formal algorithm</li> </ul>			



## **Understanding Practice and Fluency (UPF)**

MA3-7NA compares, orders and calculates with fractions, decimals and percentages					
		Quest: (1) Mult/div & order of o	perations		
Lear	Learning Journeys Contracted division-with and without remainders				
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Dividing a 2-digit number by a 1-digit divisor using the contracted algorithm, with and without remainders and zeros in answers	* apply the written algorithm to divide a 2-digit number by a 1-digit number, with and without remainders and zeros in the answer		
NA.C.2 Solve problems involving division by a one-digit number, including those that result in a remainder	2	Dividing a 3-digit number by a 1-digit divisor using the contracted algorithm, with and without remainders and zeros in answers	* apply the written algorithm to divide a 3-digit number by a 1-digit number, with and without remainders and zeros in the answer		
	3	Dividing a 4-digit number by a 1-digit divisor using the contracted algorithm, with and without remainders and zeros in answers	* apply the written algorithm to divide a 4-digit number by a 1-digit number, with and without remainders and zeros in the answer		
		Learning Journeys Division word	d problems		
NA.C.2 Solve problems involving division by a one-digit number, including those that result in a remainder	1	Solving division word problems	divide a number with 3 or more digits by a single-digit divisor		
Le	arning J	ourneys Rounding to estimate p	roducts and quotients		
NA.C.3 Use estimation	1	Rounding to estimate products	estimate products by rounding		
and rounding to check the reasonableness of answers to calculations	2	Rounding to estimate quotients	estimate quotients using rounding		
		Quest: (2) Mult/div & order of o	perations		
L	earning	g Journeys Multiplying and dividing	ng by multiples of 10		
		Multiplying any numbers by 10, 100, 1000 and their multiples	• use mental strategies to multiply by 10, 100, 1000 and their multiples		
NA.C.4 Select and apply efficient mental and	1	Using mental strategies to multiply 1-digit and 2-digit numbers by multiples of 10 000	use mental strategies to multiply 1-digit and 2-digit numbers by multiples of 10 000		
written strategies, and appropriate digital technologies, to solve problems involving multiplication and division with whole numbers	2	Dividing any numbers by 10, 100, 1000 and their multiples	• use mental strategies to divide by 10, 100, 1000 and their multiples		
	3	Using known facts to solve multiplication and division problems with multiples of 10 and	<ul> <li>use known facts and place value understanding to solve multiplication problems with multiples of 10 or 100, eg 3 x 6 = 18 so 3 x 600 = 1800</li> <li>use known facts and place value understanding</li> </ul>		
		100	to solve division problems with multiples of 10 or 100, eg $18 \div 6 = 3$ so $1800 \div 600 = 3$		



## **Understanding Practice and Fluency (UPF)**

MA3-7NA compares, orders and calculates with fractions, decimals and percentages				
Quest: (2) Mult/div & order of operations				
	Learn	ing Journeys Selecting efficient n	nult/div strategies	
Content Descriptor	Steps	Spine Nodes	Subnodes	
NA.C.4 Select and apply efficient mental and written strategies, and	1	Selecting efficient strategies to multiply whole numbers of up to 4 digits by 1- and 2-digit numbers	<ul><li>apply mental strategies</li><li>apply efficient use of formal algorithms</li></ul>	
appropriate digital technologies, to solve problems involving multiplication and division with whole numbers	2	Selecting efficient strategies to divide whole numbers of up to 4 digits by a 1-digit divisor	<ul><li>apply mental strategies</li><li>apply efficient use of formal algorithms</li></ul>	
	Learnir	ng Journeys Selecting effective st	rategies for divison	
	1	Dividing using known facts	• solve division problems using known division facts and multiplicative relationships, eg 81 divided by 3 must have a quotient that is 3 times the size of 81 divided by 9 so 81 divided by 3 = 27	
		Dividing using factorising (the distributive property)	• solve division problems by splitting factors, eg 125 $\div$ 5 as (100 $\div$ 5) + (25 $\div$ 5)	
NA.C.4 Select and apply efficient mental and written strategies, and	2	Dividing up to a 4-digit number by a 2-digit divisor using the contracted algorithm, no remainders or zeroes in the answer	apply the written algorithm to divide up to a     4-digit number by a 2-digit number	
appropriate digital technologies, to solve problems involving multiplication and division with whole numbers		Dividing up to a 4-digit number by a 2-digit divisor using the division algorithm (extended/long)	apply the written extended (long) algorithm to divide up to a 4-digit number by a 2-digit number, with and without remainders, with and without zeros in the answer	
	3	Dividing up to a 4-digit number by a 2-digit divisor using the contracted algorithm, with remainders but without zeros in answers	apply the written algorithm to divide up to a 4-digit number by a 2-digit number, with remainders and without zeros in the answer	
	4	Dividing up to a 4-digit number by a 2-digit divisor using the contracted algorithm, with and without remainders and zeros in answers	apply the written algorithm to divide up to a 4-digit number by a 2-digit number, with and without remainders and zeros in the answer	
L	earning.	g Journeys Multiplication and div	ision word problems	
NA.C.4 Select and apply efficient mental and written strategies and	1	Solving word problems involving multiplication and division	use a table or similar organiser to record methods used to solve problems	
written strategies, and appropriate digital technologies, to solve problems involving multiplication and division with whole numbers	2	Introducing speed using metric units	solve simple problems involving speed	



## **Understanding Practice and Fluency (UPF)**

MA3-7NA compares, orders and calculates with fractions, decimals and percentages			
		Quest: (2) Mult/div & order of o	perations
	Lear	rning Journeys Order of operatio	ns - no brackets
Content Descriptor	Steps	Spine Nodes	Subnodes
NA 655 1 1	1	Introducing order of operations involving addition and subtraction	solve number sentences involving addition and subtraction
NA.C.5 Explore the use of brackets and the order of operations to write number sentences	2	Introducing order of operations involving multiplication and division	solve number sentences involving multiplication and division
namber sericers	3	Introducing order of operations involving all 4 operations	solve number sentences involving all 4 operations
	Learn	ing Journeys Order of operation	s using bracketsa
	1	Introducing order of operations involving grouping symbols	<ul> <li>explore the use of brackets and the order of operations in number sentences</li> <li>perform calculations involving grouping symbols without the use of digital technologies</li> </ul>
NA.C.5 Explore the use of brackets and the order	2	Applying order of operations for mixed operations and grouping symbols	apply the order of operations to perform calculations involving mixed operations and grouping symbols
of operations to write number sentences	3	Introducing order of operations involving multiple grouping symbols	perform calculations involving grouping symbols without the use of digital technologies
	4	Applying order of operations to real life contexts	<ul> <li>investigate and establish the order of operations using real-life contexts</li> <li>write number sentences to represent real-life situations</li> </ul>



## **Understanding Practice and Fluency (UPF)**

MA3-7NA co	mpares	, orders and calculates with fract	tions, decimals and percentages
		Quest: (1) Fractions, decimals, p	ercentages
L	earning	Journeys Compare and order co	ommon unit fractions
Content Descriptor	Steps	Spine Nodes	Subnodes
NA.D.1 Compare and order common unit fractions and locate and represent them on a number line	1	Comparing and ordering unit fractions with different denominators using models and diagrams	<ul> <li>compare and order common unit fractions using models and diagrams for support</li> <li>compare and order common fractions with different denominators (halves, thirds, quarters, fifths, sixths, sevenths, eighths)</li> </ul>
	2	Comparing unit fractions with different denominators (denominators of 2, 3, 4, 5, 6, 8, 10, 12)	<ul> <li>model, compare and order common unit fractions</li> <li>locate and represent unit fractions on a number line</li> <li>compare the relative value of unit fractions by placing them on a number line between 0 and 1</li> <li>compare using &lt;, &gt;, =</li> </ul>
	Learnir	ng Journeys Adding and subtracti	ing proper fractions
NA.D.2 Investigate strategies to solve problems involving addition and subtraction of fractions with the same denominator 3424135	1	Adding proper fractions with the same denominator (denominators 2, 3, 4, 5, 6, 7, 8)	add proper fractions with the same denominator
	2	Subtracting proper fractions with the same denominator (denominators 2, 3, 4, 5, 6, 7, 8)	subtract proper fractions with the same denominator
	3	Adding and subtracting proper fractions with the same denominator (denominators 2, 3, 4, 5, 6, 7, 8)	add and subtract proper fractions with the same denominator
	4	Adding a whole number and a proper fraction	add a whole number and a proper fraction
	5	Subtracting a proper fraction from a whole number	<ul> <li>use diagrams, and mental and written strategies, to subtract a unit fraction from any whole number including 1</li> </ul>
Lear	ning Jou	urneys Add & subtract fractions -	common denominators
NA.D.2 Investigate strategies to solve problems involving addition and subtraction of fractions with the same denominator 342413	1	Adding mixed numerals with the same denominator	add mixed numerals with the same denominator
	2	Subtracting mixed numerals with the same denominator	subtract mixed numerals with the same denominator
	3	Solving word problems involving both proper fractions and mixed numerals with the same denominator	solve word problems involving adding and subtracting fractions with the same denominator



## **Understanding Practice and Fluency (UPF)**

		Quest: (1) Fractions, decimals,	percentages
	Le	arning Journeys Place value us	ing thousandths
Content Descriptor	Steps	Spine Nodes	Subnodes
NA.D.3 Recognise that	1	Introducing decimal thousandths	<ul> <li>express thousandths as decimals</li> <li>interpret decimal notation for thousandths, eg 0.123 = 123/1000</li> <li>state the place value of digits in decimal numbers of up to 3 decimal places</li> </ul>
the place value system can be extended beyond hundredths	2	Partitioning decimal thousandths	<ul> <li>use place value to partition decimals of up to 3dp</li> <li>partition decimals of up to 3d.p. in non-standard forms</li> <li>partition fractions up to thousandths into decimals and fractions</li> </ul>
	Le	earning Journeys Compare and	order decimals
NA.D.4 Compare, order and represent decimals	1	Interpreting zeros at the end of a decimal	understand that a zero at the end of a decimal does not change its value
	2	Knowing common fraction and decimal equivalences	know fraction and decimal equivalences for thirds quarters, fifths and eighths
	3	Comparing and ordering decimal fractions of up to 3 decimal places	<ul> <li>place decimal numbers of up to 3 decimal places on a number line between 0 and 1</li> <li>compare and order decimals with 3 decimal place using &gt;, &lt; and =</li> <li>compare and order decimals with a different number of decimal places, up to 3 decimal places</li> </ul>
		Quest: (2) Fractions, decimals,	percentages
		<b>Learning Journeys</b> Working w	ith fractions
NA.D.5 Compare fractions with related denominators and locate and represent them on a number line	1	Comparing and ordering proper fractions with different numerators and denominators (denominators of 2, 3, 4, 5, 6, 8, 10, 12 and 100)	<ul> <li>compare and order proper fractions using a benchmark fraction for support, eg half or quarte</li> <li>record comparisons using &gt;, &lt; or = (reference for other subnodes)</li> </ul>
	2	Recognising and finding equivalent simple fractions with related denominators using multiplicative thinking (denominators of 2, 3, 4, 5, 6, 8, 10, 12 and 100)	<ul> <li>develop mental strategies for generating equivalent fractions, such as multiplying or dividing the numerator and the denominator by the same number</li> <li>apply knowledge of equivalent fractions to converse between units of measurement</li> </ul>
	3	Using common factors to simplify proper fractions to their simplest form	<ul> <li>determine a common factor of the numerator and denominator of a fractions and use to find an equivalent fraction. Repeat until the fraction is reduced to its simplest form</li> <li>write a fraction in its simplest form using the highest common factor</li> </ul>



## **Understanding Practice and Fluency (UPF)**

MA3-7NA co	mpares	, orders and calculates with frac	ctions, decimals and percentages		
	Quest: (2) Fractions, decimals, percentages				
Lear	ning Jo	urneys Add & subtract proper f	ractions - related denoms		
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Adding proper fractions with related denominators and answers less than 1 whole	add proper fractions where the denominators are related		
	2	Adding and subtracting simple proper fractions in which 1 denominator is a multiple of another (denominators 2, 3, 4, 5, 6, 7, 8, 10, 12, 100)	add and subtract proper fractions where 1 denominator is the same as, or a multiple of, the other		
NA.D.6 Solve problems involving addition and		Adding simple fractions with related denominators	add fractions where the denominators are related		
subtraction of fractions with the same or related denominators	3	Subtracting proper fractions with related denominators and answers less than 1 whole	subtract proper fractions where the denominators are related		
	4	Subtracting simple fractions with related denominators	subtract fractions where the denominators are related		
	5	Adding and subtracting proper fractions with related denominators and answers less than 1 whole	add and subtract proper fractions where the denominators are related		
Lear	ning Jo	urneys Add & subtract mixed n	umerals - related denoms		
	1	Adding fractions, including mixed numerals, with related denominators	add fractions, including mixed numerals, where the denominators are related		
NA.D.6 Solve problems involving addition and subtraction of fractions	2	Subtracting fractions, including mixed numerals, with related denominators	subtract fractions, including mixed numerals, where the denominators are related		
with the same or related denominators	3	Adding and subtracting fractions including mixed numerals, with related denominators	add and subtract fractions where the denominators are related		
	4	Solving word problems involving fractions and mixed numerals with the related denominators	solve word problems involving the addition and subtraction of fractions where 1 denominator is the same as, or a multiple of, the other		
	Lea	arning Journeys Finding a fracti	on of a quanitity		
NA D 7 Find a river la	1	Finding a simple fraction of a quantity with and without the use of digital technologies	calculate a simple fraction of a collection/quantity, with and without the use of digital technologies		
NA.D.7 Find a simple fraction of a quantity where the result is a whole number, with and without the use of digital technologies	2	Solving word problems involving non-unit fractions	<ul> <li>find the whole given the non-unit fraction of a set</li> <li>solve word problems in different contexts, eg measurement</li> <li>solve word problems involving fractions with different denominators eg 2/5 of the children</li> </ul>		
technologies			have blue eyes, 2/6 have green eyes, if there are 30 children altogether how many children have brown eyes?		



## **Understanding Practice and Fluency (UPF)**

MA3-7NA coi	mpares	orders and calculates with fra	ctions, decimals and percentages
		Quest: (2) Fractions, decimals,	percentages
		Learning Journeys Adding	decimals
Content Descriptor	Steps	Spine Nodes	Subnodes
NA.D.8 Add and subtract	1	Adding decimals to 2 decimal places using mental strategies	<ul> <li>select and apply efficient mental strategies to solve addition problems, including compensation, bridging to 1, using place value</li> <li>estimate sums</li> </ul>
decimals, with and without the use of digital technologies, and use estimation and	2	Adding decimals to 3 decimal places using mental strategies	select and apply efficient mental strategies to solve addition problems, including compensation, bridging to 1, using place value
rounding to check the reasonableness of answers	3	Adding decimals using digital technologies	add decimals using digital technologies
	4	Adding decimals using written method	<ul> <li>use a standard algorithm to add decimals with the same number of decimal places</li> <li>use a standard algorithm to add decimals with a different number of decimal places</li> </ul>
		Learning Journeys Subtracti	ng decimals
NA.D.8 Add and subtract	1	Subtracting decimals using mental strategies	select and apply efficient mental strategies to solve subtraction problems, including compensation, bridging to 1, using place value
decimals, with and without the use of	2	Subtracting decimals using digital technologies	subtract decimals using digital technologies
digital technologies, and use estimation and rounding to check the reasonableness of answers	3	Subtracting decimals using written method	use a standard algorithm to subtract decimals with the same number of decimal places     use a standard algorithm to subtract decimals
	4	Rounding decimal hundredths	<ul> <li>with a different number of decimal places</li> <li>round hundredths to the nearest whole number</li> <li>round hundredths to the nearest tenth</li> </ul>
		Learning Journeys Multiplyi	ng decimals
NA.D.9 Multiply decimals by whole numbers and perform divisions by non-zero whole numbers where the results are terminating decimals, with and without the use of	1	Multiplying decimals	<ul> <li>use mental strategies to multiply simple decimals by single-digit numbers, eg 3.5 × 2</li> <li>multiply decimals of up to 3 decimal places by whole numbers of up to 2 digits, with and without the use of digital technologies, eg 'I measured 3 desks. Each desk was 1.25 m in length, so the total length is 3 × 1.25 = 3.75 m'</li> </ul>
digital technologies	2	Multiplying decimals using written method	multiply decimals up to thousandths using a standard algorithm
		Learning Journeys Dividing	g decimals
NA.D.9 Multiply decimals by whole numbers and perform divisions by non-zero whole numbers where the results are terminating decimals, with and without the use of digital technologies	1	Dividing decimals	<ul> <li>divide decimals by a one-digit whole number where the result is a terminating decimal, eg 5.25 ÷ 5 = 1.05 9</li> </ul>
	2	Dividing decimals using written method	divide decimals up to thousandths using a standard algorithm



## **Understanding Practice and Fluency (UPF)**

MA3-7NA co	mpares,	orders and calculates with fra	ctions, decimals and percentages
		Quest: (2) Fractions, decimals,	percentages
Lear	ning Jou	rneys Multiplying and dividing	decimals by powers of 10
Content Descriptor	Steps	Spine Nodes	Subnodes
NA.D.10 Multiply and divide decimals by powers	1	Multiplying decimals by powers of 10	use PV equipment to multiply decimals by 10
of 10	2	Dividing decimals by powers of 10	• use PV equipment to divide decimals by 10
Lear	ning Joເ	rneys Representing fractions,	decimals and percentages
NA.D.11 Make connections between equivalent fractions, decimals and percentages	1	Introducing percentages	<ul> <li>write fractions with a denominator of 100 as percentages and vice versa</li> <li>find a percent of a quantity as a rate per 100, eg 30% of a quantity means 30/100 times the quantity</li> </ul>
	2	Representing percentages and decimals	<ul> <li>write decimals (&lt; 1) to 2 decimal places as percentages</li> <li>write decimals as percentages and vice versa</li> </ul>
	r	Representing simple fractions as percentages	represent simple fractions as percentages and vice versa
	3	Representing common fractions as percentages	represent common fractions as percentages and vice versa
Le	arning J	ourneys Fraction, decimal and	percentage equivalence
NA.D.11 Make connections between equivalent fractions, decimals and percentages	1	Investigating the relationships between fractions, decimals and percentages	<ul> <li>record relationships between decimals, percentages and fractions (with denominators 2, 4, 5, 10, 20, 25, 50, 100)</li> <li>demonstrate understanding using symbolic representation</li> </ul>
	2	Representing common equivalent fractions, decimals and percentages	<ul> <li>representation</li> <li>recall the relationships between decimals, percentages and fractions with denominators of 2, 4, 5, 10, 20, 25, 50 and 100</li> <li>recognise fractions, decimals and percentages as different representations of the same value</li> </ul>
	3	Representing equivalent fractions, decimals and percentages	<ul> <li>write percentages as fractions in their simplest form</li> <li>write fractions with denominators that are factors of 100 as percentages by multiplying the numerator and denominator by a common value</li> <li>write fractions with denominators that are not factors of 100 as percentages by writing as a decimal first, eg using short division, then x100 to write as a percentage</li> <li>write percentages as decimals and vice versa</li> </ul>
	4	Solving problems relating to percentage and decimal equivalence	• solve problems which require knowing percentage and decimal equivalents of ½, ¼, 1/5, 2/5, 4/5 and those fractions with a denominator or multiple of 10 or 25



## **Understanding Practice and Fluency (UPF)**

MA3-7NA co	mpares:	orders and calculates with fra	ctions, decimals and percentages
		Quest: (2) Fractions, decimals,	percentages
		Learning Journeys Calculating	percentages
Content Descriptor	Steps	Spine Nodes	Subnodes
	1	Converting common fractions to percentages using mental strategies	use mental strategies to convert fractions to percentages
	2	Converting common fractions to percentages using a calculator	use calculator strategies to convert fractions to percentages
	3	Calculating simple percentages	estimate 0%, 1%, 10%, 25%, 50% and 100% of an amount including examples in context (exclude discounts), explain estimation      selsulate 10%, 25% and 50% of an amount.
NA.D.12 Investigate and			• calculate 10%, 25% and 50% of an amount including examples in context (exclude discounts)
calculate percentage discounts of 10%, 25% and 50% on sale items, with			• investigate and calculate percentage discounts of 10%, 25% and 50% on sale items
and without the use of digital technologies	4	Calculating simple percentage discounts	• estimate quantities using benchmarks of 10%, 25% and 50%
			• calculate sale price by subtracting the proportion from the original amount
			calculate common percentages of quantities
	5	Calculating simple percentages of quantities	• equate 10% to 1/10, 25% to 1/4 and 50% to 1/2
			• use mental strategies to estimate discounts of 10%, 25% and 50
			<ul> <li>calculate the sale price of an item after a discount of 10%, 25% and 50%, recording the strategy and result</li> </ul>
MA3-8NA analyses a		tes geometric and number pat ences, and locates points on th	tterns, constructs and completes number le Cartesian plane
		Quest: (1) Number Pat	terns
Lo	earning	Journeys Number patterns - ac	ddition and subtraction
		Describing, continuing and creating patterns resulting	<ul> <li>identify, continue and create simple number patterns involving addition and subtraction including fractions</li> </ul>
NA.E.1 Describe, continue and create patterns with	1	from addition and subtraction including fractions	• describe patterns using the terms 'increase' and 'decrease', eg 'The terms decrease by 1/4'
fractions, decimals and whole numbers resulting from addition and subtraction			find missing terms in a number sequence
	2	Describing, continuing and creating patterns resulting	identify, continue and create simple number patterns involving addition and subtraction including decimals
	from addition and subtraction including decimals	• describe patterns using the terms 'increase' and 'decrease', eg for the pattern 4.8, 4.1, 3.4, 2.7,, 'The terms decrease by 0.7'	



## **Understanding Practice and Fluency (UPF)**

MA3-8NA analyses and creates geometric and number patterns, constructs and completes number sentences, and locates points on the Cartesian plane					
	Quest: (1) Number Patterns				
Lea	arning Jo	ourneys Number sentences -mi	ultiplication and division		
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA 5211 and the	1	Using equivalent number sentences that involve more than 1 operation to find unknown quantities	<ul> <li>complete number sentences that involve more than 1 operation by calculating missing numbers, eg 5 × □ = 4 × 10, 5 × □ = 30 − 10</li> </ul>		
NA.E.2 Use equivalent number sentences involving multiplication and division to find unknown quantities	2	Describing and using inverse operations to solve number sentences with whole numbers and any of the 4 operations	• identify and use inverse operations to assist with the solution of number sentences, eg 125 ÷ 5 = □ becomes □ × 5 = 125		
unknown quantities	3	Finding the missing number in multiplication and division number sentences involving simple fractions or decimals	<ul> <li>complete number sentences involving multiplication and division, including those involving simple fractions or decimals, eg 7 × □ = 7.7</li> </ul>		
		Quest: (2) Number Pat	terns		
L	earning	Journeys Continuing and creat	ing number sequences		
NA.E.3 Continue and create sequences involving whole numbers, fractions and decimals; describe the rule used to create the sequence	1	Continuing and creating sequences involving whole numbers, fractions and decimals	<ul> <li>describe the rule used to create the sequence</li> <li>continue and create number patterns, with and without the use of digital technologies, using whole numbers, fractions and decimals, eg 1/4, 1/8, 1/16, or 1.25, 2.5, 5,</li> <li>find missing terms in a number sequence</li> </ul>		
	Learning Journeys The Cartesian plane				
NA.E.4 Introduce the Cartesian coordinate system using all four quadrants	1	Locating points on the Cartesian plane	<ul> <li>plot and label points, given coordinates, in all 4 quadrants of the number plane</li> <li>identify and label each quadrant on a number plane</li> <li>identify and record the coordinates of given points in all 4 quadrants of the number plane</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA3-9MG selects and uses the appropriate unit and device to measure lengths and distances, calculates perimeters, and converts between units of length

perimeters, and converts between units of length				
Quest: (1) Length, distance, perimeter				
	Learnir	ng Journeys Comparing and ord	lering metric lengths	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Introducing formal units for length: kilometres	<ul> <li>recognise the need for a formal unit longer than the metre for measuring distance, eg distance between known places or visible landmarks</li> <li>recognise that there are 1000 m in 1 km, ie 1000 m = 1 km</li> <li>describe 1 m as one thousandth of a kilometre</li> <li>develop a personal reference for the approximate length of 1 km and half a kilometre</li> <li>record distances using the abbreviation for kilometres (km)</li> </ul>	
MG.A.1 Choose appropriate units of measurement for length	2	Comparing lengths in metres and kilometres	compare lengths and distances using metres and kilometres	
measurement for length	2	Ordering lengths in metres and kilometres	order lengths and distances using metres and kilometres	
	3	Comparing lengths in millimetres, centimetres, metres and kilometres	compare lengths and distances using millimetres, centimetres, metres and kilometres	
		Ordering lengths in millimetres, centimetres, metres and kilometres	order lengths and distances using millimetres, centimetres, metres and kilometres	
	4	Recording lengths using mixed units	record lengths and distances using combinations of millimetres, centimetres, metres and kilometres	
	Learı	ning Journeys Calculating perin	neter of rectangles	
MG.A.2 Calculate the	1	Calculating the perimeters of rectangles	explore different methods of finding the perimeter of rectangles	
perimeters of rectangles using familiar metric units	2	Calculating the side length of a rectangle given the perimeter	<ul> <li>find the length of 1 unknown side of a rectangle given the perimeter</li> <li>find possible length combinations of 2 unknown sides of a rectangle given the perimeter</li> </ul>	
		Quest: (2) Length, distance,	perimeter	
	Learnin	g Journeys Decimal notation a	nd the metric system	
MC A 2 Connect desired	1	Recording kilometres and metres using decimal notation	record lengths and distances using decimal notation to 3 decimal places	
MG.A.3 Connect decimal representations to the metric system 3424348	2	Connecting decimal representations to the metric system	<ul> <li>recognise the equivalence of whole-number and decimal representations of measurements of length</li> <li>interpret decimal notation for lengths and distances involving millimetres, centimetres, metres and kilometres</li> </ul>	



## **Understanding Practice and Fluency (UPF)**

		rimeters, and converts between	o measure lengths and distances, calculates n units of length
		Quest: (1) Length, distance,	perimeter
L	earning	Journeys Converting standard	metric units of length
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.A.4 Convert between common metric units of	1	Converting between standard metric units of length to 1 decimal place	<ul> <li>convert between centimetres and metres and vice versa</li> <li>convert between centimetres and millimetres and vice versa</li> <li>convert between metres and kilometres and vice versa</li> <li>convert among millimetres, centimetres, metres and kilometres</li> </ul>
length	2	Converting between common metric units of length up to 2 decimal places	<ul> <li>convert between metres and kilometres</li> <li>convert between millimetres, centimetres and metres to compare lengths and distances</li> </ul>
	3	Converting between common metric units of length up to 3 decimal places	<ul> <li>convert between metres and kilometres</li> <li>convert between millimetres, centimetres and metres to compare lengths and distances</li> </ul>
		Learning Journeys Length	problems
MG.A.5 Solve problems involving the comparison of lengths using appropriate units	1	Solving one-step problems involving length	solve a variety of one-step problems involving length and perimeter, including different units of length
	2	Solving two-step problems involving length	solve a variety of two-step problems involving length and perimeter, including different units of length
MA3-10MG selects and	uses the		areas, including areas of squares, rectangles
		and triangles  Quest: (1) Calculating	2102
	o a renier		
MG.B.1 Choose appropriate units of measurement for area	_earning	Introducing formal units for area: square kilometres and hectares	<ul> <li>measure the dimensions of a large rectangular piece of land and calculate its area in hectares, eg school playground or local park</li> <li>relate one square kilometre and one hectare to known standard areas such as sports fields, courts and tracks of land</li> <li>determine side lengths of different rectangles with area of one hectare, eg 200 metres by 50 metres</li> <li>identify everyday situations where square kilometres or hectares are an appropriate unit for</li> </ul>
	l ear	rning Journeys Calculating the	measuring the area
MG.B.2 Calculate the areas of rectangles using familiar metric units	1	Developing a multiplicative formula for area of a rectangle using metric units	<ul> <li>calculate the area of a rectangle by multiplying the length and width of the rectangle</li> <li>calculate a side length of the rectangle given its area and one other side length</li> </ul>



## **Understanding Practice and Fluency (UPF)**

MA3-10MG selects and	uses the	e appropriate unit to calculate and triangles	areas, including areas of squares, rectangles
		Quest: (2) Calculating	area
	Lea	rning Journeys Calculating the	area of triangles
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.B.3 Solve problems	1	Calculating area of a right-angled triangle without a formula	<ul> <li>calculate the area of right-angled triangles using the relationship that the area is half the area of a rectangle with the same base and perpendicular height</li> <li>calculate the area of right-angled triangles where all three side lengths are given, using the relationship that the area is half the area of a rectangle with the same base and perpendicular height</li> </ul>
involving the comparison of areas using appropriate units	2	Calculating area of any triangle	calculate the area of triangles where more dimensions than are necessary are given, using the relationship that the area is half the area of a rectangle with the same base and perpendicular height
	3	Applying the formula for the area of a rectangle	<ul> <li>apply the formula for area of a rectangle to find the area of rectangles given 2 side lengths measured in the same or different units</li> <li>apply the formula for area of a rectangle to find the area of composite rectilinear figures, such as an L-shape, U-shape</li> </ul>
MA3-11MG selects a		s the appropriate unit to estima pacities, and converts between	ate, measure and calculate volumes and units of capacity
		Quest: (1) Calculating volume	e & capacity
		Learning Journeys Measuri	ng volume
	1	Selecting and justifying appropriate metric units to measure volume and capacity (ml and l)	<ul> <li>select and use appropriate units to measure the capacities of a variety of containers</li> <li>select and use appropriate units to estimate the volumes of a variety of objects</li> </ul>
MG.C.1 Choose appropriate units of measurement for volume and capacity	2	Introducing formal units for volume: cubic metres	<ul> <li>recognise the need for a formal unit larger than the cubic centimetre</li> <li>construct and use the cubic metre as a unit to measure larger volumes</li> <li>explain why volume is measured in cubic metres in certain situations, eg wood bark, soil or concrete; select and justify referents for cubic cm</li> <li>recognise that a cubic metre can have dimensions other than a cube of side 1 metre</li> <li>record volumes using the abbreviation for cubic metres (m^3)</li> <li>estimate the size of a cubic metre, half a cubic metre and 2 cubic metres</li> </ul>



### **Understanding Practice and Fluency (UPF)**

MA3-11MG selects and uses the appropriate unit to estimate, measure and calculate volumes and capacities, and converts between units of capacity			
Quest: (2) Calculating volume & capacity			
Learning Journeys Volume and capacity			
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.C.2 Connect volume and capacity and their units of measurement	1	Connecting volume and capacity	<ul> <li>select the appropriate unit to measure volume and capacity</li> <li>demonstrate that a cube of side 10 centimetre will displace 1 litre of water</li> <li>demonstrate, by using a medicine cup, that a cube of side 1 centimetre will displace 1 millilitres of water</li> <li>equate 1 cubic centimetre to 1 millilitre and 1000 cubic centimetres to 1 litre</li> <li>find the volumes of irregular solids in cubic centimetres using a displacement strategy</li> </ul>
Learning Journeys Decimal representation in capacity			
MG.C.3 Connect decimal representations to the metric system	1	Connecting decimal representations to the metric systems (to 3 decimal places)	<ul> <li>recognise the equivalence of whole-number and decimal representations of measurements of capacities</li> <li>interpret decimal notation for volumes and capacities</li> <li>record volume and capacity using decimal notation to 3 decimal places</li> </ul>
Learning Journeys Converting common units of capacity			
MG.C.4 Convert between common metric units of capacity	1	Converting between common metric units of capacity including fractions and decimals (to 2 decimal places)	<ul> <li>convert between millilitres and litres using fractions eg 1 and 1/10 litres as 1100 ml or 3.8 l as 3800 ml</li> <li>explain and use the relationship between the size of a unit and the number of units needed to assist in determining whether multiplication or division is required when converting between units</li> </ul>
	2	Converting between common metric units of capacity (to 3 decimal places)	<ul> <li>convert between millilitres and litres</li> <li>explain and use the relationship between the size of a unit and the number of units needed to assist in determining whether multiplication or division is required when converting between units</li> </ul>
Learning Journeys Volume of rectangular prisms			
MG.C.5 Calculate the volumes of rectangular prisms	1	Calculating the volumes of rectangular prisms using additive and multiplicative strategies	<ul> <li>describe rectangular prisms in terms of layers</li> <li>use repeated addition to find the volumes of rectangular prisms</li> <li>establish the relationship between the number of cubes in 1 layer, the number of layers, and the volume of a rectangular prism</li> <li>explain that the volume of a rectangular prism can be found by finding the number of cubes in 1 layer and multiplying by the number of layers</li> <li>record, using words, the method for finding the volumes of rectangular prisms</li> <li>calculate the volumes of rectangular prisms in cubic centimetres and cubic metres including calculating the volume given the net for the shape</li> <li>record calculations used to find the volumes of rectangular prisms</li> </ul>



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA3-12MG selects and uses the appropriate unit and device to measure the masses of objects, and converts between units of mass

converts between units of mass						
Quest: (1) Measure & convert mass						
Learning Journeys Working with mass						
Content Descriptor	Steps	Spine Nodes	Subnodes			
MG.D.1 Choose appropriate units of measurement for mass	1	Introducing formal units for mass: the tonne	<ul> <li>establish the need for formal units for very large masses and introduce tonnes, including that 1000 kg = 1 tonne</li> <li>identify everyday situations where tonnes are an appropriate unit for measuring the mass</li> <li>apply place value understanding to modelling, describing and recording metric units of measurement</li> <li>introduce the abbreviation 't' for recording mass in tonnes and record masses using tonnes and kilograms, eg 1 t 750 kg</li> <li>calculate the number of kilograms in a whole number of tonnes</li> <li>interpret simple fractions (¼, ½, ¾) of a tonne and relate these to the number of kilograms</li> </ul>			
	2	Selecting and using the appropriate metric unit and device to measure mass	select and use the appropriate metric unit and device to measure mass			
	3	Recognising gross mass and net mass	select and use the appropriate customary unit and device to measure mass			
	4	Solving multi-step problems involving mass	solve a variety of problems involving masses of the same unit			
		Quest: (2) Measu	re & convert mass			
		Learning Journeys Decim	nal representation in mass			
MG.D.2 Connect decimal representations to the metric system	Understanding decimal 1 representation of metric measurements of mass		<ul> <li>connect measurements of mass with their decimal representations</li> <li>recognise the equivalence of whole number and decimal representations, eg 3 kg 250 g = 3.25 kg</li> <li>record mass using decimal notation of up to 3 decimal places</li> <li>refer to SI units of mass</li> </ul>			
		Learning Journeys Co	nverting units of mass			
MG.D.3 Convert between common metric units of mass		Converting between standard metric units of mass to 1 decimal place	<ul> <li>understand the meaning of metric prefixes, eg kilo-, centi-, milli-</li> <li>convert between grams and kilograms and vice versa</li> <li>convert between kilograms and tonnes and vice versa</li> <li>convert among grams, kilograms and tonnes</li> </ul>			
	1	Converting between standard metric units of mass up to 2 decimal places	<ul> <li>understand the meaning of metric prefixes, eg kilo-, centi-, milli-</li> <li>convert between grams and kilograms and vice versa</li> <li>convert between kilograms and tonnes and vice versa</li> <li>convert among grams, kilograms and tonnes</li> </ul>			
		Converting between standard metric units of mass up to 3 decimal places	<ul> <li>understand the meaning of metric prefixes, eg kilo-, centi-, milli-</li> <li>convert between grams and kilograms and vice versa</li> <li>convert between kilograms and tonnes and vice versa</li> <li>convert among grams, kilograms and tonnes</li> <li>solve problems using diffeent units of mass</li> </ul>			



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA3-13MG uses	24-hou	r time and am and pm ı	notation in real-life situations, and constructs timelines
		Quest: (1) 24-l	hour time & timelines
		Learning Journ	eys Using 24-hour time
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.E.1 Compare 12- and 24-hour time systems and convert between them	1	Using 24-hour notation	<ul> <li>convert between 24-hour time notation and 12-hour time notation</li> <li>convert between analogue and 24-hour digital clocks</li> <li>record 24-hour time using necessary conventions</li> </ul>
		Learning Journeys	Understanding elapsed time
MG.E.2 Determine and compare the duration of event	1	Calculating elapsed time	solve problems involving elapsed time given the starting or finishing time
		Quest: (2) 24-	hour time & timelines
		Learning Jour	neys Using timetables
MG.E.3 Interpret and use timetables	1	Using timetables (12- hour and 24-hour time)	<ul> <li>use real-world timetables (12-hour and 24-hour time) to determine arrival time given the desired departure time, including when the departure time is not listed exactly in the timetable</li> <li>use real-world timetables (12-hour and 24-hour time) to determine departure time given the desired arrival time, including when the arrival time is not listed exactly in the timetable</li> <li>use real-world timetables (12-hour and 24-hour time) to determine the duration of a journey</li> </ul>
			solve real-world problems involving timetables
		Learning J	ourneys Timelines
MG.E.4 Draw and interpret timelines using a given scale	1	Introducing timelines	• interpret the sequence of events on a timeline (understanding of scale not expected)
			ts, including prisms and pyramids, on the basis of their constructs them given drawings of different views
		Quest: (1) Pro	perties of 3D objects
		Learning Journe	eys Prisms and pyramids
MG.F.1 Compare, describe and name	1	Comparing, describing and naming prisms	<ul> <li>identify and determine the number of pairs of parallel faces of three-dimensional objects, eg 'A rectangular prism has three pairs of parallel faces'</li> <li>identify the 'base' of prisms</li> <li>recognise that the base of a prism is not always the face where the prism touches the ground</li> <li>name prisms according to the shape of their base, eg rectangular prism</li> <li>recognise a cube as a special type of prism</li> </ul>
prisms and pyramids	2	Comparing, describing and naming pyramids	<ul> <li>identify and determine the number of pairs of parallel faces of three-dimensional objects</li> <li>identify the 'base' of pyramids</li> <li>recognise that the base of a pyramid is not always the face where the prism touches the groun</li> <li>name pyramids according to the shape of their base, eg square pyramid</li> </ul>



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA3-14MG identifies three-dimensional objects, including prisms and pyramids, on the basis of their properties, and visualises, sketches and constructs them given drawings of different views

Quest: (1) Properties of 3D objects				
Learning Journeys Prisms and pyramids				
Content Descriptor	Steps	Spine Nodes	Subnodes	
MG.F.1 Compare, describe and name prisms and pyramids	3	Investigating cross- sections of prisms and pyramids	<ul> <li>recognise that prisms have a 'uniform cross-section' when the section is parallel to the base</li> <li>recognise that the base of a prism is identical to the uniform cross-section of the prism</li> <li>recognise that pyramids do not have a uniform cross-section when the section is parallel to the base</li> </ul>	
	4	Investigating properties of prisms and pyramids	<ul> <li>identify, describe and compare the properties of prisms and pyramids, including: number of faces, shape of faces, number and type of identical faces, number of vertices, number of edges</li> <li>describe similarities and differences between prisms and pyramids, eg between a triangular prism and a hexagonal prism, between a rectangular prism and a rectangular(-based) pyramid</li> <li>determine that the faces of prisms are always rectangles except the base faces, which may not be rectangles</li> <li>determine that the faces of pyramids are always triangles except the base face, which may not be a triangle</li> <li>use the term 'apex' to describe the highest point above the base of a pyramid or cone</li> </ul>	
		Learı	ning Journeys Nets	
MG.F.2 Connect three-dimensional objects with their nets and other two-dimensional representations	1	Connecting three- dimensional objects with two-dimensional representations	<ul> <li>visualise and sketch three-dimensional objects from different views, including top, front and side views</li> <li>reflect on their own drawing of a three-dimensional object and consider how it can be improved</li> <li>show simple perspective in drawings by showing depth</li> </ul>	
	2	Connecting prisms and pyramids with their nets	<ul> <li>examine a diagram to determine whether it is or is not the net of a prism or pyramid</li> <li>explain why a given net will not form a prism or pyramid</li> <li>visualise and sketch nets for a given prism or pyramid</li> <li>recognise whether a diagram is a net of a particular prism or pyramid</li> <li>visualise and name prisms and pyramids, given diagrams of their nets</li> <li>select the correct diagram of a net for a given prism or pyramid from a group of similar diagrams where the others are not valid nets of the object</li> </ul>	
	3	Connecting three- dimensional objects with their nets	<ul> <li>examine a diagram to determine whether it is or is not the net of a closed three-dimensional object</li> <li>explain why a given net will not form a closed three-dimensional object</li> <li>visualise and sketch nets for given three-dimensional objects</li> <li>recognise whether a diagram is a net of a particular three-dimensional object</li> <li>visualise and name prisms and pyramids, given diagrams of their nets</li> <li>select the correct diagram of a net for a given prism or pyramid from a group of similar diagrams where the others are not valid nets of the object</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA3-14MG identifies three-dimensional objects, including prisms and pyramids, on the basis of their properties, and visualises, sketches and constructs them given drawings of different views					
Quest: (2) Properties of 3D objects					
	Learning Journeys Constructing prisms and pyramids				
Content Descriptor	Steps	Spine Nodes	Subnodes		
MG.F.3 Construct simple prisms and	1	Constructing simple right prisms	<ul> <li>create prisms using a variety of materials, eg plasticine, paper or cardboard nets, connecting cubes</li> <li>create skeletal models of prisms, eg using toothpicks and modelling clay or straws and tape</li> <li>connect the edges of prisms with the construction of their skeletal models</li> <li>construct three-dimensional models of prisms and sketch the front, side and top views</li> <li>describe to another student how to construct or draw a prism</li> <li>construct three-dimensional models of prisms, given drawings of different views</li> </ul>		
pyramids	2	Constructing simple pyramids	<ul> <li>create pyramids using a variety of materials</li> <li>create skeletal models of pyramids</li> <li>connect the edges of pyramids with the construction of their skeletal models</li> <li>construct three-dimensional models of pyramids and sketch the front, side and top views</li> <li>describe to another student how to construct or draw a pyramid</li> <li>construct three-dimensional models of pyramids, given drawings of different views</li> </ul>		
MA3-15MG manipu	ılates, c		wo-dimensional shapes, including equilateral, isosceles and , and describes their properties		
			Properties of 2D shapes		
		Learning Jou	rneys Classifying 2D shapes		
MG.G.1 Classify two- dimensional shapes and describe their features	1	Classifying triangles by their sides and angles	<ul> <li>identify and name right-angled, equilateral, isosceles and scalene triangles</li> <li>compare and describe features of the sides of equilateral, isosceles and scalene triangles</li> <li>identify triangles that are right-angled as well as scalene or isosceles</li> <li>explore, by measurement, side and angle properties of equilateral, isosceles and scalene triangles</li> </ul>		
	2	Classifying quadrilaterals by their features	<ul> <li>explore, by measurement angle properties of squares, rectangles, parallelograms and rhombuses</li> <li>select and classify a two-dimensional shape from a description of its features including parallel and perpendicular lines</li> <li>recognise that two-dimensional shapes can be classified in more than 1 way</li> <li>explain the difference between regular and irregular shapes</li> </ul>		
	3	Classifying quadrilaterals using a variety of strategies	<ul> <li>classify two-dimensional figures in a hierarchy based on properties</li> <li>interpret a hierarchy diagram of two-dimensional shapes and their properties</li> <li>use Venn diagrams to record classifications</li> <li>interpret classifications represented using Venn diagrams</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA3-15MG manipulates, classifies and draws two-dimensional shapes, including equilateral, isosceles and scalene triangles, and describes their properties

scalene triangles, and describes their properties					
Quest: (1) Properties of 2D shapes					
Learning Journeys Drawing 2D shapes					
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Drawing triangles	<ul> <li>draw triangles from descriptions of their side and angle properties</li> <li>use tools such as templates, rulers, set squares and protractors to draw triangles</li> <li>use computer drawing tools to construct a triangle from a description of its side and angle properties</li> </ul>		
MG.G.1 Classify two- dimensional shapes and describe their features	2	Drawing quadrilaterals	<ul> <li>draw quadrilaterals from descriptions of their side and angle properties; use conventional markings for parallel sides and right angles</li> <li>use tools such as templates, rulers, set squares and protractors to draw quadrilaterals</li> <li>use computer drawing tools to construct a quadrilateral from a description of its side and angle properties</li> </ul>		
	3	Drawing regular and irregular two- dimensional shapes	<ul> <li>draw regular and irregular two-dimensional shapes from descriptions of their side and angle properties</li> <li>use conventional markings for parallel sides and right angles</li> <li>use tools such as templates, rulers, set squares and protractors to draw regular and irregular two-dimensional shapes</li> <li>use computer drawing tools to construct a shape from a description of its side and angle properties</li> </ul>		
		Learning Jour	rneys Rigid transformations		
MG.G.2 Describe translations, reflections and rotations of two- dimensional shapes	1	Defining transformations: One-step translations, reflections and rotations	<ul> <li>define translations, reflections and rotations of shapes and describe the similarities and differences between the original shape and the transformed shape</li> <li>identify the one-step transformation used to move a shape from 1 position to another</li> </ul>		
		Learnin	g Journeys Symmetry		
MG.G.3 Identify line and rotational symmetries	1	Drawing lines of symmetry on given designs and shapes	<ul> <li>recognise that some designs and shapes may have more than 1 line of symmetry</li> <li>identify and draw all lines of symmetry on designs and shapes</li> <li>determine the total number of lines of symmetry on designs and shapes</li> <li>determine whether or not a given line through designs and shapes is a line of symmetry</li> </ul>		
	2	Recognising rotational symmetry in shapes and designs	<ul> <li>establish and define that rotational symmetry occurs when a shape looks identical to the original after being turned less than a full turn</li> <li>determine whether or not given shapes and designs have rotational symmetry</li> <li>sort shapes according to whether they are rotationally symmetrical or not</li> </ul>		
	3	Ordering of rotational symmetry	<ul> <li>define the order of rotational symmetry as the number of times the shape looks identical to the original as it rotates around the centre of symmetry</li> <li>determine the order of rotational symmetry for given shapes and designs</li> <li>compare order of rotational symmetry for odd and even sided regular polygons</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA3-15MG manipulates, classifies and draws two-dimensional shapes, including equilateral, isosceles and

MA3-15MG manipulates, classifies and draws two-dimensional shapes, including equilateral, isosceles and scalene triangles, and describes their properties				
Quest: (1) Properties of 2D shapes				
		Learning Jou	rneys Enlarging 2D shapes	
Content Descriptor	Steps	Spine Nodes	Subnodes	
MG.G.4 Apply the enlargement transformation to familiar two-dimensional shapes and explore the properties of the resulting image compared with the original	1	Enlarging 2D shapes	<ul> <li>enlarge a simple 2D shape using a centre of enlargement and a simple scale factor, eg 2, 3, 4, 5, 10</li> <li>recognise the simple scale factor used in an enlargement of a 2D shape.</li> </ul>	
		Quest: (2)	Properties of 2D shapes	
		Learning Jour	neys Diagonals of 2D shapes	
MG.G.5 Investigate the diagonals of two- dimensional shapes	1	Investigating diagonals of special quadrilaterals	<ul> <li>identify and name 'diagonals' of special quadrilaterals</li> <li>recognise the endpoints of the diagonals of a quadrilateral as the vertices of the shape</li> <li>determine and draw all the diagonals of quadrilaterals</li> <li>compare and describe diagonals of different quadrilaterals</li> <li>use measurement to determine which of the special quadrilaterals have diagonals that are equal in length</li> <li>determine whether any of the diagonals of a particular shape are also lines (axes) of symmetry of the shape</li> </ul>	
		Learn	ing Journeys Circles	
MG.G.5 Investigate the diagonals of two- dimensional shapes	1	Investigating diagonals of special quadrilaterals	<ul> <li>identify and name 'diagonals' of special quadrilaterals</li> <li>recognise the endpoints of the diagonals of a quadrilateral as the vertices of the shape</li> <li>determine and draw all the diagonals of quadrilaterals</li> <li>compare and describe diagonals of different quadrilaterals</li> <li>use measurement to determine which of the special quadrilaterals have diagonals that are equal in length</li> <li>determine whether any of the diagonals of a particular shape are also lines (axes) of symmetry of the shape</li> </ul>	
		Learning Jour	rneys Rigid transformations	
MG.G.7 Investigate combinations of translations, reflections and rotations, with and without the use of digital technologies	1	Creating patterns that result from rotating shapes	<ul> <li>extend and create repeating patterns that result from rotations, through investigation using a variety of tools, eg pattern blocks, dynamic geometry software, geoboards, dot paper</li> <li>describe the pattern</li> <li>predict the next term/s in the pattern</li> </ul>	
	2	Creating patterns that result from translations	<ul> <li>extend and create repeating patterns that result from translations through investigation using a variety of tools, eg pattern blocks, dynamic geometry software, dot paper</li> <li>describe the pattern</li> <li>predict the next term/s in the pattern</li> </ul>	
	3	Identifying combinations of transformations	<ul> <li>classify two-dimensional figures in a hierarchy based on properties</li> <li>interpret a hierarchy diagram of two-dimensional shapes and their properties</li> <li>use Venn diagrams to record classifications</li> <li>interpret classifications represented using Venn diagrams</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA3-16MC mea	asures a	nd constructs angles	s, and applies angle relationships to find unknown angles
		Quest: (1) Ar	ngles & angle relationships
		Learning Journeys	Identifying and measuring angles
Content Descriptor	Steps	Spine Nodes	Subnodes
	1	Identifying hidden angles	<ul> <li>identify angles in everyday situations where one arm of the angle is not visible, eg the angle of the door to the frame where one arm is the imaginary line across the bottom of the doorway</li> <li>identify angles in everyday situations where both arms are not visible, eg a ball rebounding on a billiard table</li> </ul>
MG.H.1 Estimate, measure and compare angles using degrees	2	Introducing formal units for measuring angles	establish the need for a formal unit to measure angles and introduce the degree and its symbol (°)
	3	Measuring and estimating angles of up to 180° in degrees	<ul> <li>measure angles of up to 180° using a protractor</li> <li>estimate angles of up to 180° and check by measuring</li> <li>measure angles of up to 360° using a protractor</li> <li>estimate angles of up to 360° and check by measuring</li> </ul>
		Learning Journeys	Constructing and classifying angles
MG.H.2 Construct angles using a	1	Classifying angles by their size in degrees	<ul> <li>connect the term 'right angle' with 90°, 'straight angle' with 180° and 'angle of revolution' with 360°</li> <li>establish and recall the angle size in degrees for each of the classifications: acute, obtuse and reflex</li> <li>classify angles with a specified size in degrees as acute, right, obtuse, straight, reflex or a revolution</li> </ul>
protractor	2	Constructing angles	<ul> <li>draw angles that are acute, right, obtuse, straight, reflex or a revolution using a ruler only</li> <li>sketch angles of a specified size up to 360°</li> </ul>
			• use a protractor to construct angles of up to 360° accurately
		Quest: (2) Ar	ngles & angle relationships
	L	earning Journeys Ac	ljacent and vertically opposite angles
	1	Introducing adjacent angles	<ul> <li>define adjacent angles as angles that share a common arm and a common vertex and recognise the larger angle created</li> <li>recognise adjacent angles as additive and calculate the size of an unknown angle given the whole and its other parts and find the size of the whole given the size of the parts</li> </ul>
MG.H.3 Investigate, with and without	2	Exploring adjacent angles that form a right angle	<ul> <li>explore the relationship between angles that form a right angle</li> <li>calculate an unknown angle within a right angle given the other parts</li> </ul>
the use of digital technologies, angles on a straight line, angles at a point, and vertically opposite angles; use the results to find unknown angles	3	Exploring adjacent angles that form a straight angle	<ul> <li>explore the relationship between angles that form a straight angle</li> <li>calculate an unknown angle within a straight angle given the other parts</li> </ul>
	4	Exploring adjacent angles that form an angle of revolution	<ul> <li>explore the relationship between angles that form an angle of revolution</li> <li>calculate an unknown angle within an angle of revolution given the other parts</li> </ul>
	5	Exploring vertically opposite angles	<ul> <li>explore the relationship between angles formed when 2 straight lines intersect and identify these as 'vertically opposite angles'</li> <li>use the equality of vertically opposite angles to find the size of unknown angles in diagrams</li> <li>use the equality of vertically opposite angles to find the size of unknown angles represented by variables in diagrams</li> </ul>



## **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA3-17MG locates and describes position on maps using a grid-reference system			
			Maps & grid references
		Learning Jour	neys Grid-referenced maps
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.I.1 Use a grid-	1	Interpreting grid referenced maps	<ul> <li>establish that grid referencing on maps allows for more accurate description of features/locations</li> <li>understand the structure (letter then number, horizontal then vertical) and meaning of grid references (everything in that grid square)</li> <li>use grid references to describe features/locations on maps</li> <li>identify features/locations on maps given their gird reference</li> </ul>
reference system to describe locations	2	Creating grid referenced maps	draw grid referenced maps of familiar locations such as the classroom, school or local area
		referenced maps	<ul> <li>use technology to create grid referenced maps of familiar locations such as the classroom, school or local area</li> </ul>
	3	Drawing pathways on	• draw a path from 1 feature to another on a grid referenced map given the grid reference of each feature
		grid referenced maps	• use grid references to describe a path from 1 feature to another on a grid referenced map
	Lea	arning Journeys Usir	ng landmarks and directional language
MG.I.2 Describe routes using landmarks and directional language	1	Introducing intercardinal compass directions	<ul> <li>understand, locate and label the 4 intercardinal compass directions on a compass rose: north-east (NE), south-east (SE), south-west (SW) and north-west (NW)</li> <li>connect the 4 intercardinal compass directions to features of the local area from their particular location</li> <li>determine the direction of other cardinal and intercardinal compass directions when given one of the cardinal or intercardinal compass directions</li> </ul>
	2	Describing locations on maps using cardinal and intercardinal compass directions	use the cardinal and intercardinal compass directions to describe the location of one feature in relation to another on a map that has an arrow representing north
	3	Following and giving directions involving cardinal and intercardinal compass directions	<ul> <li>follow a sequence of 2 or more directions to find a location within a safe zone of the school</li> <li>give a sequence of 2 or more directions for a another person to find a location within a safe zone of the school</li> </ul>
	4	Drawing routes on maps using cardinal and intercardinal compass directions	<ul> <li>draw a route on a map given a sequence of directions involving cardinal and intercardinal directions, and landmarks</li> <li>use cardinal and intercardinal directions, and landmarks, to describe a route between 2 locations on a map</li> </ul>
		Quest: (2)	Maps & grid references
	Le	arning Journeys NO	INFO - BOTH SECTIONS ARE IN PART 1



### **Understanding Practice and Fluency (UPF)**

#### **Statsitics and Probability**

MA3-18SP uses appropriate methods to collect data and constructs, interprets and evaluates data displays, including dot plots, line graphs and two-way tables

including dot plots, line graphs and two-way tables				
Quest: (1) Data investigations				
		Learning Journe	eys Categorical and numerical data	
Content Descriptor	Steps	Spine Nodes	Subnodes	
SP.A.1 Pose questions and collect categorical or numerical data by observation or survey	1	Conducting surveys to obtain category and numerical data	<ul> <li>pose and refine questions to construct a survey to obtain categorical and numerical data about a matter of interes</li> <li>collect categorical and numerical data through observation or by conducting surveys</li> <li>sort category and numerical data and display in a table</li> </ul>	
	2	Conducting a statistical investigation using discrete or continuous data	<ul> <li>ask and investigate statistical questions that may require sampling; demonstrate an understanding that sets of data may be samples of a larger population</li> <li>distinguish between discrete data and continuous data</li> <li>collect data by conducting a survey or an experiment to do with themselves, their environment, issues in their school or community, or content from another subject, and record observations or measurements</li> <li>organise discrete or continuous data and display the data in charts, tables, and graphs that have appropriate titles, labels and scales that suit the range and distribution of the data</li> </ul>	
		<b>Learning Jour</b>	neys Constructing data displays	
SP.A.2 Construct displays, including column graphs, dot plots and tables, appropriate for data type, with and without the use of digital echnologies	1	Constructing a line graph using a scale of many-to-one correspondence	<ul> <li>construct a line graph using a scale of many-to-one correspondence, with and without the use of digital technologies</li> <li>name and label the horizontal and vertical axes when constructing graphs</li> <li>choose an appropriate title to describe the data represented in a data display</li> <li>determine an appropriate scale of many-to-one correspondence to represent the data in a data display</li> <li>mark equal spaces on the axes when constructing graphs, and use the scale to label the markers</li> <li>interpret data in line graph representing primary data; ask and answer questions related to the data in the display; draw conclusions</li> </ul>	
	2	Constructing a dot plot	<ul> <li>represent numerical data in a dot plot</li> <li>interpret data in a dot plot; ask and answer questions related to the data in the display; draw conclusions</li> </ul>	
	3	Choosing appropriate data displays	<ul> <li>consider the data type to determine and draw the most appropriate display(s), such as column graphs, dot plots and line graphs</li> <li>discuss and justify the choice of data display used</li> <li>recognise that line graphs are used to represent data that demonstrates continuous change</li> <li>recognise which types of data display are most appropriate to represent categorical data</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

#### **Statsitics and Probability**

MA3-18SP uses appropriate methods to collect data and constructs, interprets and evaluates data displays, including dot plots, line graphs and two-way tables

including dot plots, line graphs and two-way tables				
Quest: (1) Data investigations				
Learning Journeys Describing and interpreting data sets				
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Interpreting primary and secondary data in a column graph with many-to-one correspondence	<ul> <li>describe and interpret data presented in column graphs; ask and answer questions related to data in a column graph</li> <li>determine the total number of data values represented in column graphs</li> <li>identify and describe relationships that can be observed in a column graph; compare column graphs with other data displays</li> </ul>	
SP.A.3 Describe and interpret different data sets in context	2	Interpreting primary and secondary data in a line graph	<ul> <li>interpret line graphs using the scales on the axe</li> <li>describe and interpret data presented in line graphs</li> <li>identify and describe relationships that can be observed in data displays</li> </ul>	
	3	Reading and interpreting data in a dot plot	<ul> <li>describe and interpret data in a dot plot; ask and answer questions related to the data in the display; draw conclusions</li> <li>determine the total number of data values represented in dot plots</li> <li>identify and describe relationships that can be observed in data displays</li> <li>compare dot plots to other types of displays</li> </ul>	
	4	Interpreting data and solving problems using data in tables	<ul> <li>describe and interpret data presented in tables, eg maximum and minimum values; total number of responses; differences between values</li> <li>identify and describe relationships; draw conclusions and ask questions</li> </ul>	
		Quest	t: (2) Data investigations	
		Learning	g <b>Journeys</b> Two-way tables	
SP.A.4 Interpret and compare a range of data displays, including side-by-	1	Introducing and interpreting bivariate data and two-way tables	<ul> <li>interpret data presented in two-way tables that represent two categorical variables</li> <li>ask and answer comparative and relational questions related to data in a two-way table</li> </ul>	
side column graphs for two categorical variables	2	Representing bivariate data in a two-way table	<ul> <li>create a two-way table to organise data involving 2 categorical variables</li> <li>ask and answer comparative and relational questions related to data in a two-way table</li> </ul>	
Learning Journeys Side-by-side column graphs				
SP.A.4 Interpret and compare a range of data displays, including side-byside column graphs for two categorical variables	1	Introducing and interpreting side-by-side column graphs	<ul> <li>interpret side-by-side column graphs for 2 categorical variables</li> <li>ask and answer comparative and relational questions related to data in a side-by-side column graph</li> </ul>	
	2	Representing bivariate data in a side-by-side column graph	<ul> <li>construct a side by side column graph for two categorical variables</li> <li>ask and answer comparative and relational questions related to data in a side by side column graph</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

#### **Statsitics and Probability**

MA3-18SP uses appropriate methods to collect data and constructs, interprets and evaluates data displays, including dot plots, line graphs and two-way tables

including dot plots, line graphs and two-way tables					
	Quest: (2) Data investigations				
	Learning Journeys Comparing & selecting bivariate data displays				
Content Descriptor	Steps	Spine Nodes	Subnodes		
SP.A.4 Interpret and compare a range of data displays, including side-byside column graphs for two categorical variables	1	Comparing different displays of the same data set	<ul> <li>interpret and compare different displays of the same data set to determine the most appropriate display for the data set</li> <li>compare the effectiveness of different student-created data displays</li> <li>discuss the advantages and disadvantages of different representations of the same data</li> <li>explain which display is the most appropriate for interpretation of a particular data set</li> <li>compare representations of the same data set in a side-by-side column graph and in a two-way table</li> </ul>		
	2	Selecting appropriate data displays	<ul> <li>select an appropriate type of graph to represent a set of data</li> <li>graph data using technology, and justify the choice of graph from types of graphs already studied</li> </ul>		
	Lea	arning Journeys Int	erpreting and evaluating secondary data		
	1	Interpreting discrete and continuous secondary data	<ul> <li>differentiate between first-hand and second-hand data</li> <li>read, interpret, and draw conclusions from secondary data presented in charts, tables, and graphs (including broken-line graphs)</li> </ul>		
	2	Interpreting secondary data	<ul> <li>interpret data representations found in digital media and in factual texts</li> <li>interpret tables and graphs from the media and online sources</li> <li>identify and describe conclusions that can be drawn from a particular representation of data</li> </ul>		
SP.A.5 Interpret secondary data presented in digital media and elsewhere	3	Evaluating data collection for bias and misleading information	<ul> <li>identify sources of possible bias in representations of data in the media by discussing various influences on data collection and representation</li> <li>determine, through investigation, how well a set of data represents a population, on the basis of the method that was used to collect the data</li> <li>discuss the messages that those who created a particular data representation might have wanted to convey</li> </ul>		
	4	Evaluating data displays for bias and misleading information	<ul> <li>critically evaluate data representations found in digital media and related claims</li> <li>identify misleading representations of data in the media</li> <li>explain how different scales used on graphs can influence conclusions drawn from the data</li> <li>demonstrate, through investigation, an understanding of how data from charts, tables, and graphs can be used to make inferences and convincing arguments</li> </ul>		



### **Understanding Practice and Fluency (UPF)**

#### **Statsitics and Probability**

MA3-19SP conducts chance experiments and assigns probabilities as values between 0 and 1 to describe their outcomes

their outcomes				
Quest: (1) Probability values				
		Learning Journey	S Outcomes of Chance Experiments	
Content Descriptor	Steps	Spine Nodes	Subnodes	
SP.B.1 List outcomes of chance experiments involving equally likely outcomes and represent probabilities of those outcomes using fractions	1	Investigating equally likely outcomes of chance experiments	<ul> <li>recognise that outcomes are described as 'equally likely' when any one outcome has the same chance of occurring as any other outcome</li> <li>list all outcomes in chance experiments where each outcome is equally likely to occur</li> <li>use the term 'probability' to describe the numerical value that represents the likelihood of an outcome of a chance experiment</li> <li>represent probabilities of outcomes of chance experiments using fractions</li> <li>determine the likelihood of winning simple games by considering the number of possible outcomes</li> </ul>	
	2	Describing the chances of simple events occurring using familiar language and numeric benchmarks	create, order, describe and explain the likelihood of simple events using the language of probability and numeric benchmarks of 0, 1/2 and 1	
		Learning Jou	rneys Probabilities from 0 to 1	
SP.B.2 Recognise that probabilities range from 0 to 1	1	Ordering chance outcomes in a probabilities range from 0 to 1	<ul> <li>establish that the sum of the probabilities of the outcomes of any chance experiment is equal to 1</li> <li>understand that the probability ranges cannot be less than 0 and greater than 1</li> <li>order commonly used chance words on an interval from zero ('impossible') to one ('certain')</li> <li>describe events that are impossible and events that are certain</li> <li>describe the likelihood of a variety of events as being more or less than a half (or 0.5) and order the events on an interval</li> </ul>	
		Ques	t: (2) Probability values	
	Lear	ning Journeys Freq	uency and Fairness in Chance Experiments	
SP.B.3 Compare observed frequencies across experiments with expected frequencies	1	Comparing observed frequencies with expected frequencies in chance experiments	<ul> <li>use the term 'frequency' to describe the number of times a particular outcome occurs in a chance experiment</li> <li>distinguish between the 'frequency' of an outcome and the 'probability' of an outcome in a chance experiment</li> <li>record and compare the expected frequencies of outcomes of chance experiments with observed frequencies, including where the outcomes are not equally likely</li> <li>explain why observed frequencies of outcomes in chance experiments may differ from expected frequencies</li> <li>recognise that some random generators have outcomes that are not equally likely and discuss the effect on expected outcomes</li> </ul>	
	2	Exploring fair and unfair chance experiments	<ul> <li>discuss the 'fairness' of simple games involving chance</li> <li>design a spinner or label a die so that a particular outcome is more likely than another and discuss the probabilities of the outcomes</li> <li>list all possible outcomes using tables, lists and tree diagrams (with or without digital technology) where outcomes are not equally likely to occur</li> <li>record results of chance experiments using appropriate methods</li> </ul>	



#### **Understanding Practice and Fluency (UPF)**

#### **Statsitics and Probability**

2

from chance

samples

MA3-19SP conducts chance experiments and assigns probabilities as values between 0 and 1 to describe their outcomes **Quest: (2) Probability values** Learning Journeys Probability as a Fraction, Decimal or Percent Content **Spine Nodes** Subnodes Descriptor • list the outcomes for chance experiments where the outcomes are not equally likely to occur and assign probabilities to the outcomes using Describing SP.B.4 Describe • use knowledge of equivalent fractions, decimals and percentages to probability of a probabilities using assign probabilities to the likelihood of outcomes 1 single event using fractions, decimals fractions, decimals explain real-life events in the context of probabilities and percentages and percentages use the terminology 'theoretical probabilitiy' and/or 'relative frequency' as the value given by the formula: number of times named outcome (s) did happen/total number of trials Learning Journeys Chance Experiments with Trials and Sampling assign expected probabilities to outcomes in chance experiments with random generators, including digital simulators, and compare the expected probabilities with the observed probabilities after both small Using digital and large numbers of trials SP.B.5 Conduct technologies to 1 determine and discuss the differences between the expected chance experiments conduct chance probabilities and the observed probabilities after both small and large with both small experiments numbers of trials and large numbers of trials using explain what happens to the observed probabilities as the number of appropriate digital trials increases technologies Making use sample results to make predictions about a larger sample generalisations

• discuss whether a prediction about a larger population, from which a

sample comes, would be the same if a different sample were used

5



#### **Understanding Practice and Fluency (UPF)**

#### **Number and Algebra**

MA4-4NA compares, orders and calculates with integers, applying a range of strategies to aid computation **Quest: Working with integers Learning Journeys** Laws of multiplication and division Content **Spine Nodes Subnodes Descriptor** Using factors of a number to aid mental • use factors of a number to aid mental computation involving multiplication and computation involving multiplication and Showing the connection between division show the connection between division and 2 and multiplication, including where there is multiplication, including where there is a a remainder remainder Applying the distributive law to aid in • apply the distributive law to aid in mental mental computation to expand expressions computation to expand expressions containing 2 terms within the grouping containing 2 terms within the grouping symbols symbols 3 • apply the commutativity law to aid mental computation Applying the commutativity law of multiplication to aid mental computation • apply the associativity law of multiplication to aid in mental computation NA.A.1 Apply Applying the distributive law to aid in • apply the distributive law to aid in mental the associative, mental computation to expand expressions computation to expand expressions 4 commutative containing 3 or more terms within the containing 3 or more terms within the and distributive grouping symbols grouping symbols laws to aid mental and Solving problems within a given context by solve problems within a given context by 5 written applying the distributive law applying the distributive law computation Describing the direction and magnitude of describe the direction and magnitude of 1 integers when applied to the number line integers Describing the direction and magnitude of describe the direction and magnitude of integers when applied to the number line integers 2 order integers of any size in ascending and Ordering integers descending order including negative numbers Understanding addition and subtraction of · understand addition and subtraction of integers pictorially integers pictorially 3 Understanding addition and subtraction of · understand addition and subtraction of integers symbolically integers symbolically Representing addition and subtraction on a represent addition and subtraction on a 4 horizontal or vertical number line diagram horizontal or vertical number line diagram

Adding and subtracting negative integers

add and subtract negative integers



## **Understanding Practice and Fluency (UPF)**

		Quest: Working with in	itegers		
Learning Journeys Solving temperature problems					
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Measuring temperature scales	interpret scales on thermometers to accurately read temperatures		
	2	Calculating change in temperature	<ul> <li>calculate the difference in temperature between all ranges including between 0 and a negative or positive, both positive, both negative, 1 positive and 1 negative</li> </ul>		
NA.A.2 Compare, order, add and subtract integers		Colving much long within a given contact	solve problems within a given context involving a change in temperature		
sustrace integers	3	Solving problems within a given context involving a change in temperature	<ul> <li>solve problems within a given context involving a change in temperature using temperature specific terminology, eg warmer</li> </ul>		
	4	Describing the difference between a given minimum and maximum temperature using terms such as 'temperature range'	<ul> <li>describe the difference between a given minimum and maximum temperature using terms such as 'temperature range'</li> </ul>		
		Learning Journeys Applying the four	operations to integers		
	1	Using the 4 operations with integers	use the 4 operations to solve problems involving integers		
NA.A.3 Carry out the four operations with rational	2	Applying the order of operations to evaluate expressions involving integers with no exponents or radicals	apply the order of operations to evaluate expressions involving integers with no exponents or radicals		
numbers and integers, using efficient mental and written strategies and appropriate digital technologies	3	Applying the order of operations to evaluate expressions involving integers where the operator is contained within the numerator or denominator of a fraction	<ul> <li>apply the order of operations to evaluate expressions involving integers, where an operator is contained within the numerator or denominator of a fraction and the result is a whole number</li> <li>apply the order of operations to evaluate expressions involving integers where the operator is contained within the numerator or denominator of a fraction</li> </ul>		
		MA4-5NA operates with fractions, deci	mals and percentages		
		Quest: Fractions, decimals &	percentages		
		Learning Journeys Fractions: imprope	r and proper fractions		
	1	Generating equivalent fractions with denominators (denominators 1–100, 1000)	generate equivalent fractions		
NA.B.1 Compare fractions using equivalence; locate and represent positive and negative fractions and mixed numerals on a number line	2	Expressing a fraction in its simplest form	<ul> <li>determine the highest common factor of a pair of integers</li> <li>express a fraction in its simplest form</li> </ul>		
	3	Expressing improper fractions as mixed numerals	<ul> <li>express improper fractions as mixed numerals the do not require simplification of the proper fraction</li> <li>express improper fractions as mixed numerals the require simplification of the proper fraction</li> </ul>		
	4	Expressing mixed numerals as improper fractions	express mixed numerals as improper fractions		



## **Understanding Practice and Fluency (UPF)**

		MA4-5NA operates with fractions, de	ecimals and percentages
		Quest: Fractions, decimals	& percentages
		Learning Journeys Fractions: cor	mparing and ordering
Content Descriptor	Steps	Spine Nodes	Subnodes
	1	Comparing and ordering proper fractions	<ul> <li>compare and order proper fractions where the denominators are not always multiples of the same number</li> <li>record comparisons using =, ≠, &lt;, &gt; ≤, ≥ symbols</li> </ul>
NA.B.1 Compare fractions using equivalence; locate and	2	Comparing and ordering improper fractions	<ul> <li>compare and order improper fractions where the denominators are not always multiples of the same number</li> <li>record comparisons using =, ≠, &lt;, &gt; ≤, ≥ symbols</li> </ul>
represent positive and negative fractions and mixed numerals on a number line	3	Comparing and ordering proper fractions, improper fractions and mixed numerals	<ul> <li>compare and order proper fractions, improper fractions and mixed numerals where the denominators are not always multiples of the same number</li> <li>record comparisons using =, ≠, &lt;, &gt; ≤, ≥ symbols</li> </ul>
	4	Placing positive and negative fractions, decimals and mixed numbers on a number line in order to compare	place positive and negative fractions, decimals and mixed numbers on a number line in order to compare
		Learning Journeys Fractions	: adding fractions
		Adding proper fractions with common denominators	add proper fractions with common denominators
NA.B.2 Solve problems involving addition and subtraction	1	Adding improper fractions with common denominators	<ul> <li>add improper fractions with common denominators</li> <li>add improper fractions with common denominators expressing answers as a mixed numeral</li> </ul>
of fractions, including those	2	Adding proper fractions with unlike denominators	add proper fractions with unlike denominators
with unrelated denominators	3	Adding improper fractions with unlike denominators	<ul> <li>add improper fractions with unlike denominators</li> <li>add improper fractions with unlike denominators expressing answers as a mixed numeral</li> </ul>
		Learning Journeys Fractions: s	ubtracting fractions
	1	Subtracting proper fractions with common denominators	subtract proper fractions with common denominators
NA.B.2 Solve problems involving addition and subtraction of fractions, including those with unrelated denominators	2	Subtracting improper fractions with common denominators	<ul> <li>subtract improper fractions with common denominators</li> <li>subtract improper fractions with common denominators, expressing answers as a mixed numeral</li> </ul>
	3	Subtracting mixed numbers with common denominators	subtract mixed numbers with common denominators
	4	Subtracting proper fractions with unlike denominators	subtract proper fractions with unlike denominators
	5	Subtracting improper fractions with unlike denominators	<ul> <li>subtract improper fractions with unlike denominators</li> <li>subtract improper fractions with unlike denominators expressing answers as a mixed numeral</li> </ul>
		Subtracting mixed numbers with unlike denominators	subtract mixed numbers with unlike denominators



## **Understanding Practice and Fluency (UPF)**

MA4-5NA operates with fractions, decimals and percentages					
	Quest: Fractions, decimals & percentages				
		Learning Journeys Fractions: adding	and subtracting fractions		
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Performing addition or subtraction with fractions where fractions can be in different forms	perform addition or subtraction with fractions where fractions can be in different forms		
NA.B.2 Solve problems involving addition	2	Subtracting a fraction from an integer	subtract a fraction from a whole number using written methods		
and subtraction of fractions, including those with unrelated denominators	3	Demonstrating an understanding of adding and subtracting positive fractions and mixed numerals, with like and unlike denominators, concretely, pictorially and symbolically	demonstrate an understanding of adding and subtracting positive fractions and mixed numerals, with like and unlike denominators, concretely, pictorially and symbolically		
	4	Recognising and explaining incorrect operations with fractions	recognise and explain incorrect operations with fractions		
		Learning Journeys Multiplying deci	mals & finding quantities		
NA.B.3 Multiply	1	Multiplying decimals using a calculator	multiply decimals using a calculator		
and divide fractions and	2	Multiplying decimals using written/ mental methods	multiply decimals using mental/written methods		
decimals using efficient written strategies	3	Calculating decimals of quantities using a calculator	calculate decimals of quantities using a calculator		
and digital technologies	4	Calculating decimals of quantities using mental/written methods	calculate decimals of quantities using mental, written and calculator methods		
		Learning Journeys Multiplying fract	ions & finding quanitites		
	1	Multiplying proper fractions by a whole number greater than 1	<ul> <li>multiply proper fractions by a whole number greater than 1</li> <li>multiply improper fractions by a whole number greater than 1</li> </ul>		
		Multiplying improper fractions by a whole number greater than 1, expressing answer as a mixed numeral	multiply improper fractions, expressing answer as a mixed numeral		
NA.B.3 Multiply	2	Multiplying 2 proper fractions	multiply 2 proper fractions using written methods		
and divide fractions and		Multiplying 2 improper fractions	multiply improper fractions using written methods		
decimals using efficient written strategies and digital technologies	3	Multiplying 2 improper fractions, expressing the answer as a mixed numeral	multiply 2 improper fractions expressing the answer as a mixed numeral		
		Multiplying 2 mixed numerals	multiply mixed numerals using written methods		
	4	Multiplying mixed numerals by a whole number greater than 1	multiply mixed numerals by a whole number greater than 1		
	5	Multiplying proper fractions, improper fractions and mixed numerals using written methods	multiply proper fractions, improper fractions and mixed numerals using written methods		
		Calculating fractions of quantities using mental or written strategies	calculate fractions of quantities using mental or written strategies		



## **Understanding Practice and Fluency (UPF)**

		MA4-5NA operates with fractions, d	ecimals and percentages
		Quest: Fractions, decimals	& percentages
		Learning Journeys Dividing integer	s, fractions and decimals
Content Descriptor	Steps	Spine Nodes	Subnodes
NA.B.3 Multiply and divide	1	Dividing positive integers by unit fractions	divide positive integers by unit fractions
fractions and decimals using efficient written	2	Dividing fractions and decimals using a calculator	divide fractions and decimals using a calculator
strategies and digital technologies	3	Dividing decimals by powers of 10	divide decimals by powers of 10
	ı	Learning Journeys Dividing fractions	by fractions and integers
	1	Dividing a unit fraction by a positive integer	• divide unit fractions by whole numbers, eg $1/3 \div 2 = 1/6$
		Dividing a positive integer by a proper fraction	divide a positive integer by a proper fraction
NA.B.3 Multiply	2	Dividing a proper fraction by a positive	divide a non-unit proper fraction by a whole number (where the divisor is a factor of the numerator). Use diagrams for support
and divide fractions and		integer	divide a non-unit proper fraction by any whole number
decimals using efficient written strategies	3	Dividing a proper fraction by a proper fraction	divide a proper fraction by a proper fraction
and digital technologies	4	Dividing a positive integer by an improper fraction	divide a positive integer by an improper fraction and mixed numeral
		Dividing an improper fraction by a positive integer	divide an improper fraction by a positive integer
	5	Dividing improper fractions by proper fractions and vice versa	divide improper fractions by proper fractions and vice versa
		Dividing an improper fraction by an improper fraction	divide an improper fraction by an improper fraction
	Lea	arning Journeys Expressing one qua	ntity as a fraction of another
NA.B.4 Express one quantity as a fraction of another, with	1	Expressing 1 quantity as a fraction (proper/improper/mixed) of another	express 1 quantity as a fraction of another
and without the use of digital technologies	2	Expressing 1 quantity as a fraction of another (using digital technology)	express 1 quantity as a fraction of another with the use of digital technology
		Learning Journeys Roun	ding decimals
NA.B.5 Round decimals to a	1	Rounding decimals to a specified number of decimal places (simple rounding)	<ul> <li>round decimals to a given number of decimal places when rounding decimals up/down to the next decima place value</li> </ul>
specified number of decimal places	2	Rounding decimals to a specified number of decimal places (complex rounding)	round decimals to a given number of decimal places when rounding decimals requires places to be filled with zeroes



## **Understanding Practice and Fluency (UPF)**

MA4-5NA operates with fractions, decimals and percentages					
	Quest: Fractions, decimals & percentages				
	Le	arning Journeys Investigate terminati	ng and recurring decimals		
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.B.6 Investigate terminating and recurring decimals	1	Converting fractions to terminating decimals by manipulating the denominator to be a power of 10	<ul> <li>convert fractions to terminating decimals by manipulating the denominator to be a power of 10</li> <li>convert improper fractions to terminating decimals by manipulating the denominator to be a power of 10</li> <li>convert mixed numerals to terminating decimals by manipulating the denominator to be a power of 10</li> </ul>		
		Learning Journeys Convert	ing decimals		
	1	Demonstrating that the decimal expansion of a rational number either repeats or terminates	demonstrate that the decimal expansion of a rational number either repeats or terminates		
NA.B.7 Connect fractions, decimals and percentages and carry out simple conversions	2	Converting decimals to percentages	<ul> <li>convert decimals with up to 2 decimal places to percentages containing whole-numbers only</li> <li>convert decimals with more than 2 decimal places to percentages, writing answers as a percentage with decimal parts</li> <li>convert decimals with 3-4 decimal places to percentages, writing answers in fraction form</li> <li>convert decimals with 5 or more decimal places to percentages, writing answers in decimal form rounded to an appropriate degree of accuracy</li> </ul>		
		Learning Journeys Convertin	g percentages		
		Converting percentages less than or equal to 100% into fractions	convert percentages less than or equal to 100% into fractions		
	1	Converting terminating percentages less than 100% into a decimal	convert terminating percentages less than 100% into a decimal		
NA.B.7 Connect		Converting percentages greater than 100% to mixed numerals	convert percentages greater than 100% to mixed numerals		
fractions, decimals and percentages and carry out simple conversions	2	Converting percentages greater than 100% to improper fractions	convert percentages greater than 100% to improper fractions		
		Converting terminating percentages greater than or equal to 100% into a decimal	convert terminating percentages greater than or equal to 100% into a decimal		
	3	Converting recurring percentages less than 100% into a decimal	convert recurring percentages less than 100% into a decimal		
		Converting recurring percentages greater than or equal to 100% into a decimal	convert recurring percentages greater than or equal to 100% into a decimal		



## **Understanding Practice and Fluency (UPF)**

MA4-5NA operates with fractions, decimals and percentages					
	Quest: Fractions, decimals & percentages				
		Learning Journeys Conver	ting fractions to decimals		
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Converting fractions to decimals using a calculator	convert fractions to decimals using a calculator		
NA.B.7 Connect fractions, decimals and percentages and	2	Converting fractions to terminating decimals using division	<ul> <li>convert unit fractions to terminating decimals using division</li> <li>convert improper fractions to terminating decimals using division</li> <li>convert mixed numerals to terminating decimals using division</li> </ul>		
carry out simple conversions	3	Converting fractions to recurring decimals using division	<ul> <li>convert fractions to recurring decimals using division</li> <li>convert improper fractions to recurring decimals using division</li> <li>convert mixed numerals to recurring decimals using division</li> </ul>		
		Learning Journeys Converti			
	1	Converting fractions to percentages using a calculator	convert fractions to percentages using a calculator		
NA.B.7 Connect fractions, decimals and percentages and carry out simple conversions	2	Converting fractions to terminating percentages by manipulating the denominator to 100	<ul> <li>convert fractions to terminating percentages by manipulating the denominator to be 100</li> <li>convert improper fractions to terminating percentages by manipulating the denominator to be 100</li> <li>convert mixed numerals to terminating percentages by manipulating the denominator to be 100</li> </ul>		
	3	Converting fractions to terminating percentages using division	<ul> <li>convert fractions to terminating percentages using division</li> <li>convert improper fractions to terminating percentages using division</li> <li>convert mixed numerals to terminating percentages using division</li> </ul>		
	4	Converting fractions to recurring percentages using division	<ul> <li>convert fractions to recurring percentages using division</li> <li>convert improper fractions to recurring percentages using division</li> <li>convert mixed numerals to recurring percentages using division</li> </ul>		
	Le	earning Journeys Ordering fract	tions, decimals and percentages		
NA.B.7 Connect fractions, decimals and percentages and carry out simple conversions	1	Ordering fractions, decimals and percentages	order fractions, decimals and percentages		
		Learning Journeys Investin	gating irrational numbers		
NA.B.8 Investigate the concept of irrational numbers, including π	1	Describing, informally, the properties of irrational numbers	describe, informally, the properties of irrational numbers		



## **Understanding Practice and Fluency (UPF)**

MA4-5NA operates with fractions, decimals and percentages				
Quest: Fractions, decimals & percentages				
		<b>Learning Journeys</b> Perc	entages of quantities	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Determining percentages of quantities (written and mental methods)	determine percentages of quantities using written and mental strategies	
NA.B.9 Find percentages of quantities and	2	Determining percentages of quantities (calculator method)	determine percentages of quantities using a calculator	
express one quantity as a percentage of another, with and	3	Expressing a smaller quantity/ value as a percentage amount of another larger quantity/value	<ul> <li>express a smaller quantity/value as a percentage amount of another larger quantity/value in the same units</li> <li>express a smaller quantity/value as a percentage amount of another larger quantity/value in different units</li> </ul>	
without the use of digital technologies	4	Expressing a larger quantity/value as a percentage amount of another smaller quantity/value	<ul> <li>express a larger quantity/value as a percentage amount of another smaller quantity/value in the same units</li> <li>express a larger quantity/value as a percentage amount of another smaller quantity/value in different units</li> </ul>	
		Learning Journeys Increasing	g and decreasing amounts	
	1	Increasing and decreasing amounts by percentages (calculator method)	increase and decrease a quantity by a given percentage using the calculator method	
NA.B.10 Solve problems involving the use of percentages, including percentage increases and decreases, with and without the use of digital technologies	2	Increasing and decreasing amounts by percentages (written and mental methods)	<ul> <li>increase an amount by first calculating the percentage increase value of the original amount, and then adding that result to the original amount</li> <li>decrease an amount by first calculating the percentage decrease value of the original amount, and then subtracting that result from the original amount</li> </ul>	
	3	Recognising and using equivalences when calculating percentage increases and decreases	<ul> <li>increase an amount by a percentage by multiplying the original amount by 1 + the percentage increase expressed as a decimal</li> <li>decrease an amount by a percentage by multiplying the original amount by 1 - the percentage decrease expressed as a decimal</li> <li>decrease an amount by a percentage by calculating the complementary percentage of that amount</li> </ul>	
		Learning Journeys Problem so	olving involving percentages	
NA.B.10 Solve problems involving the use of percentages, including percentage increases and decreases, with and without the use of digital technologies	1	Using the unitary method to solve problems involving percentages (written method)	<ul> <li>use the unitary method to find the original quantity/value following a percentage increase/decrease, eg find the original value, given the value after an increase of 20%</li> <li>find original value after a percentage increase/decrease</li> </ul>	
	2	Using the unitary method to solve problems involving percentages (calculator method)	<ul> <li>use the unitary method with a calculator to solve problems involving percentages, eg find the original value given the value after an increase of 20%</li> <li>find the original value after a percentage increase/ decrease</li> </ul>	



## **Understanding Practice and Fluency (UPF)**

	MA4-5NA operates with fractions, decimals and percentages				
		Quest: Fractions, deci	mals & percentages		
		Learning Journeys Problem so	olving involving percentages		
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.B.10 Solve problems involving the use of percentages,	3	Interpreting and using nutritional information panels on product packaging where percentages are involved	interpret and use nutritional information panels on product packaging where percentages are involved		
including percentage increases and decreases, with	3	Interpreting and using statements about the environment involving percentages, eg energy use for different purposes such as lighting	interpret and use statements about the environment involving percentages, eg energy use for different purposes, such as lighting		
and without the use of digital technologies	4	Solving real-life problems involving percentages	solve a variety of real-life problems involving percentages, including percentage composition problems and problems involving money		
	М	A4-6NA solves financial probler	ns involving purchasing goods		
		Quest: Solving financi	al maths problems		
		Learning Journeys	Calculating GST		
	1	Calculating GST given the pre- GST price with the use of digital technology	calculate GST for goods purchased in Australia, given the pre-GST price with the use of digital technology		
	2	Calculating GST given the pre-GST price without the use of digital technology	<ul> <li>calculate GST for goods purchased in Australia, given the pre-GST price without the use of digital technology</li> <li>calculate GST-inclusive prices for goods purchased in Australia, given the pre-GST price without the use of digital technology</li> </ul>		
NA.C.1 Investigate and calculate the Goods and Services Tax (GST), with and without the use of digital technologies	3	Calculating GST given the GST- inclusive price with the use of digital technology	<ul> <li>calculate GST for goods purchased in Australia, given the GST-inclusive price with the use of digital technology</li> <li>calculate pre-GST prices for goods purchased in Australia, given the GST-inclusive price with the use of digital technology</li> </ul>		
	4	Calculating GST given the pre- GST price with the use of digital technology	<ul> <li>calculate GST for goods purchased in Australia, given the pre-GST price with the use of digital technology</li> <li>calculate GST-inclusive prices for goods purchased in Australia, given the pre-GST price with the use of digital technology</li> </ul>		
	5	Calculating GST given the GST- inclusive price without the use of digital technology	<ul> <li>calculate GST for goods purchased in Australia, given the GST-inclusive price without the use of digital technology</li> <li>calculate pre-GST prices for goods purchased in Australia, given the GST-inclusive price without the use of digital technology</li> </ul>		



## **Understanding Practice and Fluency (UPF)**

MA4-6NA solves financial problems involving purchasing goods				
Quest: Solving financial maths problems				
		Learning Journeys Bes	t buys and discounts	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Calculating 'best buys' by comparing price per unit, or quantity per monetary unit, with the use of digital technologies	calculate 'best buys' by comparing price per unit, or quantity per monetary unit, with the use of digital technologies, eg 500 g for \$4.50 compared with 300 g for \$2.75	
NA.C.2 Investigate and calculate 'best	2	Calculating discounts given the original price	<ul> <li>calculate a discount amount given the original price and the percentage discount</li> <li>calculate the final price of an item given the discount percentage and original price</li> </ul>	
buys', with and without the use of digital technologies	3	Calculating 'best buys' by comparing price per unit, or quantity per monetary unit, without the use of digital technology	calculate 'best buys' by comparing price per unit, or quantity per monetary unit without the use of digital technology, eg 500 g for \$4.50 compared with 300 g for \$2.76	
	4	Calculating discounts starting with the final price	<ul> <li>calculate a discount amount given the final price and the percentage discount</li> <li>calculate the original price given the final price and the percentage discount</li> </ul>	
	- 1	Learning Journeys Solving prob	lems involving profit and loss	
	1	Understanding the financial terms 'profit' and 'loss'	understand the meaning of the terms 'cost price', 'sale price', 'profit and loss' and the relationships between them	
NA.C.3 Solve	2	Solving problems involving profit and loss with the use of digital technology	<ul> <li>calculate the selling price, given the percentage profit/loss on the cost price with the use of digital technology</li> <li>express profit/loss as a percentage of the cost price with the use of digital technology</li> <li>calculate the cost price, given the selling price and</li> </ul>	
problems involving profit and loss,			percentage profit/loss with the use of digital technology	
with and without the use of digital technologies	3	Solving problems involving profit and loss without the use of digital technology	<ul> <li>calculate the selling price, given the percentage profit/loss on the cost price without the use of digital technology</li> <li>express profit/loss as a percentage of the cost price without the use of digital technology</li> <li>calculate the cost price, given the selling price and percentage profit/loss without the use of digital technology</li> </ul>	
	4	Solving complex problems involving multiple steps	solve complex problems involving multiple steps	



## **Understanding Practice and Fluency (UPF)**

MA4-6NA solves financial problems involving purchasing goods						
Quest: Rates and ratios						
	Learning Journeys Using simple ratios					
Content Descriptor	Steps	Spine Nodes	Subnodes			
	4	Comparing quantities measured in the same units using ratios	compare quantities measured in the same units using ratios			
NA.D.1 Recognise and solve	1	Dividing an interval into a given ratio on a number line	divide an interval into a given ratio on a number line			
problems involving simple ratios	2	Expressing 1 part of a ratio as a fraction of the whole	express 1 part of a ratio as a fraction of the whole			
	3	Identifying terms of a ratio as 'parts' of the ratio	identify terms of a ratio as 'parts' of the ratio			
		Learning Journeys	Simplfying ratios			
	1	Simplifying ratios using highest common factors	simplify ratios using highest common factors			
NA.D.1 Recognise and solve	2	Simplifying ratios with fractions involved	simplify ratios containing one or more fraction parts using the HCF to re-write as a pair of fractions with a common denominator first			
problems involving simple ratios	3	Simplifying ratios with decimals involved	simplify ratios containing one or more decimal parts multiplying both parts by a common power of 10 that removes the decimal. Write the resultant ratio in simplest form			
	4	Identifying equivalent ratios	identify equivalent ratios			
		Learning Journeys Solve simp	le problems involving ratios			
NA.D.1 Recognise	1	Applying the unitary method to ratio problems	apply the unitary method to ratio problems			
and solve problems involving simple ratios	2	Dividing a quantity into a given ratio	<ul> <li>divide a quantity into a given ratio</li> <li>express the division of a quantity into 2 parts as a ratio using original amounts</li> </ul>			
		<b>Learning Journeys</b> Solve p	roblems involving ratios			
NA.D.2 Solve a range of problems	1	Dividing a given quantity into 2 parts in a given part:whole ratio	divide a given quantity into 2 parts in a given part:whole ratio			
involving ratios and rates, with and without the use of digital technologies	2	Solving a variety of real-life problems involving dividing quatities into a given ratio	solve a variety of real-life problems involving dividing quantities into a given ratio			
	Learning Journeys Ratios involving more than two parts					
NA.D.2 Solve a	1	Simplifying ratios using highest common factors (ratio composed of 3 or more numbers)	simplify ratios using highest common factors			
range of problems involving ratios and rates, with and without the use of	2	Dividing a quantity into a given ratio (ratio composed of 3 or more numbers)	divide a quantity in a given ratio			
digital technologies	3	Applying the unitary method to ratio problems (ratio composed of 3 or more numbers)	apply the unitary method to ratio problems			



## **Understanding Practice and Fluency (UPF)**

		Quest Pates	and ratios	
Quest: Rates and ratios				
_		Learning Journeys	Converting ratios	
Content Descriptor	Steps	Spine Nodes	Subnodes	
NA.D.2 Solve a range of problems involving ratios	1	Converting units in a ratio into the same unit then simplifying	<ul><li>convert units of a ratio into the same unit</li><li>simplify ratios</li></ul>	
and rates, with and without the use of digital technologies	2	Converting between units of measurement using ratios	convert between units of measurement using ratios	
		Learning Journey	ys Using rates	
	1		• use rates to compare quantities measured in different unit	
NA.D.2 Solve a	2	Converting given information into a simplified rate	convert given information into a simplified rate	
range of problems	3	Comparing rates	compare 2 quantities of different rates	
involving ratios and rates, with and without the use of	4	Determining an amount for a given time period given a rate	determine an amount for a given time period given a unit rate	
digital technologies			determine an amount for a given time period given a rate	
	5	Solving problems comparing 2 given rates by simplifying	solve problems comparing 2 given rates by simplifying	
		Learning Journeys Dis	stance/time graphs	
	1	Matching a distance/time graph to a description of a particular journey and explaining the reasons for the choice	match a distance/time graph to a description of a particula journey and explain the reasons for the choice	
		Recognising concepts such as change of speed and direction in distance/time graphs	recognise concepts such as change of speed and direction in distance/time graphs	
	2	Understanding the meaning of straight line segments with different gradients in the graph of a particular journey	understand the meaning of straight-line segments with different gradients in the graph of a particular journey	
NA.D.3 Investigate, interpret and analyse graphs from authentic		Recognising the significance of horizontal line segments in distance/time graphs	recognise the significance of horizontal line segments in distance/time graphs	
data		Understanding which variables go on the horizontal and vertical axis	understand which variables go on the horizontal and vertical axis	
	3	Comparing distance/time graphs of the same situation to decide which one is the most appropriate	compare distance/time graphs of the same situation to decide which one is the most appropriate	
		Solving problems involving distance/time rates	solve a variety of real-life problems involving rate of travel problems	
	4	Calculating speeds for straight line segments of given distance/time graphs	calculate speeds for straight-line segments of given distance/time graphs	
	5	Constructing distance/time graphs	construct distance/time graphs	



## **Understanding Practice and Fluency (UPF)**

MA4-6NA solves financial problems involving purchasing goods					
	Quest: Rates and ratios				
	Learning Journeys Graphs and rates extension				
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.D.3 Investigate, interpret and analyse graphs	1	Interpreting information using the relative positions of 2 points on a line graph, rather than a detailed scale	<ul> <li>interpret information using the relative positions of 2 points on a line graph, rather than a detailed scale</li> </ul>		
from authentic data	2	Calculating unit rates associated with ratios of fractions	<ul> <li>calculate unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units</li> </ul>		
		Quest: Operating with a	lgebraic expressions		
	Le	arning Journeys Variable and e	quivalent algebraic expressions		
	1	Using equivalent algebraic expressions involving addition	<ul> <li>recognise and use equivalent algebraic expressions using algebraic symbols and words involving addition</li> </ul>		
NA.E.1 Introduce	1	Using equivalent algebraic expressions involving multiplication	recognise and use equivalent algebraic expressions using algebraic symbols and words involving multiplication		
the concept of variables as a way of representing	2	Using equivalent algebraic expressions involving multiplication to indices	recognise and use equivalent algebraic expressions using algebraic symbols and words involving multiplication		
numbers using letters		Using equivalent algebraic expressions involving division	<ul> <li>recognise and use equivalent algebraic expressions using algebraic symbols and words using division</li> </ul>		
	3	Using algebraic symbols to represent mathematical operations written in words and vice versa	<ul> <li>use algebraic symbols to represent mathematical operations written in words and vice versa, eg the product of x and y is xy, x + y is the sum of x and y</li> </ul>		
		Learning Journeys Simplfyi	ng algebraic expressions		
	1	Simplifying algebraic expressions that involve addition and	<ul> <li>extend and apply the laws and properties of arithmetic to algebraic terms and expressions</li> </ul>		
		subtraction	<ul> <li>recognise like terms and add and subtract them to simplify algebraic expressions</li> </ul>		
	2	Simplifying algebraic expressions that involve multiplication	<ul> <li>simplify algebraic expressions that involve multiplication</li> <li>recognise the equivalence of algebraic expressions involving multiplication, eg 3bc = 3cb</li> </ul>		
NA.E.2 Extend and apply the laws and properties of arithmetic to	3	Simplifying algebraic expressions that involve division	<ul> <li>simplify algebraic expressions that involve division</li> <li>recognise whether particular algebraic expressions involving division are equivalent or not</li> </ul>		
algebraic terms and expressions	4	Connecting algebra with the commutative and associative properties of arithmetic to determine that $a + b = b + a$ and $(a + b) + c = a + (b + c)$	<ul> <li>connect algebra with the commutative and associative properties of arithmetic to determine that a + b = b + a and (a + b) + c = a + (b + c)</li> </ul>		
		Recognising the role of grouping symbols and the different meanings of expressions, such as 2a + 1 and 2(a + 1)	<ul> <li>recognise the role of grouping symbols and the different meanings of expressions, such as 2a + 1 and 2(a + 1)</li> </ul>		



## **Understanding Practice and Fluency (UPF)**

MA4-6NA solves financial problems involving purchasing goods					
	Quest: Rates and ratios				
-	_earnin	g Journeys Simplfying algebraic	expressions using mixed operations		
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.E.3 Simplify algebraic expressions involving the four operations	1	Simplifying algebraic expressions involving the 4 operations	<ul> <li>simplify a range of algebraic expressions, including those involving mixed operations</li> <li>apply the order of operations to simplify algebraic expressions</li> </ul>		
		Learning Journeys	Number patterns		
NA.E.4 Create algebraic expressions and evaluate them	1	Using objects to build a geometric pattern, record the results in a table of values, describe the pattern in words and algebraic symbols, and represent the relationship on a number grid	use objects to build a geometric pattern, record the results in a table of values, describe the pattern in words and algebraic symbols, and represent the relationship on a number grid		
by substituting a given value for	2	Checking pattern descriptions by substituting further values	check pattern descriptions by substituting further values		
each variable	3	Replacing written statements describing patterns with equations written in algebraic symbols	replace written statements describing patterns with equations written in algebraic symbols		
		Learning Journeys Ev	valuating formulae		
	1	Substituting known values in for pronumerals	• substitute known values in for pronumerals to find the value of an expression, eg if x = 2 and y = 3, find the value of 2x + 3y		
NA.E.4 Create algebraic expressions and evaluate them	2	Using simple formulas to solve problems involving substituting in known variables to solve a problem	use simple formulas to solve problems involving substituting in known variables to solve a problem		
by substituting a given value for each variable	3	Using authentic formulas to solve problems involving substituting in known variables to solve a problem	use authentic formulas to solve problems involving substituting in known variables to solve a problem		
	4	Determining whether a particular pattern can be described using algebraic symbols	describe patterns using algebraic symbols		
	Learning Journeys Creating algebraic expressions				
NA.E.4 Create algebraic	1	Creating algebraic expressions	create algebraic expressions and evaluate them by substituting a given value for each variable		
expressions and evaluate them by substituting a given value for each variable	2	Substituting into algebraic expressions and evaluating the result	<ul> <li>substitute into algebraic expressions and evaluate the result</li> <li>substitute numerical values into formulas and expressions, including scientific formulas</li> </ul>		



## **Understanding Practice and Fluency (UPF)**

MA4-6NA solves financial problems involving purchasing goods				
Quest: Rates and ratios				
	L	earning Journeys Extending an	d applying the distibutive law	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Expanding algebraic expressions in the form a(b+c) by removing grouping symbols (distributive law) where a and c are positive integers and b is a variable with coefficient of 1	expand algebraic expressions in the form a(b+c) by removing grouping symbols (distributive law) where a and c are positive integers and b is a variable with coefficient of 1	
	2	Expanding algebraic expressions in the form a(b+c) by removing grouping symbols (distributive law) where a and c are positive or negative integers and b is a variable with coefficient of 1	expand algebraic expressions in the form a(b+c) by removing grouping symbols (distributive law) where a and c are positive or negative integers and b is a variable with coefficient of 1	
NA.E.5 Extend and apply the distributive law to the expansion of algebraic expressions	3	Expanding algebraic expressions in the form a(b+c) by removing grouping symbols (distributive law) where a, b, and c can be positive numbers or variables (coefficients are 1)	expand algebraic expressions in the form a(b+c) by removing grouping symbols (distributive law) where a, b, and c can be positive numbers or variables (coefficients are 1)	
·	4	Expanding algebraic expressions in the form a(b+c) by removing grouping symbols (distributive law) where a, b and c can be positive or negative numbers or variables (coefficients 1 or -1)	expand algebraic expressions in the form a(b+c) by removing grouping symbols (distributive law) where a, b and c can be positive or negative numbers or variables (coefficients 1 or -1)	
5		Expanding algebraic expressions in the form a(b+c) by removing grouping symbols (distributive law) where a, b and c can be positive or negative numbers or variables (coefficients integers not limited to 1)	expand algebraic expressions in the form a(b+c) by removing grouping symbols (distributive law) where a, b and c can be positive or negative numbers or variables (coefficients integers not limited to 1)	
Learning Journeys Factorising algebraic expressions				
NA.E.6 Factorise	1	Decomposing (factorising) algebraic expressions by identifying numerical and algebraic factors	decompose (factorise) algebraic expressions by identifying numerical and algebraic factors and writing it as a product of these	
algebraic expressions by identifying	2	Factorising algebraic expressions by identifying numerical factors	factorise algebraic expressions by finding a common numerical factor and bringing it out the front of the brackets with its product inside the brackets	
numerical factors	3	Factorising algebraic expressions by identifying negative numerical factors	factorise algebraic expressions by finding a common negative numerical factor and bringing it out the front of the brackets with its product inside the brackets	



## **Understanding Practice and Fluency (UPF)**

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	MA4-6NA solves financial problems involving purchasing goods  Quest: Rates and ratios				
	Learning Journeys Factorising algebraic expressions 2				
Content Descriptor	Steps		Subnodes		
NA.E.7 Factorise algebraic	1	Factorising algebraic expressions by identifying only algebraic factors	factorise algebraic expressions by finding a common algebraic factor and bringing it out the front of the brackets with its product inside the brackets		
expressions by identifying algebraic factors	2	Factorising algebraic expressions by identifying algebraic and numerical factors	factorise algebraic expressions by finding a common algebraic and numerical factor and bringing it out the front of the brackets with its product inside the brackets		
N	1A4-9N	A operates with positive-intege	r and zero indices of numerical bases		
		Quest: Ir	ndices		
		Learning Journeys In	ntroducing indices		
	1	Describing numbers written in 'index form' using terms such as 'base', 'power', 'index', 'exponent', 'to the power of', 'squared', 'cubed'	<ul> <li>describe numbers written in 'index form' using terms such as 'base', 'power', 'index', 'exponent', 'to the power of', 'squared', 'cua describe numbers written in 'index form' using terms such as 'base', 'power', 'index', 'exponent', 'to the power of', 'squared', 'cubed'</li> <li>use index notation to express powers of numbers (positive)</li> </ul>		
NA.F.1 Investigate index notation and represent	2	Evaluating numbers expressed as powers of integers	indices only) bed'     evaluate numbers expressed as powers of integers		
whole numbers as products of powers of prime numbers	3	Evaluating expressions involving indices without using a calculator	<ul> <li>evaluate expressions involving indices without using a calculator</li> <li>apply the order of operations to evaluate expressions involving indices</li> </ul>		
	4	Evaluating expressions involving indices using a calculator	<ul> <li>evaluate expressions involving indices using a calculator</li> <li>apply the order of operations to evaluate expressions involving indices</li> </ul>		
	5	Using index laws to simplify equations with numerical bases	use index laws to simplify equations with numerical bases		
		Learning Journeys Divisib	ility, indices and factors		
	1	Determining and applying tests of divisibility for 2, 3, 4, 5, 6 and 10	• determine and apply tests of divisibility for 2, 3, 4, 5, 6 and 10		
NA.F.1 Investigate index notation and represent whole numbers as products of powers of prime numbers	2	Using index notation to express prime factors	<ul> <li>use factor trees to express a number as a product of its prime factors, using index notation where appropriate</li> <li>use the ladder method to express a number as a product of its prime factors, using index notation where appropriate</li> </ul>		
	3	Finding the highest common factor of large numbers by first expressing the numbers as products of prime factors	find the highest common factor of large numbers by first expressing the numbers as products of prime factors		



## **Understanding Practice and Fluency (UPF)**

MA4-9NA operates with positive-integer and zero indices of numerical bases						
	Quest: Indices					
	Learning Journeys Working with square roots					
Content Descriptor	Steps	Spine Nodes	Subnodes			
	1	Finding square roots of perfect square whole numbers only	find the square roots of perfect square whole numbers up to 100			
	2	Finding square roots of non-perfect squares using a calculator	find the square roots of non-perfect squares using a calculator			
NA.F.2 Investigate and use square roots of perfect square numbers		Determining between which 2 whole numbers lies the square root of a non-perfect square number up to 100	determine mentally, between which 2 whole numbers lies the square root of a non-perfect square number up to 100			
	3	Estimating the square root of non- square numbers	<ul> <li>estimate the square root of a non-square number up to 100</li> <li>estimate the square root of a non-square number up to 100 using a number line to estimate</li> </ul>			
		Learning Journeys Worki	ng with cube roots			
	1	Finding cube roots of perfect cube whole numbers	find the cube roots of perfect cube whole numbers up to 125			
NA.F.2 Investigate	2	Finding cube roots of non-perfect cubes using a calculator	find cube roots of non-perfect cubes using a calculator			
and use square roots of perfect square numbers	3	Determining mentally, between which 2 whole numbers lies the cube root of a non-perfect cube number up to 125	determine mentally, between which 2 whole numbers lies the cube root of a non-perfect cube number up to 125			
		Estimating the cube root of a non- perfect cube number up to 125	• estimate the cube root of a non-perfect cube number up to 125			
	Le	arning Journeys Solving problems	s with square and cube roots			
NA.F.2 Investigate	1	Finding square roots of large perfect square whole numbers from prime factors	find square roots of large perfect square whole numbers from prime factors			
and use square roots of perfect square numbers	2	Applying the order of operations to evaluate expressions involving square roots and cube roots, with and without a calculator	apply the order of operations to evaluate expressions involving square roots and cube roots, with and without a calculator			
	Learning Journeys Invesitgating index laws					
	1	Multiplying 2 or more terms with the same numerical base and a positive-integer power, leaving the solution in index form	multiply 2 or more terms with the same numerical base and a positive-integer power, leaving the solution in index form			
NA.F.3 Use index notation with numbers to establish the index	2	Dividing 2 or more terms with the same numerical base and a positive-integer power, leaving the solution in index form	divide 2 or more terms with the same numerical base and a positive-integer power, leaving the solution in index form			
laws with positive- integer indices and the zero index	3	Calculating an expression in which a number in index form is raised by a positive-integer power	calculate an expression in which a number in index form is raised by a positive-integer power			
	4	Using the zero index rule to simplify expressions involving numbers to the power of zero	use the zero index rule to simplify expressions involving numbers to the power of zero			



## **Understanding Practice and Fluency (UPF)**

	MA4-9N	A operates with positive-integer and ze	ero indices of numerical bases
		Quest: Solving equat	ions
		Learning Journeys Equations	introduction
Content Descriptor	Steps	Spine Nodes	Subnodes
	1	Demonstrating an understanding of equivalence and the preservation of equality or 'balance'	<ul><li>model preservation of equality pictorially</li><li>model preservation of equality symbolically</li></ul>
NA.G.1 Solve simple linear	2	Finding pairs of numbers that satisfy an equation with 2 unknowns	• find pairs of numbers that satisfy an equation with 2 unknowns
equations	3	Solving simple linear equations using concrete materials	solve simple linear equations using concrete materials, such as the balance model or cups and counters, stressing the notion of performing the same operation on both sides of an equation
	Le	arning Journeys Solving 1-step equatio	ns: addition/subtraction
	1	Solving linear equationsusing inverse operations involving 1 step of addition or subtraction (integers) with integer solutions	solve linear equationsusing inverse operations involving 1 step of addition or subtraction (integers) with integer solutions
NA.G.1 Solve simple linear equations	2	Solving linear equations using inverse operations involving 1 step of addition or subtraction (integers or decimals) with integer and non-integer solutions	solve linear equations using inverse operations involving 1 step of addition or subtraction (integers or decimals) with integer and non-integer solutions
	3	Solving linear equations using inverse operations involving 1 step of addition or subtraction (integers or fractions) with integer and non-integer solutions	solve linear equations using inverse operations involving 1 step of addition or subtraction (integers or fractions) with integer and non-integer solutions
		Learning Journeys Solving 1-step equa	ations: multiplication
NA.G.1 Solve simple linear equations	1	Solving linear equations using inverse operations involving 1 step of multiplication with integer solutions	solve linear equations using inverse operations involving 1 step of multiplication with integer solutions
	2	Solving linear equations using inverse operations involving 1 step of multiplication (integers or decimals) with integer and non-integer solutions	solve linear equations using inverse operations involving 1 step of multiplication (integers or decimals) with integer and non-integer solutions
	3	Solving linear equations using inverse operations involving 1 step of multiplication (integers or decimals) with integer and non-integer solutions	solve linear equations using inverse operations involving 1 step of multiplication (integers or decimals) with integer and non-integer solutions
		Learning Journeys Solving 1-step e	quations: division
	1	Solving linear equations using inverse operations involving 1 step of division (integers) with integer solutions	solve linear equations using inverse operations involving 1 step of division (integers) with integer solutions
NA.G.1 Solve simple linear equations	2	Solving linear equations using inverse operations involving 1 step of division with integer and non-integer solutions (pronumeral in numerator position)	solve linear equations using inverse operations involving 1 step of division with integer and non-integer solutions (pronumeral in numerator position)
	3	Solving linear equations (integer, fraction or decimal coefficients) using inverse operations involving 1 step of division with integer and non-integer solutions (pronumeral in numerator position)	solve linear equations (integer, fraction or decimal coefficients) using inverse operations involving 1 step of division with integer and non-integer solutions (pronumeral in numerator position)  13



## **Understanding Practice and Fluency (UPF)**

	MA4-9N	A operates with positive-integer and ze	ero indices of numerical bases	
		Quest: Solving equat	ions	
	L	earning Journeys Solving 1-step equat	ions: mixed operations	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Solving linear equations using inverse operations involving 1 step with mixed operations with integer solutions	solve linear equations using inverse operations involving 1 step with mixed operations with integer solutions	
NA.G.1 Solve simple linear equations	2	Solving linear equations using inverse operations involving 1 step with mixed operations with integer and non-integer solutions	solve linear equations using inverse operations involving 1 step with mixed operations with integer and non-integer solutions	
	3	Solving linear equations using inverse operations involving 1 step with mixed operations with integer and non-integer solutions	solve linear equations using inverse operations involving 1 step with mixed operations with integer and non-integer solutions	
	Lea	irning Journeys Solving 2-step equation	ns: variable in numerator	
NA.G.1 Solve simple linear equations	1	Solving linear equations using inverse operations involving 2 steps with mixed operations with integer solutions (pronumeral always in numerator position)	solve linear equations using inverse operations involving 2 steps with mixed operations with integer solutions (pronumeral always in numerator position)	
	2	Solving linear equations using inverse operations involving 2 steps with mixed operations with integer and non-integer solutions (pronumeral always in numerator position)	solve linear equations using inverse operations involving 2 steps with mixed operations with integer and non-integer solutions (pronumeral always in numerator position)	
	3	Solving linear equations using inverse operations involving 2 steps with mixed operations with integer and non-integer solutions (pronumeral always in numerator position)	solve linear equations using inverse operations involving 2 steps with mixed operations with integer and non-integer solutions (pronumeral always in numerator position)	
	Lear	ning Journeys Solving 2-step equations	s: variable in denominator	
NA.G.1 Solve simple linear equations	1	Solving linear equations using inverse operations involving 2 steps with mixed operations with integer solutions (pronumeral in numerator or denominator position)	solve linear equations using inverse operations involving 2 steps with mixed operations with integer solutions (pronumeral in numerator or denominator position)	
	2	Solving linear equations using inverse operations involving 2 steps with mixed operations with integer and non-integer solutions (pronumeral in numerator or denominator position)	solve linear equations using inverse operations involving 2 steps with mixed operations with integer and non-integer solutions (pronumeral in numerator or denominator position)	
	3	Solving linear equations using inverse operations involving 2 steps with mixed operations with integer and non-integer solutions (pronumeral in numerator or denominator position)	solve linear equations using inverse operations involving 2 steps with mixed operations with integer and non-integer solutions (pronumeral in numerator or denominator position)	



## **Understanding Practice and Fluency (UPF)**

MA4-9NA operates with positive-integer and zero indices of numerical bases					
Quest: Solving equations					
		Learning Jo	urneys Solving 3-s	tep equations	
Content Descriptor	Steps	Spine Nodes		Subnodes	
	1	Solving linear equations (integer coefficients) using inverse operations involving 3 steps with mixed operations with integer solutions		solve linear equations (integer coefficients) using inverse operations involving 3 steps with mixed operations with integer solutions	
NA.G.2 Solve linear equations using algebraic techniques and verify solutions by	2	Solving linear equation coefficients) using investinvolving 3 steps with with integer and non-i	erse operations mixed operations	solve linear equations (integer coefficients) using inverse operations involving 3 steps with mixed operations with integer and non-integer solutions	
substitution	3	Solving linear equation or decimal coefficients operations involving 3 operations with integer solutions	s) using inverse steps with mixed	solve linear equations (integer, fraction or decimal coefficients) using inverse operations involving 3 steps with mixed operations with integer and non- integer solutions	
	Le	earning Journeys So	olving equations wit	h variable on both sides	
NA.G.2 Solve linear equations using algebraic techniques and verify solutions by substitution	1	Solving linear equations (integer coefficients) using inverse operations involving pronumerals on both sides of the equation		solve linear equations (integer coefficients) using inverse operations involving pronumerals on both sides of the equation	
	2	Solving linear equations (integer, fraction or decimal coefficients) using inverse operations involving pronumerals on both sides of the equation		solve linear equations (integer, fraction or decimal coefficients) using inverse operations involving pronumerals on both sides of the equation	
		Learning Journey	s Solving equation	s involving brackets	
NA.G.2 Solve linear equations using algebraic	1	Solving linear equations (integer coefficients) using inverse operations involving expanding brackets		solve linear equations (integer coefficients) using inverse operations involving expanding brackets	
techniques and verify solutions by substitution	2	Solving linear equations (integer, fraction or decimal coefficients) using inverse operations involving expanding brackets		solve linear equations (integer, fraction or decimal coefficients) using inverse operations involving expanding brackets	
		Learning Journe	e <b>ys</b> Solving basic qu	uadratic equations	
NA.G.3 Solve	Exploring simple quadratic equations		<ul><li>quadratic equation</li><li>understand that the root' operation</li><li>explain why quadra</li></ul>	of then there are 2 values of x that solve a simple of the form x <sup>2</sup> = c inverse operation of squaring a number is the 'square tic equations could be expected to have 2 solutions does not have a solution if c is a negative number	
simple quadratic equations	1	Solving simple quadra integer answers	tic equations with	<ul> <li>solve simple quadratic equations of the form x² = c, leaving answers in 'exact form' and as decimal approximations</li> </ul>	
	2	Solving simple quadratic equations with non-integer answers left as decimals		solve simple quadratic equations with non-integer answers left as decimals	
	3	Solving simple quadratic equations with non-integer answers left in exact form		solve simple quadratic equations with non-integer answers left in exact form	



## **Understanding Practice and Fluency (UPF)**

MA4-9NA operates with positive-integer and zero indices of numerical bases					
	Quest: Relationships & transformations				
		Learning Journeys Using the	e coordinate system		
Content Descriptor	Steps	Spine Nodes	Subnodes		
NA.H.1 Given coordinates, plot points on the Cartesian plane, and find coordinates for a given point	1	Locating points on the Cartesian plane	<ul> <li>plot and label points, given coordinates, in all 4 quadrants of the number plane</li> <li>identify and label each quadrant on a number plane</li> <li>identify and record the coordinates of given points in all 4 quadrants of the number plane</li> </ul>		
	2	Plotting coordinates on the Cartesian plane (not whole numbers)	<ul> <li>plot and label points on the Cartesian plane, given coordinates, including those with coordinates that are not whole numbers</li> <li>identify and record the coordinates of given points on the Cartesian plane, including those with coordinates that are not whole numbers</li> </ul>		
		Learning Journeys Transformation	ons on the cartesian plane		
NA.H.2 Describe translations, reflections in an axis, and rotations of multiples of 90° on the Cartesian plane using coordinates	1	Plotting transformations of points on the Cartesian plane	plot and state the coordinates of the image of a point on the Cartesian plane resulting from 1 or more translations		
	2	Plotting and stating the coordinates of the image of a given point on the Cartesian plane resulting from reflection in either the x-axis or y-axis	plot and state the coordinates of the image of a given point on the Cartesian plane resulting from reflection in either the x-axis or y-axis		
	3	Plotting and stating the coordinates of the image of a given point on the Cartesian plane resulting from rotation of multiples of 90° about the origin	<ul> <li>plot and state the coordinates of the image of a given point on the Cartesian plane resulting from a rotation of 90° about the origin</li> <li>plot and state the coordinates of the image of a given point on the Cartesian plane resulting from a rotation of 180° about the origin</li> <li>plot and state the coordinates of the image of a given point on the Cartesian plane resulting from a rotation of 270° about the origin</li> </ul>		
		Learning Journeys Working w	vith Linear Sequences		
NA.H.3 Plot linear relationships on the Cartesian plane, with and without the use of digital technologies	1	Investigating and extending numeric and geometric patterns represented in a table	<ul> <li>investigate and extend numeric patterns represented in a table</li> <li>investigate and extend geometric patterns represented in a table</li> </ul>		
	2	Finding the nth term of linear sequences arising from a given set of numbers or sequences generated from concrete/visual representations with integer coefficients of n	<ul> <li>find the nth term of increasing linear sequences arising from a given set of numbers or sequences generated from concrete/visual representations with integer coefficients of n</li> <li>find the nth term of decreasing linear sequences arising from a given set of numbers or sequences generated from concrete/visual representations with integer coefficients of n</li> </ul>		



## **Understanding Practice and Fluency (UPF)**

MA4-9NA operates with positive-integer and zero indices of numerical bases				
Quest: Relationships & transformations				
		Learning Journeys Working w	vith Linear Sequences	
Content Descriptor	Steps	Spine Nodes	Subnodes	
	3	Finding the nth term of linear sequences arising from a given set of numbers or sequences generated from concrete/visual representations with decimal coefficients of n	<ul> <li>find the nth term of increasing linear sequences arising from a given set of numbers or sequences generated from concrete/visual representations with decimal coefficients of n</li> <li>find the nth term of decreasing linear sequences arising from a given set of numbers or sequences generated from concrete/visual representations with decimal coefficients of n</li> </ul>	
NA.H.3 Plot linear relationships on the Cartesian plane, with and without the use of digital technologies		Finding the nth term of linear sequences arising from a given set of numbers or sequences generated from concrete/visual representations with fractional coefficients of n	<ul> <li>find the nth term of increasing linear sequences arising from a given set of numbers or sequences generated from concrete/visual representations with fractional coefficients of n</li> <li>find the nth term of a decreasing linear sequences arising from a given set of numbers or sequences generated from concrete/visual representations with fractional coefficients of n</li> </ul>	
	4	Using the nth term rule for a linear series	<ul> <li>use the nth term rule to find missing terms of the sequence, eg 100th term</li> <li>use the nth term rule to determine whether a number exists in a sequence</li> </ul>	
	5	Solving problems involving the use of the nth term formula for a linear sequence	solve problems involving the use of the nth term formula for a linear sequence	
		<b>Learning Journeys</b> Ta	able of values	
NA.H.3 Plot linear relationships on the Cartesian plane, with and without the use of digital technologies  Investigating linear relationships on Cartesian plane (number plane) for number and geometric (spatial) patterns		on Cartesian plane (number plane) for number and geometric (spatial)	<ul> <li>identify a table of values matching a linear relationship plotted on the number plane (with and without digital technology)</li> <li>identify the table of values for a given number pattern that matches the points plotted on a number plane</li> <li>describe the linear relationship and the rules (term-to-term and also position-to-term)</li> </ul>	
Learning Journeys Solving linear equations graphically				
NA.H.4 Solve linear equations using graphical techniques	1	Solving linear equations using graphical techniques	use graphs of linear relationships to solve a corresponding linear equation, with and without the use of digital technologies	
	2	Graph two intersecting lines on the same set of axes and read off the point of intersection	<ul> <li>Use tables of values to plot two straight lines on a single Cartesian planea Use tables of values to plot two straight lines on a single Cartesian plane</li> <li>Read the point of intersection of two plotted straight lines on a single Cartesian plane</li> </ul>	



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA4-12MG calculates the perimeters of plane shapes and the circumferences of circles					
	Quest: Perimeter of quadrilaterals and circles				
		Learning Journeys Findi	ng the perimeter		
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Finding perimeters of special quadrilaterals	<ul> <li>find the perimeter of parallelograms, trapeziums, rhombuses and kites</li> <li>apply knowledge of geometric markings to find the perimeters of special quadrilaterals</li> </ul>		
	2	Solving problems involving perimeters of regular polygons	<ul> <li>solve problems involving the perimeters of regular polygons</li> <li>solve problems involving perimeters of regular polygons with dimensions given in different units</li> </ul>		
MG.A.1 Find perimeters of parallelograms, trapeziums, rhombuses and kites	3	Solving problems involving perimeters of composite polygons	<ul> <li>solve problems involving perimeters of composite polygons formed using only triangles, squares, rectangles or parallelograms</li> <li>solve problems involving perimeters of composite polygons formed using regular polygons</li> <li>solve problems involving perimeters of composite polygons formed using only triangles, squares, rectangles or parallelograms with dimensions given in different units</li> <li>solve problems involving perimeters of composite polygons formed using regular polygons with dimensions given in different units</li> </ul>		
		Learning Journeys Identify	ying parts of circles		
MG.A.3 Investigate the relationship between features of circles, such as the circumference, radius and diameter; use formulas to solve problems involving circumference	1	Identifying parts of a circle	identify and apply circle definitions and properties, including: centre, radius, chord, diameter, circumference, tangent, arc, sector and segment		
Learning Journeys Working with circumferences of circles					
MG.A.3 Investigate the relationship between features of circles such as the	1	Finding circumferences	develop and use the formulas to find the circumferences of circles in terms of the diameter d or radius r		
circles, such as the circumference, radius and diameter; use formulas to solve problems involving circumference	2	Finding the diameter and/or radius of a circle given its circumference	find the diameter and/or radius of a circle given its circumference		



# **Understanding Practice and Fluency (UPF)**

MA4-12M	IG calcı	ulates the perimeters of plane sl	napes and the circumferences of circles		
	Quest: Perimeter of quadrilaterals and circles				
		Learning Journeys Finding perin	neters of parts of circles		
Content Descriptor	Steps	Spine Nodes	Subnodes		
MG.A.3 Investigate the relationship between features of	1	Finding the perimeters of quadrants and semicircles	<ul> <li>find the perimeters of quadrants and semicircles given the appropriate information</li> <li>find the diameter and/or radius of a semicircle/quadrant given the perimeter</li> </ul>		
circles, such as the circumference, radius and diameter; use formulas to solve	2	Finding the perimeters of simple composite figures	find the perimeters of simple composite figures consisting of 2 shapes, including quadrants and semicircles		
problems involving circumference	3	Finding the perimeters of composite figures	<ul> <li>find the perimeters of composite figures containing 3 or more shapes consisting, including quadrants and semicircles</li> </ul>		
	Lear	ning Journeys Finding arc lengtl	hs and perimeters of sectors		
MC A 2 Investigate	1	Finding arc lengths and the perimeters of sectors	<ul> <li>find the arc length of a sectora find the arc length of a sector</li> <li>find the perimeter of a sector</li> </ul>		
MG.A.3 Investigate the relationship between features of circles, such as the circumference, radius and diameter; use	2	Solving problems involving perimeters of sectors	<ul> <li>find the diameter and/or radius of a sector given the arc length and angle</li> <li>find the perimeters of complex composite figures</li> <li>solve problems involving arcs and sectors</li> </ul>		
formulas to solve problems involving circumference	3	Solving problems involving circles with exact answers	• solve a variety of practical problems involving circles and parts of circles, giving an exact answer in terms of $\pi$		
circumierence		Solving problems involving circles with approximate answers	• solve a variety of practical problems involving circles and parts of circles, giving an approximate answer using a calculator's $\boldsymbol{\pi}$ function		
MA4-13MG uses for	mulas	to calculate the areas of quadril area	aterals and circles, and converts between units of		
		Quest: Solving area	a problems		
	L	.earning Journeys Choosing and			
MG.B.1 Choose appropriate units of measurement for area and convert from one unit to another	1	Choosing an appropriate unit to measure the areas of different shapes and surfaces	choose an appropriate unit to measure the areas of different shapes and surfaces, eg floor space, fields		
	2	Converting between different metric units of area (square millimetres, square centimetres, square metres, square kilometres, hectares)	<ul> <li>convert between square millimetres and square centimetres and vice versa</li> <li>convert between square centimetres and square metres and vice versa</li> <li>convert between square metres and hectares and vice versa</li> <li>convert between square metres and square kilometres and vice versa</li> </ul>		



## **Understanding Practice and Fluency (UPF)**

### **Measurement and Geometry**

area					
	Quest: Solving area problems				
	Lea	arning Journeys Solving area pro	blems involving rectangles		
Content Descriptor	Steps	Spine Nodes	Subnodes		
MG.B.2 Establish the formulas for areas of rectangles, triangles and parallelograms and use these in problem solving	1	Applying the formula for the area of a rectangle	<ul> <li>apply the formula for area of a rectangle to find the area of rectangles given 2 side lengths measured in the same or different units</li> <li>apply the formula for area of a rectangle to find the area of composite rectilinear figures, such as an L-shape, U-shape</li> <li>apply the formula to real life contexts</li> </ul>		
	2	Investigating and comparing the areas of rectangles that have the same perimeter	investigate and compare the areas of rectangles that have the same perimeter, eg compare the areas of all possible rectangles with whole-number dimensions and a perimeter of 20 centimetres		
	3	Finding the dimensions of rectangles and squares given their areas	find the possible dimensions of rectangles and squares given their areas		
	Le	arning Journeys Solving area pr	oblems involving triangles		
	1	Applying the formula to find the areas of right-angled triangles	apply the formula to find the areas of right-angled triangles		
	2	Applying the formula to find the areas of non right-angled triangles	<ul> <li>apply the formula to find the areas of triangles in which the perpendicular height meets the base within the length of the base</li> <li>apply the formula to find the areas of triangles in which the perpendicular height meets the base outside the length of the base</li> </ul>		
MG.B.2 Establish the formulas for areas of rectangles, triangles	3	Finding the dimensions of a right- angled triangle given its area	find the dimensions of a right-angled triangle given its area and either its base or height by using the formula for the area of a triangle		
and parallelograms and use these in problem solving	4	Finding the dimensions of a non right-angled triangle given its area	<ul> <li>find the dimensions of non right-angled triangles given its area and either its base or height using the formula for the area of a triangle</li> <li>find the dimensions of non right-angled triangles in which the perpendicular height meets the base outside the length of the base given its area and either its base or height by using the formula for the area of a triangle</li> </ul>		
	5	Solving real-life problems involving calculating the area of triangles	solve real-life problems involving calculating the area of triangles		



## **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

area					
	Quest: Solving area problems				
Learning Journeys Solving area problems involving parallelograms					
Content Descriptor	Steps Spine Nodes Subnodes		Subnodes		
MG.B.2 Establish the formulas for areas of rectangles, triangles and parallelograms and use these in problem solving	1	Finding the area of a parallelogram using a formula	<ul> <li>apply the formula to find the area of parallelograms in different orientations</li> <li>apply the formula to find the area of parallelograms in different orientations which include more dimensions than are necessary to calculate the area</li> </ul>		
	2	Finding the dimensions of a parallelogram given its area	<ul> <li>find the dimensions of a parallelogram given its area and either its length or width by using the formula for the area of a parallelogram</li> <li>find the dimensions of a parallelogram in different orientations given its area and either its length or width by using the formula for the area of a parallelogram</li> </ul>		
	3	Solving real-life problems involving calculating the area of parallelograms	solve real-life problems involving calculating the area of parallelograms		
	Learn	ing Journeys Solving area probl	ems: simple composite figures		
MG.B.2 Establish the formulas for areas of rectangles, triangles and parallelograms and use these in problem solving	1	Calculating the area of composite shapes constructed from triangles and special quadrilaterals	apply area formulas for a variety of composite shapes to calculate their area		
	Lea	rning Journeys Solving area pro	blems involving trapeziums		
MG.B.3 Find areas of trapeziums, rhombuses and kites	1	Finding the area of a trapezium using the formula	<ul> <li>apply the formula to find the areas of trapeziums of different orientations and shapes, including 4 unequal sides with no right angles, 2 right angles and isosceles trapezium</li> <li>apply the formula to find the area of trapeziums in different orientations which include dimensions that are not necessary to calculate the area</li> </ul>		
	2	Finding the dimensions of a trapezium given its area	<ul> <li>find the dimensions of a trapezium given its area and 2 of either its height, roof or base by using the formula for the area of a trapezium</li> <li>find the dimensions of a trapezium in different orientations given its area and 2 of either its height, roof or base by using the formula for the area of a trapezium</li> </ul>		
	3	Solving real-life problems involving calculating the area of trapeziums	solve real-life problems involving calculating the area of trapeziums		



## **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

area				
Quest: Solving area problems				
Learning Journeys Solving area problems involving rhombuses				
Content Descriptor	Steps	Spine Nodes	Subnodes	
MG.B.3 Find areas of trapeziums, rhombuses and kites	1	Finding the area of a rhombus using the formula	<ul> <li>apply the formula to find the area of rhombuses in different orientations</li> <li>apply the formula to find the area of rhombuses in different orientations which include dimensions that are not necessary to calculate the area</li> </ul>	
	2	Finding the dimensions of a rhombus given its area	<ul> <li>find the dimensions of a rhombus given its area by using the formula for the area of a rhombus</li> <li>find the dimensions of a rhombus in different orientations given its area by using the formula for the area of a rhombus</li> </ul>	
	3	Solving real-life problems involving calculating the area of rhombus'	solve real-life problems involving calculating the area of rhombus'	
	ı	Learning Journeys Solving area	problems involving kites	
MG.B.3 Find areas of trapeziums, rhombuses and kites	1	Finding the area of a kite using the formula	<ul> <li>apply the formula to find the area of kites in different orientations</li> <li>apply the formula to find the area of kites in different orientations which include dimensions that are not necessary to calculate the area</li> </ul>	
	2	Finding the dimensions of a kite given its area	<ul> <li>find the dimensions of a kite given its area and either its length or width by using the formula for the area of a kite</li> <li>find the dimensions of a kite in different orientations given its area and either its length or width by using the formula for the area of a kite</li> </ul>	
	3	Solving real-life problems involving calculating the area of kites	solve real-life problems involving calculating the area of kites	
	L	earning Journeys Solving area p	problems involving circles	
MG.B.4 Investigate the relationship between features of circles, such as the area and the radius; use formulas to solve problems involving area	1	Finding the area of a circle using the formula	<ul> <li>apply the formula to find the areas of circles given the radius</li> <li>apply the formula to find the areas of circles given the diameter</li> </ul>	
	2	Finding the dimensions of a circle given its area	<ul> <li>find the radius of a circle given its area using the formula for the area of a circle</li> <li>find the diameter of a circle given its area using the formula for the area of circle</li> </ul>	
	3	Solving real-life problems involving calculating the area of circles	<ul> <li>solve real-life problems involving calculating the area of circles</li> </ul>	



## **Understanding Practice and Fluency (UPF)**

### **Measurement and Geometry**

Quest: Solving area problems				
	Learning Journeys Solving area problems involving parts of circles			
Content Descriptor	Steps	Spine Nodes	Subnodes	
	1	Finding the area of a semicircle or quadrant of a circle	<ul> <li>find the area of a semicircle or quadrant of a circle</li> <li>find the diameter or radius of a semicircle or quadrant given its area</li> <li>find the diameter or radius of a semicircle or quadrant given its area within the context of a problem</li> </ul>	
MG.B.4 Investigate the relationship between features of circles, such as the area and the radius; use formulas to solve	2	Applying the area of a sector formula with angle given in degrees: $A=\square/360*\pi*r^2$	<ul> <li>find the area of a sector using the formula where radius is given and angle is given in degrees</li> <li>find the radius of a sector using the formula where the area is given and angle is given in degrees</li> <li>find the angle of a sector in degrees using the formula where the area and radius are given</li> <li>find the unknown variable using the area of a sector formula in the context of a problem in</li> </ul>	
use formulas to solve problems involving area	3	Finding the area of composite shapes involving circles, semicircles and quadrants	<ul> <li>degrees</li> <li>find the area of composite shapes involving circles, semicircles and quadrants</li> <li>find the area of composite shapes involving circles, semicircles and quadrants within the context of a problem</li> </ul>	
	4	Finding the area of composite shapes involving circles, semicircles and quadrants giving an exact answer in terms of pi	<ul> <li>find the area of composite shapes involving circles, semicircles and quadrants giving an exact answer in terms of pi</li> <li>find the area of composite shapes involving circles, semicircles and quadrants within the context of a problem giving an exact answer in terms of pi</li> </ul>	
MA4-14MG uses fo	rmulas	to calculate the volumes of prisms a volume	and cylinders, and converts between units of	
		Quest: Solving volume p	roblems	
	Lear	ning Journeys Exploring different vi	ews of prisms and solids	
	1	Drawing (in two dimensions) prisms from different views by connecting cubes, including top, side, front and back views	draw from connecting cubes (in two dimensions)     prisms from different views, including top, side,     front and back views	
	2	Drawing (in two dimensions) solids formed from combinations of prisms by connecting cubes, from different views, including top, side, front and back views	<ul> <li>draw from connecting cubes (in two dimensions) solids formed from combinations of prisms, from different views, including top, side, front and back views</li> </ul>	
MG.C.1 Draw different views of prisms and solids formed from combinations of		Drawing (in two dimensions) prisms from different views, including top, side, front and back views	draw (in two dimensions) prisms from different views, including top, side, front and back views	
prisms	3	Drawing (in two dimensions) solids formed from combinations of prisms, from different views, including top, side, front and back views	draw (in two dimensions) solids formed from combinations of prisms, from different views, including top, side, front and back views	
	4	Identifying prisms from their cross- section	identify the cross-sections of different prisms	
	4	Drawing the cross-sections of prisms	draw the cross-sections of prisms	



## **Understanding Practice and Fluency (UPF)**

### **Measurement and Geometry**

MA4-14MG uses formulas to calculate the volumes of prisms and cylinders, and converts between units of

MA4-14MG uses to	rmulas	to calculate the volumes of prisms a volume	and cylinders, and converts between units of		
	Quest: Solving volume problems				
	L	earning Journeys Choosing and cove	rting units of volume		
Content Descriptor	Steps	Spine Nodes	Subnodes		
MG.C.2 Choose	1	Choosing appropriate units to measure the capacities of a variety of containers	choose appropriate units to measure the capacities of a variety of containers, eg millilitres for a drinking glass, litres for a water urn		
appropriate units of measurement for volume and convert			<ul> <li>convert between metric units of volume: 1km<sup>3</sup></li> <li>= 1000000m<sup>3</sup>, 1m<sup>3</sup> = 10000cm<sup>3</sup>, 1cm<sup>3</sup></li> <li>= 1000mm<sup>3</sup></li> </ul>		
from one unit to another	2	Converting between metric units of volume and capacity (mL, L, kL and ML)	• convert between metric units of capacity: 1ML = 1000000L, 1kL = 1000L, 1L = 1000mL		
			<ul> <li>convert between metric units of volume and capacity:</li> <li>1cm³ = 1mL, 1m^3 = 1000L</li> </ul>		
		Learning Journeys Finding the ve	olume of prisms		
	1	Developing methods and formulas to find the volume of any prism	recognise the area of the 'base' of a prism as being identical to the area of its uniform cross-section		
MG.C.3 Develop the formulas for the volumes of rectangular and triangular prisms and of prisms in general; use formulas to solve problems involving volume	2	Finding the volume of prism with a composite/irregular polygon uniform cross-section, given their perpendicular heights and area of their cross-sections all in the same units	find the volume of prism with a composite/ irregular polygon uniform cross-section, given their perpendicular heights and area of their cross- sections all in the same units		
	3	Finding the volume of prism with a composite/irregular polygon with uniform cross-section, given their perpendicular heights and dimensions of the cross-sections all in the same units	find the volume of prism with a composite/irregular polygon with uniform cross-section, given their perpendicular heights and dimensions of the cross- sections all in the same units		
	4	Finding the volume of prism with a composite/irregular polygon uniform cross-section, given their perpendicular heights and area of their cross-sections all in different units	find the volume of prism with a composite/ irregular polygon uniform cross-section, given their perpendicular heights and area of their cross- sections all in different units		
	5	Finding the volume of prism with a composite/irregular polygon with uniform cross-section, given their perpendicular heights and dimensions of the cross-sections all in different units	find the volume of prism with a composite/irregular polygon with uniform cross-section, given their perpendicular heights and dimensions of the cross- sections all in different units		



## **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA4-14MC uses formulas to calculate the volumes of prisms and cylinders, and converts between units of volume

volume						
	Quest: Solving volume problems					
	Learning Journeys Finding the volume of rectangular prisms					
Content Descriptor	Steps	Spine Nodes	Subnodes			
	1	Finding the volumes of rectangular prisms, given their perpendicular heights and the dimensions of their uniform cross-sections	find the volumes of rectangular prisms, given their perpendicular heights and the dimensions of their uniform cross-sections			
MG.C.3 Develop the formulas for		Finding the volume of a rectangular prism given the area of the uniform cross-section and perpendicular height in the same units	find the volume of a rectangular prism given the area of the uniform cross-section and perpendicular height in the same units			
the volumes of rectangular and triangular prisms and	2	Finding the volume of a rectangular prism given the area of the uniform cross-section and perpendicular height in different units	find the volume of a rectangular prism given the area of the uniform cross-section and perpendicular height in different units			
of prisms in general; use formulas to solve problems involving	3	Finding the height/area of the uniform cross-section given the volume in the same units	find the height or area of the uniform cross- section given the volume in the same units			
volume	4	Finding the height/area of the uniform cross-section given the volume in different units	find the height/area of the uniform cross-section given the volume in different units			
		Finding a missing dimension of a rectangular prism given the volume in different units	find a missing dimension of a rectangular prism given the volume in different units			
	L	earning Journeys Finding the volume o	of triangular prisms			
	1	Finding the volume of a triangular prism given the area of the uniform cross-section and perpendicular height in the same units	find the volume of a triangular prism given the area of the uniform cross-section and perpendicular height in the same units			
		Finding the volume of triangular prisms, given their perpendicular heights and dimensions of their uniform cross-sections all in the same units	find the volume of triangular prisms, given their perpendicular heights and dimensions of their uniform cross-sections all in the same units			
MG.C.3 Develop the formulas for	2	Finding the volume of a triangular prism given the area of the uniform cross-section and perpendicular height in different units	find the volume of a triangular prism given the area of the uniform cross-section and perpendicular height in different units			
the volumes of rectangular and triangular prisms and of prisms in general; use formulas to solve problems involving volume		Finding the volume of triangular prisms, given their perpendicular heights and dimensions of their uniform cross-sections all in different units	find the volume of triangular prisms, given their perpendicular heights and dimensions of their uniform cross-sections all in different units			
	3	Finding the volume of triangular prisms, given their perpendicular heights, dimensions of their uniform cross-sections and additional measurements not required for the calculation in the same/ different units	find the volume of triangular prisms, given their perpendicular heights, dimensions of their uniform cross-sections and additional measurements not required for the calculation in the same/ different units			
	4	Finding a missing dimension of a triangular prism given the volume in the same units	find a missing dimension of a triangular prism given the volume in the same units			
	4	Finding a missing dimension of a triangular prism given the volume in different units	find a missing dimension of a triangular prism given the volume in different units			



## **Understanding Practice and Fluency (UPF)**

### **Measurement and Geometry**

MA4-14MG uses formulas to calculate the volumes of prisms and cylinders, and converts between units of volume

		volume	nd cylinders, and converts between units of
		Quest: Solving volume pro	blems
		Learning Journeys Solving problems	involving prisms
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.C.3 Develop the formulas for the volumes of rectangular and triangular prisms and of prisms in general; use formulas to solve problems involving volume	1	Solving a variety of practical problems involving the volumes and capacities of right prisms	<ul> <li>solve a variety of practical problems involving the volumes and capacities of right prisms</li> <li>find the height or area of a prism with a composite/irregular polygon with uniform cross-section given the volume in the same units</li> <li>find the height or area of a prism with a composite/irregular polygon with uniform cross-section given the volume in different units</li> </ul>
		Learning Journeys solving problems in	nvolving cylinders
MG.C.4 Calculate the volumes of cylinders and solve related problems	1	Using the formula to find the volumes of cylinders	<ul> <li>find the volume of a right cylinder given the area of the circle cross-section and perpendicular height in the same units</li> <li>find the volume of a right cylinder given the area of the circle cross-section and perpendicular height in different units</li> </ul>
	2	Finding the height or area of the circle cross-section for a right cylinder given the volume in the same units	<ul> <li>find the height or area of the circle cross-section for a right cylinder given the volume in the same units</li> <li>find the height or area of the circle cross-section for a right cylinder given the volume in different units</li> </ul>
	3	Finding the volume of right cylinders, given their perpendicular heights and radius/diameter of their circular cross-sections all in the same units	<ul> <li>find the volume of right cylinders, given their perpendicular heights and radius/diameter of their circular cross-sections all in the same units</li> <li>find the volume of right cylinders, given their perpendicular heights and radius/diameter of their circular cross-sections all in different units</li> </ul>
	4	Finding the radius, diameter or height of right cylinders, given their volume all in the same units	<ul> <li>find the radius, diameter or height of right cylinders, given their volume all in the same units</li> <li>find the radius, diameter or height of right cylinders, given their volume all in different units</li> </ul>
	5	Solving a variety of practical problems involving the volume and capacity of right prisms and cylinders	solve a variety of practical problems involving the volumes and capacities of right prisms and cylinders



# **Understanding Practice and Fluency (UPF)**

MA4-15MG performs calculations of time that involve mixed units, and interprets time zones			
		Quest: Working with time and	timezones
		Learning Journeys Solving problems	s involving time
Content Descriptor	Steps	Spine Nodes	Subnodes
	1	Ordering a series of events according to the time taken to complete each one	order a series of events according to the time taken to complete each one
	2	Calculating the elapsed time of events using start and finish times using only 12-hour time	calculate the elapsed time of events using start and finish times using only 12-hour time
	2	Calculating the elapsed time of events using start and finish times using 12-hour and 24-hour time	calculate the elapsed time of events using start and finish times using 12-hour and 24-hour time
MG.C.3 Develop	3	Calculating the starting time of events given the elapsed time and the finishing time using only 12-hour time	calculate the starting time of events given the elapsed time and the finishing time using only 12-hour time
the formulas for the volumes of rectangular and triangular prisms and		Calculating the starting time of events given the elapsed time and the finishing time using 12-hour and 24-hour time	<ul> <li>calculate the starting time of events given the elapsed time and the finishing time using 12- hour and 24-hour time</li> </ul>
of prisms in general; use formulas to solve problems involving	4	Calculating the finishing time of events given the elapsed time and the finish times using only 12-hour time	<ul> <li>calculate the finishing time of events given the elapsed time and the finish times using only 12- hour time</li> </ul>
volume		Calculating the finishing time of events given the elapsed time and the finish times using only 12-hour and 24-hour time	<ul> <li>calculate the finishing time of events given the elapsed time and the finish times using 12-hour and 24-hour time</li> </ul>
	5	Solving problems within a given context involving starting and finishing times of events and elapsed time using only 12-hour time	solve problems within a given context involving starting and finishing times of events and elapsed time using only 12-hour time
		Solving problems within a given context involving starting and finishing times of events and elapsed time using 12-hour and 24-hour time	solve problems within a given context involving starting and finishing times of events and elapsed time using 12-hour and 24-hour time



# **Understanding Practice and Fluency (UPF)**

MA4-15MG performs calculations of time that involve mixed units, and interprets time zones			
		Quest: Working with time and	timezones
		Learning Journeys Rounding and c	converting time
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.D.1 Solve	1	Introducing the calculator button degrees, minutes, seconds	add and subtract time using the 'degrees- minutes-seconds' button on the calculator
problems involving duration, including	2	Rounding time measurements to the nearest hour, minute or second	round time measurements to the nearest hour, minute or second
using 12-hour and 24-hour time within a	3	Converting time given in decimal form into hours, minutes and seconds	convert time given in decimal form into hours, minutes and seconds
single time zone	4	Converting time given in hours, minutes and seconds into decimal form	convert time given in hours, minutes and seconds into decimal form
	L	earning Journeys Solving problems in	nvolving time zones
MG.D.2 Solve problems involving international time zones		Calculating different time zones using a	<ul> <li>use a map of the world showing different time zones to calculate the time difference between 2 different ta use a map of the world showing different time zones to calculate the time difference between 2 different time zones of the world (ignoring seasonal time shifts)</li> </ul>
	1	map	• use a map of the world showing different time zones to calculate the time in another part of the world (ignoring seasonal time shifts) given a time in a particular place (12-hour and 24-hour time) ime zones of the world (ignoring seasonal time shifts)
	2	Comparing the local times in various time zones, including during daylight saving	compare the local times in various time zones, including during daylight saving
	3	Solving problems involving time duration between different time zones on the same date	solve problems involving time duration between different time zones on the same date
	4	Solving problems involving time duration between different time zones on different dates	solve problems involving time duration between different time zones on the different dates



# **Understanding Practice and Fluency (UPF)**

MA4-16MG appl	ies Pytł	nagoras' theorem to calculate side leng related problems	gths in right-angled triangles, and solves
		Quest: Pythagoras' Theo	rem
	Le	arning Journeys Identifying sides on ri	ight-angled triangles
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.E.1 Investigate	1	Identifying the hypotenuse as the longest side in any right-angled triangle and also as the side opposite the right angle	identify the hypotenuse as the longest side in any right-angled triangle and also as the side opposite the right angle
Pythagoras' theorem and its application to solving simple problems involving right-angled triangles	2	Identifying and labelling sides of a right- angled triangle without any angle measures given	<ul> <li>identify and label the hypotenuse and the 2 shorter sides of a right-angled triangle</li> <li>label the hypotenuse c and the shorter sides a and b in a right-angled triangle</li> <li>label the hypotenuse c and the shorter sides a and b in a right-angled triangle within a given context</li> </ul>
	Lea	rning Journeys Exploring the sides of a	a right-angled triangle
MG.E.1 Investigate Pythagoras' theorem and its application to solving simple problems involving right-angled triangles	1	CLASSROOM BASED	
	Learni	ng Journeys Finding a shorter side usi	ng Pythagoras' Theorem
	1	Finding the length of an unknown side (shorter sides only) using Pythagoras' theorem	find the length of an unknown side (shorter sides only) using Pythagoras' theorem
MG.E.1 Investigate Pythagoras' theorem and its application	2	Finding the length of an unknown side (shorter sides only) using Pythagoras' theorem rounding answers	find the length of an unknown side (shorter sides only) using Pythagoras' theorem rounding answers
to solving simple problems involving right-angled triangles	3	Finding the length of an unknown side (shorter sides only) using Pythagoras' theorem in a variety of practical problems within a given context with and without diagrams given	find the length of an unknown side (shorter sides only) using Pythagoras' theorem in a variety of practical problems within a given context with and without diagrams given
I	Learnin	g Journeys Finding the hypotenuse us	ing Pythagoras' Theorem
	1	Finding the length of an unknown side (hypotenuse only) using Pythagoras' theorem	find the length of an unknown side (hypotenuse only) using Pythagoras' theorem
MG.E.1 Investigate Pythagoras' theorem and its application	2	Finding the length of an unknown side (hypotenuse only) using Pythagoras' theorem rounding answers	find the length of an unknown side (hypotenuse only) using Pythagoras' theorem rounding answers
to solving simple problems involving right-angled triangles	3	Finding the length of an unknown side (hypotenuse only) using Pythagoras' theorem in a variety of practical problems within a given context with and without diagrams given	find the length of an unknown side (hypotenuse only) using Pythagoras' theorem in a variety of practical problems within a given context with and without diagrams given



### **Understanding Practice and Fluency (UPF)**

#### Measurement and Geometry

right-angled triangles

MA4-16MG applies Pythagoras' theorem to calculate side lengths in right-angled triangles, and solves related problems Quest: Pythagoras' Theorem Learning Journeys Solving problems involving Pythagoras' Theorem Content **Steps Spine Nodes Subnodes** Descriptor Finding the length of an unknown side • find the length of an unknown side (shorter side (shorter side and hypotenuse) using and hypotenuse) using Pythagoras' theorem Pythagoras' theorem 1 Finding the length of an unknown side • find the length of an unknown side (shorter side (shorter side and hypotenuse) using and hypotenuse) using Pythagoras' theorem Pythagoras' theorem rounding answers rounding answers Finding the length of an unknown side • find the length of an unknown side (shorter side (shorter side and hypotenuse) using and hypotenuse) using Pythagoras' theorem in 2 Pythagoras' theorem in a variety of a variety of practical problems within a given practical problems within a given context MG.E.1 Investigate context with and without diagrams given with and without diagrams given Pythagoras' theorem • solve a variety of practical problems within given and its application contexts involving finding missing sides to solving simple problems involving • solve a variety of practical problems within given Solving a variety of practical problems right-angled triangles contexts involving calculating perimeters involving Pythagoras' Theorem within given 3 contexts involving finding missing sides and solve a variety of practical problems within given calculating perimeters with and without contexts including when sides have different diagrams given solve a variety of practical problems within given contexts including when diagrams are not given Solving a variety of problems involving solve a variety of problems involving unknown unknown lengths in two-dimensional 4 lengths in two-dimensional shapes that contain shapes that contain right-angled triangles right-angled triangles within them within them **Learning Journeys** Exploring Pythagorean Triads MG.E.1 Investigate • idea identify a Pythagorean triad as a set of 3 Pythagoras' theorem numbers that satisfy Pythagoras' theorem and its application Identifying a Pythagorean triad as a set of 3 1 establish new Pythagorean triads by starting to solving simple numbers that satisfy Pythagoras' theorem with another ntify a Pythagorean triad as a set of problems involving 3 numbers that satisfy Pythagoras' theorem right-angled triangles **Learning Journeys** Using the Converse of Pythagoras' Theorem use the converse of Pythagoras' theorem to MG.E.1 Investigate establish whether a triangle is a right-angled Pythagoras' theorem and its application Using the converse of Pythagoras' theorem 1 use the converse of Pythagoras' theorem to to solving simple to solve problems establish whether a triangle is a right-angled problems involving triangle for a practical problem within a given



## **Understanding Practice and Fluency (UPF)**

## **Measurement and Geometry**

	es Pytr	related problems	gths in right-angled triangles, and solves
		Quest: Pythagoras' Theo	rem
		Learning Journeys Exploring irrationa	al numbers (surds)
Content Descriptor	Steps	Spine Nodes	Subnodes
	1	Describing, informally, the properties of irrational numbers	describe, informally, the properties of irrational numbers
MG.E.2 Investigate the concept of irrational numbers	2	Using rational approximations of irrational numbers to compare the size of irrational numbers	use rational approximations of irrational numbers to compare the size of irrational numbers
	3	Approximating the location of irrational numbers on a number line	• approximate the location of irrational numbers on a number line
L	earnin	g <b>Journeys</b> Solving Pythagoras' Theore	em problems: exact values
	1	Finding the length of an unknown side (shorter sides only) using Pythagoras' theorem leaving answers in surd form (exact form)	find the length of an unknown side (shorter side only) using Pythagoras' theorem leaving answer in surd form (exact form)
MC F 2 Investigate the	2	Finding the length of an unknown side (hypotenuse only) using Pythagoras' theorem leaving answers in surd form (exact form)	find the length of an unknown side (hypotenuse only) using Pythagoras' theorem leaving answer in surd form (exact form)
MG.E.2 Investigate the concept of irrational numbers	3	Finding the length of an unknown side (shorter side and hypotenuse) using Pythagoras' theorem leaving answers in surd form (exact form)	find the length of an unknown side (shorter side and hypotenuse) using Pythagoras' theorem leaving answers in surd form (exact form)
	4	Finding the length of an unknown side (shorter side and hypotenuse) using Pythagoras' theorem in a variety of practical problems within a given context, with and without diagrams given, with answers given in surd form	find the length of an unknown side (shorter side and hypotenuse) using Pythagoras' theorem in a variety of practical problems within a given context, with and without diagrams given, with answers given in surd form
MA4-17MG classi	fies, de cor		ngles and quadrilaterals, and determines e lengths and angles
		Quest: Triangles and quadr	ilaterals
		Learning Journeys Labelling and nar	ning conventions
MG.F.1 Classify triangles according to their side and angle properties and describe quadrilaterals	1	Labelling common shapes	<ul> <li>label and name triangles         (eg triangle ABC or ΔABC) and quadrilaterals         (eg ABCD) in text and on diagrams</li> <li>use the common conventions to mark         equal intervals on diagrams</li> </ul>
		Learning Journeys Properties	of triangles
MG.F.1 Classify triangles according to their side and angle properties	1	Classifying types of triangles	<ul> <li>recognise and classify types of triangles on the basis of their properties (acute-angled, right- angled, obtuse-angled, equilateral, isosceles and scalene triangles)</li> <li>recognise that a given triangle may belong to</li> </ul>
angle properties and describe quadrilaterals	2	Sketching and labelling triangles from a worded or verbal description	more than 1 class     determine whether the triangle exists according to its physical description.

worded or verbal description

to its physical description



## **Understanding Practice and Fluency (UPF)**

### **Measurement and Geometry**

MA4-17MG classifies, describes and uses the properties of triangles and quadrilaterals, and determines congruent triangles to find unknown side lengths and angles

congruent triangles to find unknown side lengths and angles					
Quest: Triangles and quadrilaterals					
	L	earning Journeys Convex and non-co	nvex quadrilaterals		
Content Descriptor	Steps	Spine Nodes	Subnodes		
MG.F.1 Classify triangles according to their side and angle properties and describe quadrilaterals	1	Distinguishing between convex and non- convex quadrilaterals	<ul> <li>distinguish between convex and non-convex quadrilaterals ua distinguish between convex and non-convex quadrilaterals using the fact that the diagonals of a convex quadrilateral lie inside the figure</li> <li>distinguish between convex and non-convex quadrilaterals using the fact that a non-convex quadrilateral that has an interior angle greater than 180 degrees sing the fact that the diagonals of a convex quadrilateral lie inside the figure</li> </ul>		
		Learning Journeys Properties of o	quadrilaterals		
	1	Investigating properties of special quadrilaterals: rectangles	prove a quadrilateral is a rectangle using properties		
MG.F.1 Classify		Investigating properties of special quadrilaterals: squares	prove a quadrilateral is a square using properties		
triangles according to their side and	2	Investigating properties of special quadrilaterals: parallelograms	prove a quadrilateral is a parallelogram using properties		
angle properties and describe	3	Investigating properties of special quadrilaterals: rhombuses	prove a quadrilateral is a rhombus using properties		
quadrilaterals	4	Investigating properties of special quadrilaterals: trapeziums/trapezoids	prove a quadrilateral is a trapezium using properties		
	5	Investigating properties of special quadrilaterals: kites	prove a quadrilateral is a kite using properties		
	Learnir	ng Journeys Reasoning, sketching and	describing quadrilaterals		
MG.F.1 Classify triangles according to their side and angle properties and describe quadrilaterals	1	Reasoning about special quadrilaterals on the basis of their properties	<ul> <li>classify a set of quadrilaterals based on their properties</li> <li>identify a given quadrilateral from its description</li> <li>identify a given quadrilateral from a diagram</li> </ul>		
	2	Describing special quadrilaterals	describe a quadrilateral in sufficient detail for it to be sketched		
	3	Reasoning about triangles and special quadrilaterals	<ul> <li>use the properties of special triangles and quadrilaterals to solve simple numerical problems with appropriate reasoning</li> <li>recognise special types of triangles and quadrilaterals embedded in composite figures or drawn in various orientations</li> </ul>		



## **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA4-17MG classifies, describes and uses the properties of triangles and quadrilaterals, and determines congruent triangles to find unknown side lengths and angles

congruent triangles to find unknown side lengths and angles					
Quest: Triangles and quadrilaterals					
Learning Journeys Line and rotational symmetry					
Content Descriptor	Steps	Spine Nodes	Subnodes		
MG.F.2 Identify line and rotational symmetries	1	Identifying line symmetry	<ul> <li>identify, draw and determine the total number of lines of symmetry on designs and shapes, including special triangles, quadrilaterals and polygons</li> <li>complete symmetrical designs and shapes given their line of symmetry</li> </ul>		
	2	Determining rotational symmetry	<ul> <li>dea determine whether or not given shapes and designs have rotational symmetry</li> <li>determine the order of rotational symmetry for given shapes and designs termine whether or not given shapes and designs have rotational symmetry</li> </ul>		
	3	Determining lines (axes) of symmetry and the order of rotational symmetry of polygons, including the special quadrilaterals	determine if particular triangles and quadrilaterals have line and/or rotational symmetry		
	4	Investigating the line and rotational symmetries of circles and of diagrams involving circles, such as a sector or a circle with a marked chord or tangent	investigate if a particular circle with a marked chord or tangent, sector of a circle or a regular circle has a line and/or rotational symmetry		
	5	Identifying line and rotational symmetries in pictures and diagrams	identify if a picture or diagram has a line and/or rotational symmetry		
	Learı	ning Journeys Solving problems involv	ing interior angle sums		
MG.F.3 Demonstrate that the angle sum of a triangle is 180°	1	Exploring and proving the interior angle sum of a triangle	calculate an unknown angle represented by a variable within a triangle, given the other 2 angles		
and use this to find the angle sum of a quadrilateral	2	Finding the interior angle sum of a quadrilateral	calculate an unknown angle/s represented by a variable/s within quadrilaterals, given the appropriate angles		
Learning Journeys Using properties of triangles & quadrilaterals					
MG.F.4 Use the properties of special triangles and quadrilaterals to solve simple numerical problems with appropriate reasoning	1	Reasoning about triangles and special quadrilaterals	<ul> <li>use the properties of special triangles and quadrilaterals to solve simple numerical problems with appropriate reasoning</li> <li>recognise special types of triangles and quadrilaterals embedded in composite figures or drawn in various orientations</li> </ul>		
	2	Determining unknown sides and angles embedded in diagrams, using the properties of special triangles and quadrilaterals, giving reasons	determine unknown sides and angles embedded in diagrams, using the properties of special triangles and quadrilaterals, giving reasons		



## **Understanding Practice and Fluency (UPF)**

### **Measurement and Geometry**

MA4-17MC classifies, describes and uses the properties of triangles and quadrilaterals, and determines

MA4-17MG classifies, describes and uses the properties of triangles and quadrilaterals, and determines congruent triangles to find unknown side lengths and angles					
Quest: Triangles and quadrilaterals					
	L	earning Journeys Defining and workir	ng with congruence		
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Identifying congruent figures by superimposing them through a combination of rotations, reflections and translations	identify congruent figures by superimposing them through a combination of rotations, reflections and translations		
MG.F.5 Define congruence of	2	Matching sides and angles of 2 congruent polygons	determine which angles and sides of a polygon are matched to another polygon's sides and angles		
plane shapes using transformations	3	Determining the condition for 2 circles or parts of circles to be congruent	<ul> <li>determine when 2 circles are congruent according to their radii/diameters</li> <li>determine when 2 semi-circles are congruent according to their radii/diameters</li> <li>determine when 2 sectors are congruent according to equal internal angles at the centre and radii/diameters</li> </ul>		
		Learning Journeys Determining congr	ruence in triangles		
	1	Determining if 2 triangles are congruent using the SSS test	use the SSS test to determine if 2 or more triangles are congruent		
	2	Determining if 2 triangles are congruent using the SAS test	use the SAS test to determine if 2 or more triangles are congruent		
	3	Determining if 2 triangles are congruent using the AAS test	use the AAS test to determine if 2 or more triangles are congruent		
MG.F.6 Develop the conditions for	4	Determining if 2 triangles are congruent using the RHS test	use the RHS test to determine if 2 or more triangles are congruent		
congruence of triangles	5	Determining if 2 triangles are congruent using the SSS, SAS, AAS and RHS test	<ul> <li>identify which test to use to determine congruence of triangles</li> <li>use the SSS, SAS, AAS and RHS tests to determine if 2 or more triangles are congruent</li> </ul>		
	3	Using the congruency tests to identify a pair of congruent triangles from a selection of 3 or more triangles or from triangles embedded in a diagram	<ul> <li>use the congruency tests (SSS, SAS, AAS, RHS) to identify a pair of congruent triangles from a selection of 3 or more triangles or from triangles embedded in a diagram</li> </ul>		
Learning Journeys Using properties of congruent triangles					
MG.F.7 Establish properties of quadrilaterals using congruent triangles and angle properties, and solve related numerical problems using reasoning	1	Applying the properties of congruent triangles to find an unknown side and/or angle in a diagram, giving a reason	apply the properties of congruent triangles to determine a missing angle or length by observing a congruent triangle that has the matching length or angle		



## **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA4-18MG identifies and uses angle relationships, including those related to transversals on sets of parallel lines

		Quest: A	ngle relationships
		Learning Journe	eys Geometry conventions
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.G.1 Use the language, notation and conventions of geometry	1	Using the language and conventions of geometry	<ul> <li>define, name, label and draw points using capital letters</li> <li>define, name, label and draw lines using capital letters</li> <li>define, name, label and draw rays using capital letters</li> <li>define, name, label and draw line segments using capital letters</li> <li>define, name, label and draw angles using capital letters</li> <li>name, label and draw triangles using capital letters</li> <li>name, label and draw quadrilaterals and other polygons using capital letters</li> <li>use common conventions to label right angles and equal angles on diagrams</li> <li>use common conventions to label equal line segments on diagrams</li> </ul>
		Learning lou	rneys Angles at a point
		Investigating and defining complementary angles	<ul> <li>investigate, with and without digital technology, adjacent angles that form a right angle and establish that they add to 90°</li> <li>define complementary angles and identify them in diagrams</li> </ul>
	1	Calculating complementary angles	calculate the size of an unknown angle in a diagram and explain how this is done (using complementary angles)
	1	Investigating and defining supplementary angles	<ul> <li>investigate, with and without digital technology, adjacent angles that form a straight angle and establish that they add to 180°</li> <li>define supplementary angles and identify them in diagrams</li> </ul>
		Calculating supplementary angles	calculate the size of an unknown angle in a diagram and explain how this is done (using supplementary angles)
	2	Investigating and identifying adjacent angles	<ul><li>investigate features of adjacent angles</li><li>identify adjacent angles within a diagram</li></ul>
MG.G.2 Recognise	3	Investigating angles at a point that form angles of revolution	• investigate, with and without digital technology, angles at a point that form an angle of revolution and establish that they add to 360°
the geometrical properties of angles at a point		Calculating where angles form a revolution	<ul> <li>calculate the size of an unknown angle in a diagram and explain how this is done (using knowledge of angles that add to 360°)</li> <li>understand the ambiguity when labelling the reflex angle when 2 angles make up an angle of revolution</li> </ul>
	4	Identifying and naming right angles, straight angles, vertically opposite angles and angles of complete revolution embedded in diagrams	identify and name right angles, straight angles, vertically opposite angles and angles of complete revolution embedded in diagrams
	5	Applying geometric reasoning for adjacent angle relationships	<ul> <li>apply theorems of complementary angles, supplementary angles, vertically opposite and adjacent angles, calculating unknown angles</li> <li>apply theorems for adjacent angles represented by variables in multi-step problems, writing equations to solve for an unknown angle, checking the reasonableness of the answer</li> <li>apply theorems of complementary angles, supplementary angles, vertically opposite and adjacent angles in multi-step problems,</li> </ul>



### **Understanding Practice and Fluency (UPF)**

#### Measurement and Geometry

MA4-18MG identifies and uses angle relationships, including those related to transversals on sets of parallel lines **Quest: Angle relationships** Learning Journeys Parallel and perpendicular line conventions **Content Steps Spine Nodes Subnodes** Descriptor • name and record perpendicular lines using the conventional MG.G.3 Identify notationa name and record perpendicular lines using the corresponding, conventional notation alternate and co-Identifying perpendicular interior angles when define parallel lines and identify them in pictures, designs, and parallel lines two straight lines diagrams and the environment, using conventional notation to are crossed by a mark them transversal • name and record parallel lines using the conventional notation **Learning Journeys** Angle relationships on parallel lines • define, identify and draw transversals on sets of 2 or more parallel explore, through measurement, the relationships between pairs of angles formed when a transversal is drawn on a pair of parallel Exploring special pairs of 1 define and identify pairs of equal corresponding angles when 2 or angles on parallel lines more parallel lines are cut by a transversal • define and identify pairs of equal alternate angles when 2 or more parallel lines are cut by a transversal • define and identify pairs of supplementary cointerior angles when 2 or more parallel lines are cut by a transversal MG.G.3 Identify apply geometric reasoning with corresponding angles on parallel corresponding, Applying geometric alternate and coreasoning with lines 2 interior angles when corresponding angles on • use corresponding angles on parallel lines to calculate unknown two straight lines parallel lines angles represented by variables are crossed by a • apply geometric reasoning with alternate angles on parallel lines Applying geometric transversal 3 reasoning with alternate • use alternate angles on parallel lines to calculate unknown angles angles on parallel lines represented by variables Applying geometric • apply geometric reasoning with cointerior angles on parallel lines reasoning with co-4 use cointerior angles on parallel lines to calculate unknown angles interior angles on parallel represented by variables Applying geometric apply geometric reasoning with angles on parallel lines by choosing reasoning with angles on the appropriate angle relationship 5 parallel lines by choosing choose and apply the appropriate angle property to calculate the appropriate angle unknown angles on parallel lines represented by variables relationship **Learning Journeys** Proving parallel lines Understanding that corresponding, alternate and cointerior angles are understand that corresponding, alternate and cointerior angles are 1 not limited to when a not limited to when a transversal cuts a set of parallel lines MG.G.4 Investigate transversal cuts a set of conditions for two parallel lines lines to be parallel • prove or disprove that a pair of lines are parallel using the 2 Proving lines are parallel relationships between corresponding angles, alternate angles, and cointerior angles



# **Understanding Practice and Fluency (UPF)**

MA4-18MG identifi	es and		including those related to transversals on sets of parallel lines
		Quest: Ang	lle relationships
	Lea	rning Journeys Geometri	c reasoning using angle properties
Content Descriptor	Steps	Spine Nodes	Subnodes
MG.G.5 Solve simple numerical problems using reasoning	1	Applying geometric reasoning with angles at a point and angles on parallel lines	apply theorems of angles at a point and angles on parallel lines to solve numerical geometric problems involving up to 3 theorems/steps, giving a reason for each step of the solution
		Quest: Interpreting	g and representing data
		Learning Journ	neys Collecting data
SP.A.1 Investigate techniques for collecting data, including census, sampling and observation	1	Classifying data/recognising variables as categorical (qualitative) or numerical (quantitative) - either discrete or continuous	<ul> <li>identify examples of categorical variables (eg colour, gender) discrete numerical variables (eg number of students, shoe size) and continuous numerical variables (eg height, weight)</li> <li>recognise that data collected on a rating scale (Likert-type scale) is categorical, eg 1 = dislike, 2 = neutral, 3 = like</li> </ul>
	2	Recognising and explaining the difference between a 'population' and a 'sample' selected from a population when collecting data	recognise and explain the difference between a 'population' and a 'sample' selected from a population when collecting data
	3	Investigating and determine the differences between collecting data by observation, census and sampling	<ul> <li>identify examples of variables for which data could be collected by observation, eg direction travelled by vehicles arriving at an intersection, native animals in a local area</li> <li>identify examples of variables for which data could be collected by a census or by a sample, eg a census to collect data about the income of Australians, a sample for TV ratings</li> <li>discuss the practicalities of collecting data through a census compared to a sample, including limitations due to population size, eg in countries such as China and India, a census is conducted only once per decade</li> </ul>
		Learning Journeys	Exploring data sampling
SP.A.2 Explore the practicalities and implications of obtaining data through sampling using a variety of investigative processes	CLASSF	ROOM BASED	
I	earnin	<b>g Journeys</b> The relationsh	nip between a sample & the population
SP.A.2 Explore the practicalities and implications of obtaining data through sampling using a variety of investigative processes	1	Using samples to make predictions about a larger 'population' from which the sample comes	<ul> <li>use samples to make predictions about a larger 'population' from which the sample comes</li> <li>discuss whether a prediction about a larger population, from which a sample comes, would be the same if a different sample were used</li> </ul>
	2	Inferring properties of populations or distributions from a sample, whilst knowing the limitations of sampling	infer properties of populations or distributions from a sample, whilst knowing the limitations of sampling
		Investigating ways in which different random samples may be drawn from the same population	investigate ways in which different random samples may be drawn from the same population, eg random samples from a census may be chosen by gender, postcode, state, etc  1



### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

compare a range

of data displays,

leaf plots and dot

plots

including stem-and-

MA4-18MG identifies and uses angle relationships, including those related to transversals on sets of parallel lines Quest: Interpreting and representing data Learning Journeys Issues with data from primary & secondary sources Content **Spine Nodes** Subnodes **Steps** Descriptor • identify and investigate issues involving numerical data collected Identifying and investigating from primary and secondary sources issues involving numerical 1 identify the difference between data collected from primary and data collected from primary secondary sources, eg data collected in the classroom compared and secondary sources SP.A.3 Identify and with data drawn from a media source investigate issues discuss the effect of different sample sizes involving numerical describe, in practical terms, how a random sample may be data collected Exploring issues involved in from primary and selected in order to collect data about a matter of interest constructing and conducting secondary sources surveys, such as sample detect and discuss bias, if any, in the selection of a sample size, bias, type of data explore issues around the type of data collected in a survey required, and ethics explore the ethics involved in constructing and conducting **Learning Journeys** Collecting and interpreting data Constructing appropriate construct a recording sheet that allows efficient collection of the survey questions and a different types of data expected related recording sheet in order to collect both refine questions in a survey after trialling the survey numerical and categorical decide whether a census or a sample is more appropriate to data about a matter of collect the data required to investigate the matter of interest interest collect and interpret information from secondary sources, presented as tables and/or graphs, about a matter of interest, eg sporting data, information about the relationship between wealth or education and the health of populations of different • interpret and use scales on graphs, including those where Collecting and interpreting SP.A.3 Identify and abbreviated measurements are used, eg '50' on a vertical axis information from secondary investigate issues representing thousands is interpreted as '50 000' involving numerical sources, presented as tables and/or graphs, about a data collected • analyse a variety of data displays used in the print or digital from primary and matter of interest media and in other school subject areas, eg share movement secondary sources graphs, data displays showing sustainable food production identify features on graphical displays that may mislead and result in incorrect interpretation, eg displaced zeros, the absence of labelling on 1 or both axes, potentially misleading units of measurement Using spreadsheets or use spreadsheets or statistical software packages to tabulate 3 statistical software packages and graph data to tabulate and graph data Discussing ethical issues that may arise from · discuss ethical issues that may arise from collecting and 4 collecting and representing representing data Learning Journeys Tallies and frequency distribution tables SP.A.4 Construct and

into a frequency distribution | • use a tally to organise data into a frequency distribution table

Using a tally to organise data

table



#### **Understanding Practice and Fluency (UPF)**

#### **Measurement and Geometry**

MA4-18MG identifies and uses angle relationships, including those related to transversals on sets of parallel lines Quest: Interpreting and representing data Learning Journeys Frequency histograms and polygons **Content Steps Spine Nodes Subnodes** Descriptor Interpreting a discrete data 1 set from its histogram and • interpret a discrete data set from its histogram and polygon SP.A.4 Construct and polygon compare a range construct and interpret frequency histograms and polygons of data displays, including stem-and- select and use appropriate scales and labels on horizontal Constructing and interpreting leaf plots and dot 2 frequency histograms and and vertical axes plots polygons recognise why a half-column-width space is necessary between the vertical axis and the first column of a histogram **Learning Journeys** Frequency histograms and polygons: grouped data Interpreting a discrete data set from its histogram and interpret a discrete data set from its histogram and polygon 1 polygon where grouping is where grouping is required SP.A.4 Construct and required compare a range Constructing histograms construct histograms for discrete data sets where grouping is of data displays, 2 for discrete data sets where including stem-andrequired grouping is required leaf plots and dot Constructing combined plots · construct combined histograms and polygons for discrete histograms and polygons 3 data sets where grouping is required for discrete data sets where grouping is required Learning Journeys Dot plots SP.A.4 Construct and 1 Interpreting dot plots interpret dot plots compare a range of data displays, including stem-and- construct dot plots leaf plots and dot 2 Constructing dot plots • explain the importance of aligning data points when plots constructing dot plots **Learning Journeys** Ordered stem-and-leaf plots Interpreting ordered steminterpret ordered stem-and-leaf plots with whole numbers and-leaf plots with whole 1 numbers and simple decimal and simple decimal values SP.A.4 Construct and compare a range Constructing ordered stem-• construct ordered stem-and-leaf plots with whole numbers of data displays, 2 and-leaf plots with whole including stem-andonly numbers leaf plots and dot Constructing ordered stemplots and-leaf plots with whole construct ordered stem-and-leaf plots with whole numbers 3 numbers and simple decimal and simple decimal values values Learning Journeys Divided bar graphs Interpreting divided bar graphs interpret divided bar graphs Constructing divided bar SP.A.4 Construct and construct divided bar graphs with the use of digital graphs with the use of digital 2 compare a range technology technology of data displays, including stem-and-• construct divided bar graphs without the use of digital Constructing divided bar leaf plots and dot technology graphs without the use of 3 plots calculate the length of the bar required for each section of digital technology divided bar graphs



#### **Understanding Practice and Fluency (UPF)**

digital technology

#### **Measurement and Geometry**

MA4-18MG identifies and uses angle relationships, including those related to transversals on sets of parallel lines Quest: Interpreting and representing data **Learning Journeys** Sector graphs **Content Steps Spine Nodes Subnodes** Descriptor Interpreting sector graphs · interpret sector graphs SP.A.4 Construct and Constructing sector graphs compare a range 2 with the use of digital construct sector graphs with the use of digital technology of data displays, technology including stem-and- construct sector graphs without the use of digital technology Constructing sector graphs leaf plots and dot 3 without the use of digital • calculate the angle at the centre required for each sector of plots technology sector graphs **Learning Journeys** Line graphs SP.A.4 Construct and 1 Interpreting line graphs · interpret line graphs compare a range of data displays, including stem-and-Constructing line graphs with 2 construct line graphs with the use of digital technology leaf plots and dot the use of digital technology plots **Learning Journeys** Interpreting a variety of different graphs • interpret a variety of graphs, including dot plots, stem-andleaf plots, divided bar graphs, sector graphs and line graphs SP.A.4 Construct and calculate the percentage of the whole represented by Interpreting a variety of compare a range different categories in a divided bar graph or sector graph graphs, including dot plots, of data displays, stem-and-leaf plots, divided • draw conclusions from data displayed in a graph, eg 'The including stem-andbar graphs, sector graphs and graph shows that the majority of Year 8 students who play a leaf plots and dot line graphs musical instrument play a string instrument' plots • critique ways in which data is presented in sector graphs, line graphs, bar graphs and pictographs **Quest: Analysing single sets of data Learning Journeys** Calculating the mean calculate the mean of a set of data using mean = sum of data values/number of data values Calculating the mean of a set of SP.B.1 Calculate mean, recognise that the mean is often referred to as the 'average' in 1 data using mean = sum of data median, mode and everyday language values/number of data values range for sets of identify that the bar notation represents the mean score for a data and interpret set of data (x ) these statistics in the Using the statistical functions context of data use the statistical functions of a spreadsheet to determine the 2 of a spreadsheet to determine mean for large sets of data the mean for large sets of data Learning Journeys Median mode and range determine the median for sets of data without the use of Determining the median for SP.B.1 Calculate mean, digital technology and containing an odd number of scores 1 sets of data without the use of median, mode and determine the median for sets of data without the use of digital technology range for sets of digital technology and containing an even number of scores data and interpret Determining the mode for these statistics in the determine the mode for sets of data without the use of digital 2 sets of data without the use of context of data technology



## **Understanding Practice and Fluency (UPF)**

### **Measurement and Geometry**

MA4-18MG identifies and uses angle relationships, including those related to transversals on sets of parallel

MA4-18MG identifies and uses angle relationships, including those related to transversals on sets of parallel lines					
Quest: Analysing single sets of data					
		Learning Journeys M	edian mode and range		
Content Descriptor	Steps	Spine Nodes	Subnodes		
SP.B.1 Calculate mean, median, mode and	3	Determining the range for sets of data without the use of digital technology	determine the range for sets of data without the use of digital technology		
range for sets of data and interpret these statistics in the context of data	4	Determining the median, mode and range for sets of data using digital technology	<ul> <li>determine the median, mode and range for sets of data using digital technology</li> <li>use the statistical functions of a spreadsheet to determine the median, mode and range for large sets of data</li> </ul>		
SP.B.1 Calculate mean, median, mode and range for sets of data and interpret these statistics in the context of data	CLASSF	ROOM BASED			
		Learning Journeys Cluster	rs, gaps and outliers in data		
	1	Identifying any clusters, gaps and outliers in sets of data	<ul> <li>identify any clusters, gaps and outliers in sets of data</li> <li>identify any clusters, gaps and outliers in sets of data when represented in different displays</li> </ul>		
SP.B.2 Investigate the effect of individual data values, including outliers, on the mean and median	2	Investigating the effect of outliers on the mean, median, mode and range by considering a small set of data and calculating each measure, with and without the inclusion of an outlier	<ul> <li>investigate the effect of outliers on the mean, median, mode and range by considering a small set of data and calculating each measure, with and without the inclusion of an outlier</li> <li>explain why it is more appropriate to use the median than the mean when the data contains 1 or more outliers</li> <li>determine situations when it is more appropriate to use the median or mode, rather than the mean, when analysing data, eg median for property prices, mode for shoe sizes</li> </ul>		
L	.earnin	g Journeys Using mean, me	dian, mode to analyse data displays		
SP.B.3 Describe and interpret data displays using mean, median and range	1	Calculating measures of location (mean, median and mode) and the range for data represented in a variety of statistical displays, including frequency distribution tables, frequency histograms, stemand-leaf plots and dot plots	Calculating measures of location (mean, median and mode) and the range for data represented in a variety of statistical displays, including frequency distribution tables, frequency histograms, stem-and-leaf plots and dot plots		
	2	Drawing conclusions based on the analysis of data displays using the mean, median and/or mode, and range	<ul> <li>draw conclusions based on the analysis of data displays using the mean, median and/or mode, and range</li> </ul>		
SP.B.4 Explore the variation of means and proportions of random samples drawn from the same population	CLASSROOM BASED				



## **Understanding Practice and Fluency (UPF)**

	MA4-2	21SP represents probabilities of	f simple and compound events		
Quest: Understanding probability					
		Learning Journeys Language	of chance experiments		
Content Descriptor	Steps	Spine Nodes	Subnodes		
SP.C.1 Construct sample spaces for single-step experiments with equally likely outcomes	1	Understanding the language around chance	<ul> <li>understand that the term 'chance experiment' is used when referring to actions such as tossing a coin, rolling a dice or randomly selecting an object from a bag</li> <li>understand that the term 'outcome' is used to describe a possible result of a chance experiment and list all of the possible outcomes for a single-step experiment</li> <li>understand that the term 'sample space' is used to describe a list of all of the possible outcomes for a chance experiment</li> <li>use the term 'probability' to describe the numerical value that represents the likelihood of an outcome of a chance experiment</li> <li>arrange the likelihood of chance experiment outcomes in order from least likely to most likely (and vice versa)</li> </ul>		
		Learning Journeys	Sample spaces		
	1	Identifying equally likely outcomes in single-step chance experiments	identify equally likely outcomes in single-step chance experiments		
SP.C.1 Construct sample spaces for single-step experiments with equally likely outcomes	2	Identifying the sample space for a probability experiment involving 1 event	identify the sample space for a probability experiment involving 1 event		
	3	Identifying the sample space for a probability experiment involving 2 independent events	identify the sample space (where the combined sample space has 36 or fewer elements) for a probability experiment involving 2 independent events		
	4	Listing the outcomes for chance experiments where the outcomes are not equally likely to occur and assign probabilities to the outcomes using fractions	list the outcomes for chance experiments where the outcomes are not equally likely to occur and assign probabilities to the outcomes using fractions		
		<b>Learning Journeys</b> Cha	ance experiments		
SP.C.1 Construct sample spaces for single-step experiments with equally likely outcomes	1	Describing single-step chance experiments in which the outcomes are equally likely	<ul> <li>describe single-step chance experiments in which the outcomes are equally likely</li> <li>use the terms 'chance experiment', 'outcome' and 'sample space' appropriately for experiments in which the outcomes are equally likely</li> </ul>		
	2	Describing single-step chance experiments in which the outcomes are equally and not equally likely	<ul> <li>describe single-step chance experiments in which the outcomes are equally and not equally likely</li> <li>use the terms 'chance experiment', 'outcome' and 'sample space' appropriately for experiments in which the outcomes are equally and not equally likely</li> </ul>		
	3	Creating and conducting a chance experiment given equally probable events	<ul> <li>create a chance experiment given equally probable events</li> <li>determine the theoretical probability of a series of events using tree diagrams</li> <li>conduct the chance experiment with both small and large numbers of trials using digital technologies</li> <li>compare the expected probabilities with the observed probabilities after both small and large numbers of trials for the chance experiment given equally probable events</li> </ul>		



# **Understanding Practice and Fluency (UPF)**

MA4-21SP represents probabilities of simple and compound events					
Quest: Understanding probability					
		<b>Learning Journeys</b> Cha	ance experiments		
Content Descriptor	Steps	Spine Nodes	Subnodes		
SP.C.1 Construct sample spaces for single-step experiments with equally likely outcomes	4	Creating and conducting a chance experiment given unequally probable events	<ul> <li>determine the theoretical probability of a series of unequally probable events using tree diagrams</li> <li>compare the expected probabilities with the observed probabilities after both small and large numbers of trials, given unequally probable events</li> </ul>		
		<b>Learning Journeys</b> Lang	uage of probability		
	1	Recognising that a probability of 0 is for events that are impossible and a probability of 1 for events that are certain to occur	recognise that a probability of 0 is for events that are impossible and a probability of 1 for events that are certain to occur		
SP.C.2 Assign probabilities to the outcomes of events	2	Relating calculated probabilities with the language of chance and the likelihood number line	relate calculated probabilities with the language of chance and the likelihood number line		
and determine probabilities for events	3	Assigning numerical probabilities with their associated language	<ul> <li>assign language such as impossible, highly unlikely, unlikely, even chance, likely, highly likely and certain to the known probabilities of outcomes occurring</li> <li>allocate words such as impossible, highly unlikely, unlikely, even chance, likely, highly likely and certain along a number line from 0 to 1 representing their respective probabilities</li> </ul>		
		Learning Journeys Understa	nding basic probability		
	1	Explaining the meaning of 0, 1/2 and 1 in a given chance situation, using the language of chance	explain the meaning of 0, 1/2 and 1 in a given chance situation, using the language of chance		
	2	Applying probabilities to simple events by reasoning about equally likely outcomes	apply probabilities to simple events by reasoning about equally likely outcomes		
SP.C.2 Assign probabilities to the outcomes of events and determine probabilities for events	3	Expressing the theoretical probability of an event formally	express the theoretical probability of an event, given a number of equally likely outcomes in the sample space, as P(event) = number of favourable outcomes ÷ total number of outcomes		
		Expressing probabilities as decimals, fractions and percentages	express probabilities as decimals, fractions and percentages		
		Interpreting probabilities expressed as fractions, percentages or decimals	interpret probabilities expressed as fractions, percentages or decimals		
	5	Calculating the probability of an event of a single-step experiment using cards, dice, spinners, etc	calculate the probability of an event of a single-step experiment using cards, dice, spinners, etc		



# **Understanding Practice and Fluency (UPF)**

	MA4-2	21SP represents probabilities of sir	mple and compound events		
		Quest: Understanding	probability		
Learning Journeys Complementary events					
Content Descriptor	Steps	Spine Nodes	Subnodes		
	1	Understanding the term 'complement' to describe events that are mutually exclusive and add to 1	understand the term 'complement' to describe events that are mutually exclusive and add to 1		
SP.C.3 Identify complementary events and use the sum of probabilities to	2	Finding the complement of an event	• find the probability of the complement of an event by using the fact that the sum of the probabilities of an event and its complement is 1		
solve problems	3	Identifying the complementary event for a given event, and calculating the theoretical probability that a given event will not occur	<ul> <li>identify the complementary event for given event, and calculate the theoretical probability that a given event will not occur</li> <li>describe in words the complement of an event</li> </ul>		
	Lea	arning Journeys Language of prob	·		
SP.C.4 Describe events using language of 'at least', exclusive 'or' (A or B but not both), inclusive 'or' (A or B or both) and 'and'	1	Describing events using language of 'at least', exclusive 'or' (A or B but not both), inclusive 'or' (A or B or both) and 'and' ( both A and B)	<ul> <li>describe events using language of 'at least', exclusive 'or' (A or B but not both), inclusive 'or' (A or B or both) and 'and' (both A and B)</li> <li>recognise the difference between mutually exclusive and non-mutually exclusive events</li> </ul>		
	2	Describing compound events using the terms 'at least', 'at most', 'not' and 'and'	describe compound events using the terms 'at least',     'at most', 'not' and 'and'		
	3	Posing problems that involve the use of the terms 'at least', 'at most', 'not', 'and' and solve problems posed by others	<ul> <li>pose problems that involve the use of the terms 'at least', 'at most', 'not', 'and'</li> <li>solve problems posed by others that involve the use of the terms 'at least', 'at most', 'not', 'and'</li> </ul>		
	4	Understanding the effect of the use of 'and' and 'or' when using internet search engines	understand the effect of the use of 'and' and 'or' when using internet search engines		
		Classifying compound events	<ul> <li>classify compound events using inclusive 'or' and exclusive 'or'</li> <li>recognise that the word 'or' on its own often needs a qualifier, such as 'both' or 'not both', to determine inclusivity or exclusivity</li> </ul>		
	Learr	ning Journeys Understanding and	contructing Venn diagrams		
SP.C.5 Represent events in two-way tables and Venn diagrams and solve	1	Interpreting Venn diagrams involving two or three mutually exclusive attributes	<ul> <li>interpret Venn diagrams involving two or three mutually exclusive attributes</li> <li>describe regions in Venn diagrams representing</li> </ul>		
	2	Interpreting Venn diagrams involving two or three non- mutually exclusive attributes	<ul> <li>mutually exclusive attributes</li> <li>interpret Venn diagrams involving two or three non-mutually exclusive attributes</li> <li>describe individual regions or combinations of regions in Venn diagrams representing non-mutually exclusive attributes, using the language 'and', exclusive 'or', inclusive 'or', 'neither' and 'not'</li> </ul>		
related problems		Representing events in Venn diagrams	represent events of 2 or 3 attributes using Venn diagrams		
	3	Constructing Venn diagrams to represent all possible combinations of 2 attributes from given or collected data	construct Venn diagrams to represent all possible combinations of 2 attributes from given or collected data		



# **Understanding Practice and Fluency (UPF)**

MA4-21SP represents probabilities of simple and compound events						
	Quest: Understanding probability					
	L	earning Journeys Using Venn diag	grams to solve problems			
Content Descriptor	Steps	Spine Nodes	Subnodes			
SP.C.5 Represent	1	Using data presented in venn diagrams to answer problems, including probability questions	use data presented in venn diagrams to answer problems, including probability questions			
events in two-way tables and Venn	2	Using given data to calculate missing values in a Venn diagram	use given data to calculate missing values in a Venn diagram			
diagrams and solve related problems	3	Using data presented in venn diagrams to answer problems where missing values must first be found, including probability questions	use data presented in venn diagrams to answer problems where missing values must first be found, including probability questions			
	Lea	rning Journeys Interpreting and c	onstructing two-way tables			
	1	Interpreting given two-way tables representing non-mutually exclusive attributes	<ul> <li>interpret given two-way tables representing non-mutually exclusive attributes</li> <li>describe relationships displayed in two-way tables using the language 'and', exclusive 'or', inclusive 'or', 'neither' and 'not'</li> </ul>			
SP.C.5 Represent events in two-way	2	Constructing two-way tables to represent the relationships between attributes	construct two-way tables to represent the relationships between attributes			
tables and Venn diagrams and solve related problems	3	Using data presented in two-way tables to answer problems, including probability questions	use data presented in a two-way table to answer problems, including probability questions			
	4	Using given data to calculate missing values in a two-way table	use given data to calculate missing values in a two-way table			
	5	Using data presented in two-way tables to answer problems where missing values must first be found, including probability questions	use data presented in two-way tables to answer problems where missing values must first be found, including probability questions			
Learning Journeys Two-way tables and Venn diagrams						
SP.C.5 Represent events in two-way tables and Venn diagrams and solve related problems	1	Converting between representations of the relationships between 2 attributes in Venn diagrams and twoway tables	convert between representations of the relationships between 2 attributes in Venn diagrams and two-way tables			



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